

Search for $\tau \rightarrow 3\mu$ at Belle II

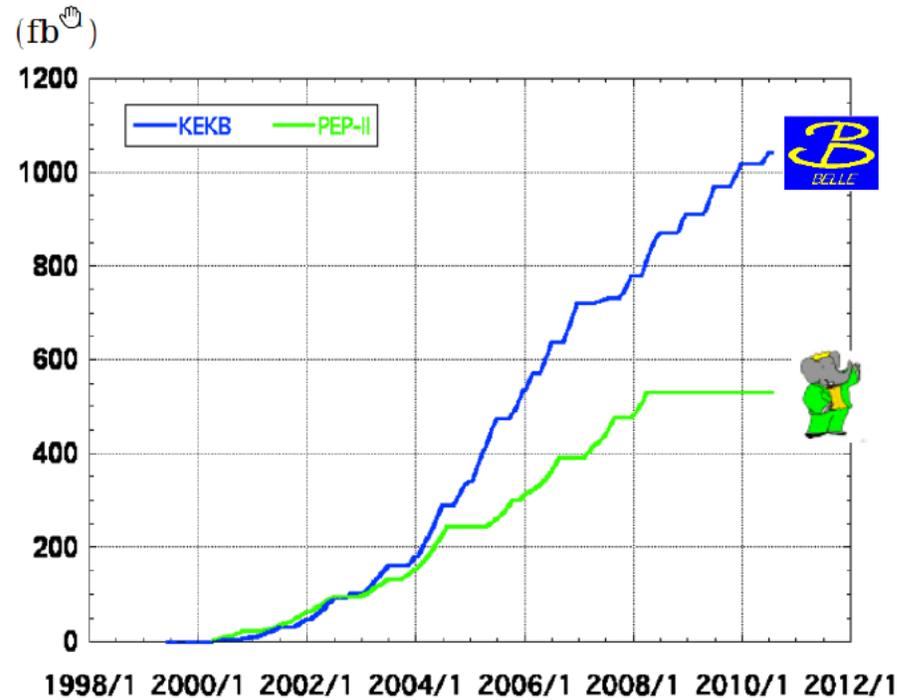
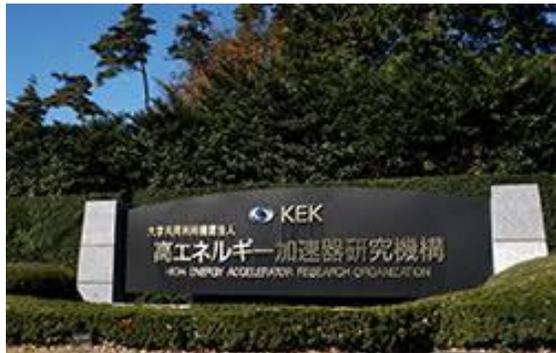
Justine Serrano
Aix Marseille Univ, CNRS/IN2P3, CPPM
On behalf of the Belle II Collaboration

Topical workshop on LFV decays of the tau
Orsay, April 11th 2024



Back in the 2000s : Belle and Babar era

Belle at KEKB
Japan



> 1 ab^{-1}

On resonance:

$\Upsilon(5S)$: 121 fb^{-1}

$\Upsilon(4S)$: 711 fb^{-1}

$\Upsilon(3S)$: 3 fb^{-1}

$\Upsilon(2S)$: 25 fb^{-1}

$\Upsilon(1S)$: 6 fb^{-1}

Off reson./scan:

$\sim 100 \text{ fb}^{-1}$

$\sim 550 \text{ fb}^{-1}$

On resonance:

$\Upsilon(4S)$: 433 fb^{-1}

$\Upsilon(3S)$: 30 fb^{-1}

$\Upsilon(2S)$: 14 fb^{-1}

Off resonance:

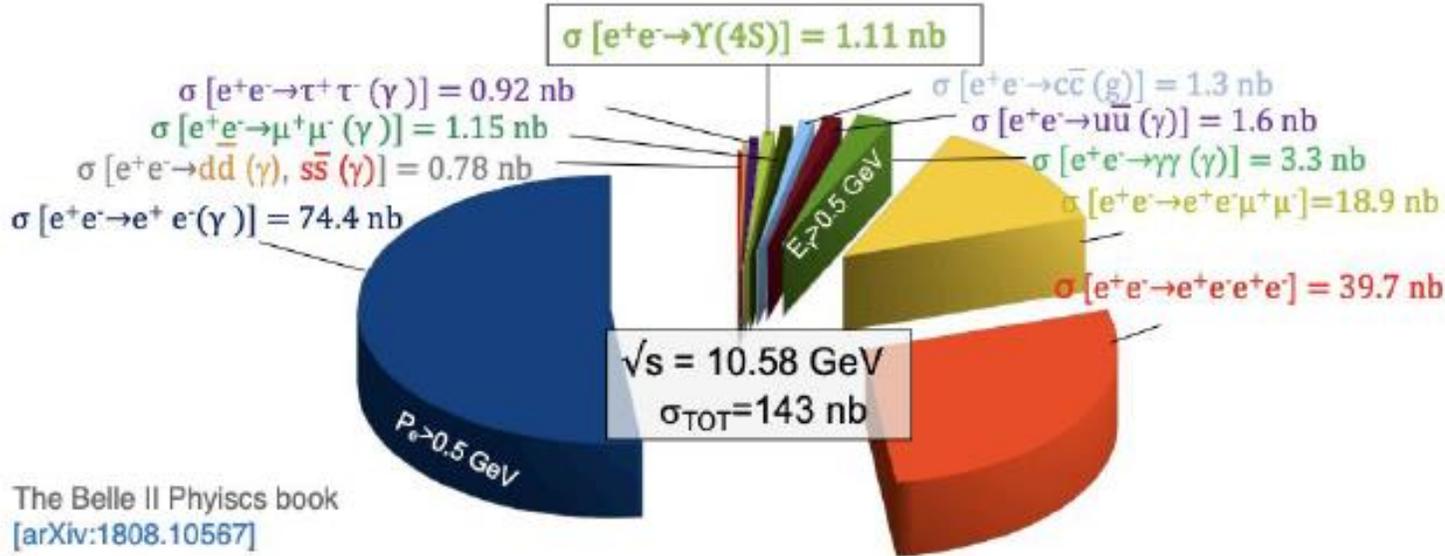
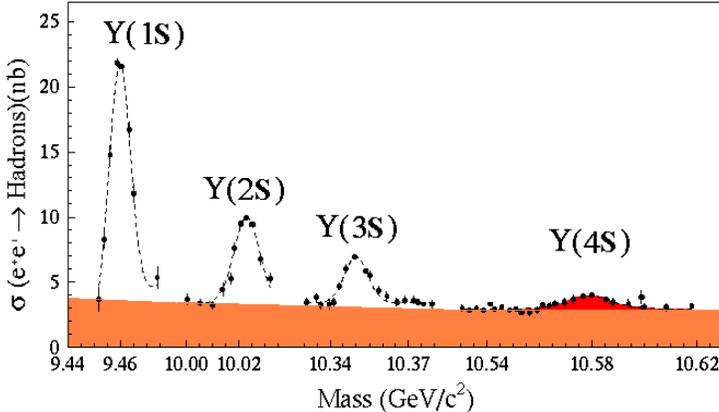
$\sim 54 \text{ fb}^{-1}$

Babar at PEP-II
California

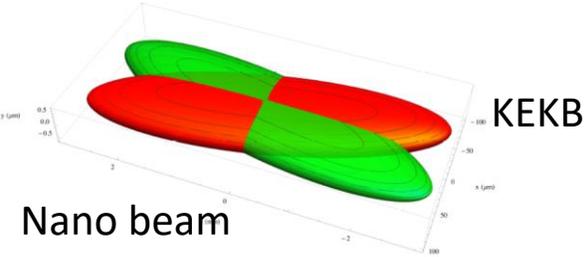
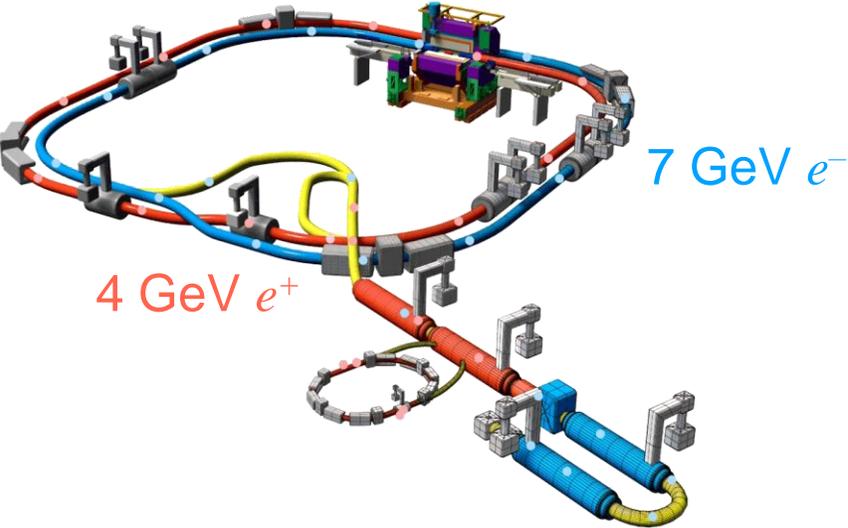


Physics processes at B-factories

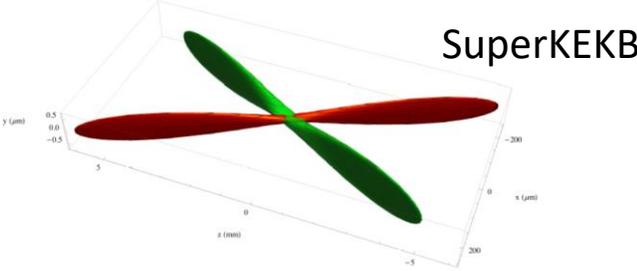
- e^+e^- collider, mainly working at the $Y(4S)$ energy which produce pairs of B^+B^- and (quantum correlated) $B^0\bar{B}^0$
- Asymmetric beams \rightarrow study time dependent effects in B hadron decays
- Also τ /charm factory (similar cross section as B)!



Back to the future: SuperKEKB and Belle II



Nano beam scheme technology ↓



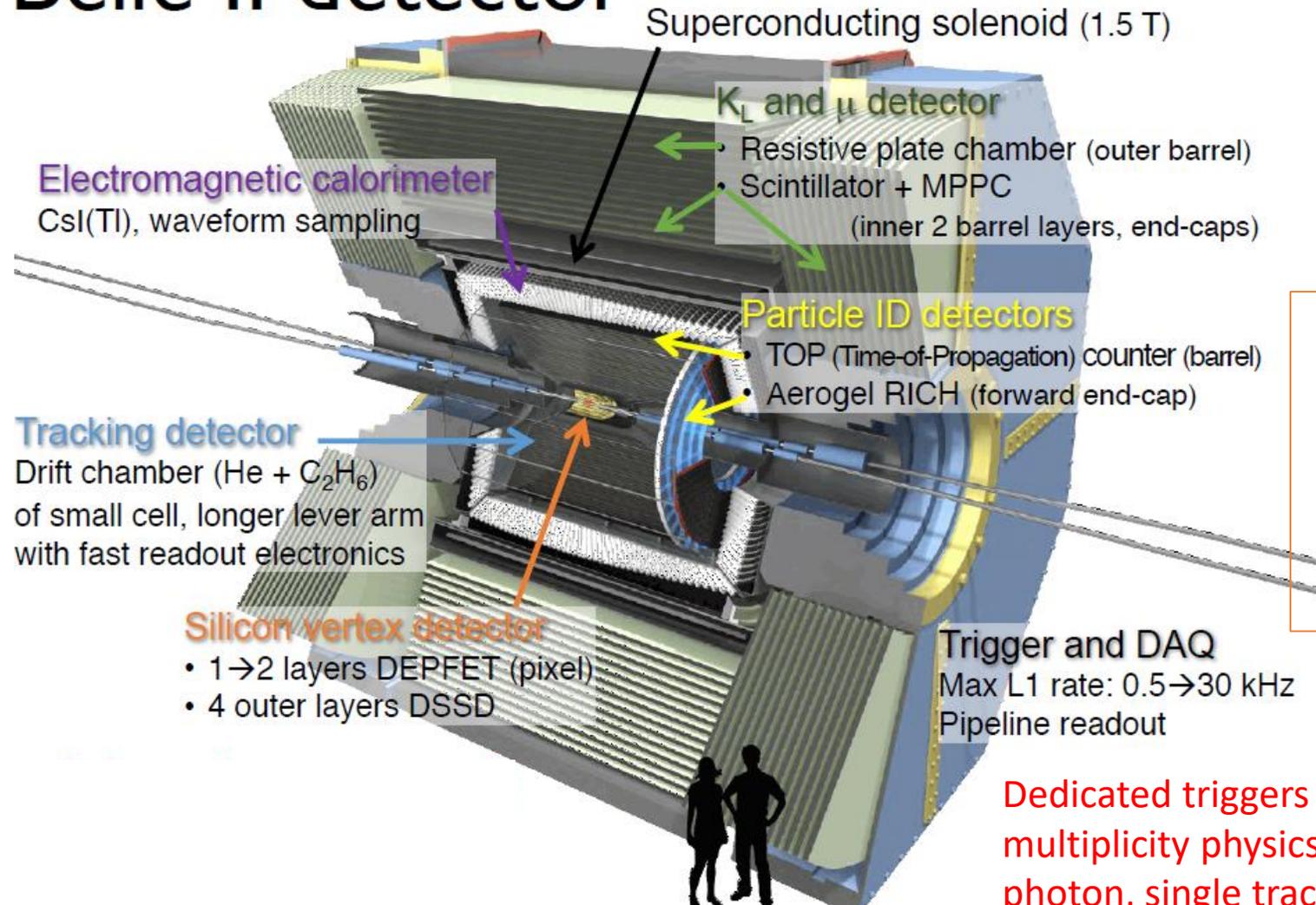
	KEKB	SuperKEKB
Energy (GeV) LER/HER	3.5/8	4/7
Current (A) LER/HER	1.6/1.2	2.8/2.0
β_y^* (mm)	5.9	0.3
Inst. Lumi ($\text{cm}^{-2}/\text{s}^{-1}$)	2.1×10^{34}	6×10^{35}

$$L = \frac{\gamma_{\pm}}{2e r_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{y\pm}}{\beta_{y\pm}^*} \left(\frac{R_L}{R_{\xi}} \right)$$

Lorentz factor γ_{\pm} , beam current I_{\pm} , beam-beam parameter $\xi_{y\pm}$, geometrical reduction factors R_L/R_{ξ} , beam aspect ratio at the IP σ_y^*/σ_x^* , vertical beta-function at the IP $\beta_{y\pm}^*$.

Belle II detector

3



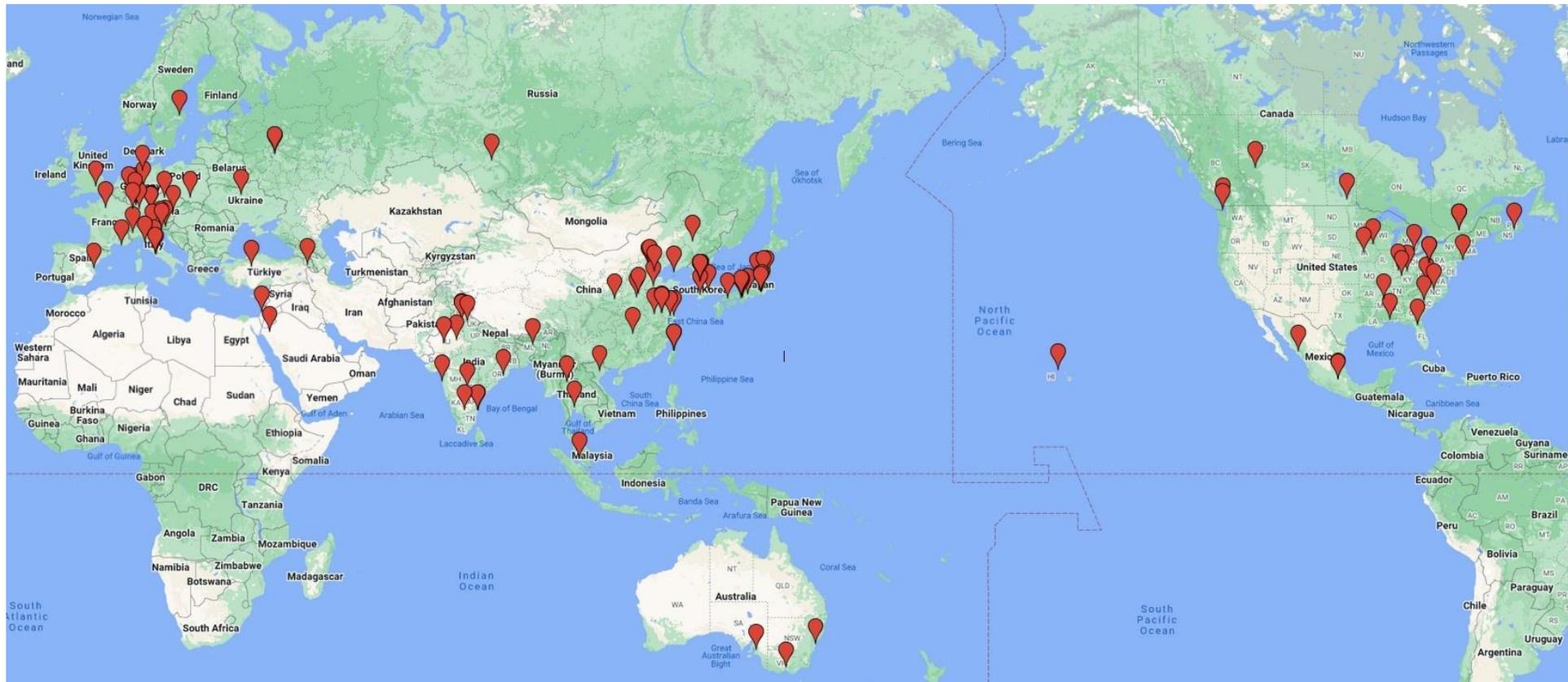
Advantage for τ studies:

- almost hermetic detector + well defined initial state energy = measurement of missing energy
- Clean environment
- excellent PID for e and μ

Dedicated triggers for low multiplicity physics: single-photon, single track, two-track, ..

Belle II collaboration

- About 1100 physicists from 120 countries



Experiment status

Run1 end 2019-mid 2022 with complete detector (except for PXD layer 2)

Long shutdown 1 mid 2022 – beginning 2024 : improvements on accelerator and installation of complete pixel detector

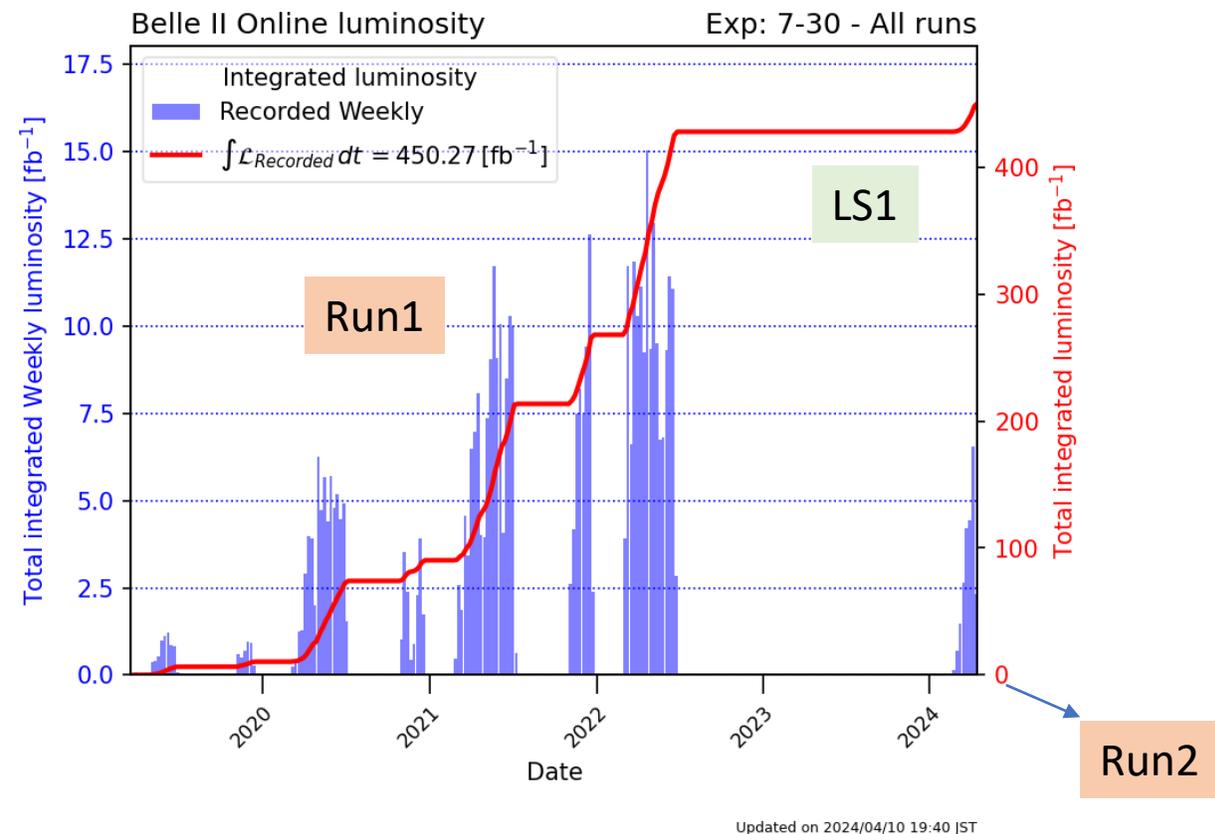
Run2 started February 2024

Achieved so far:

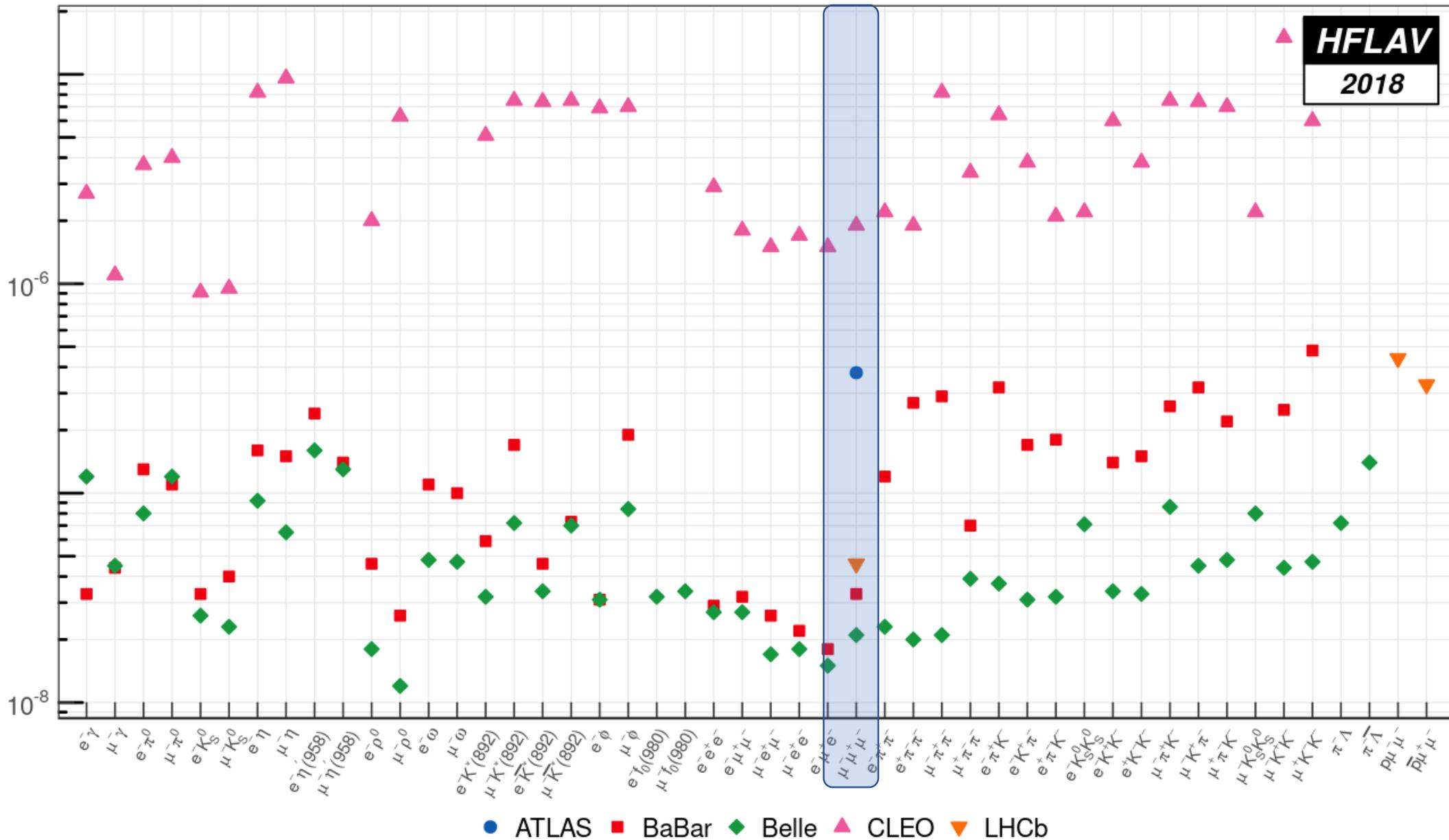
- World record of instantaneous lumi at $4.7 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Recorded 450 fb^{-1} since 2019
- The analysis presented here is based on Run1 data (424 fb^{-1} among which 362 fb^{-1} at Y(4S))

Main limitations to the luminosity during Run1:

- Shorter beam lifetime (sudden beam losses) and lower bunch-current limit than expected
- Beam beam effects
- Low machine operation efficiency



90% CL upper limits on τ LFV decays

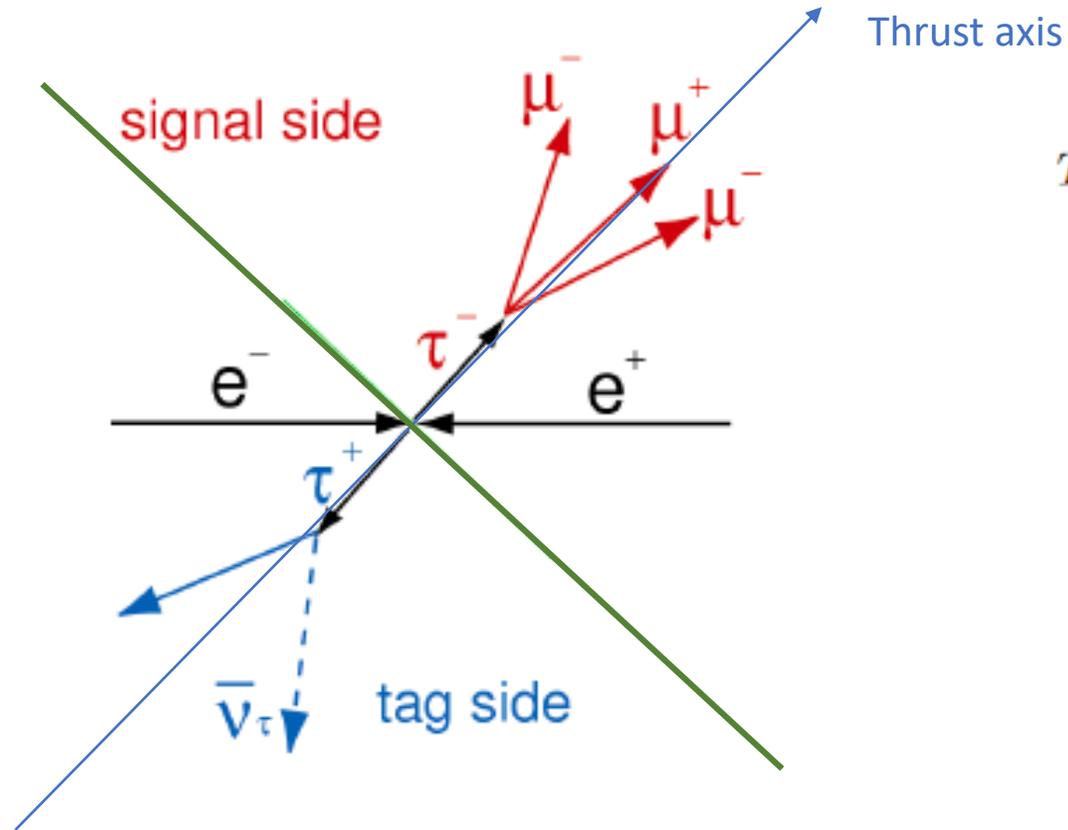


τ LFV searches at B factories

Historical approach uses a **full reconstruction** of the event:

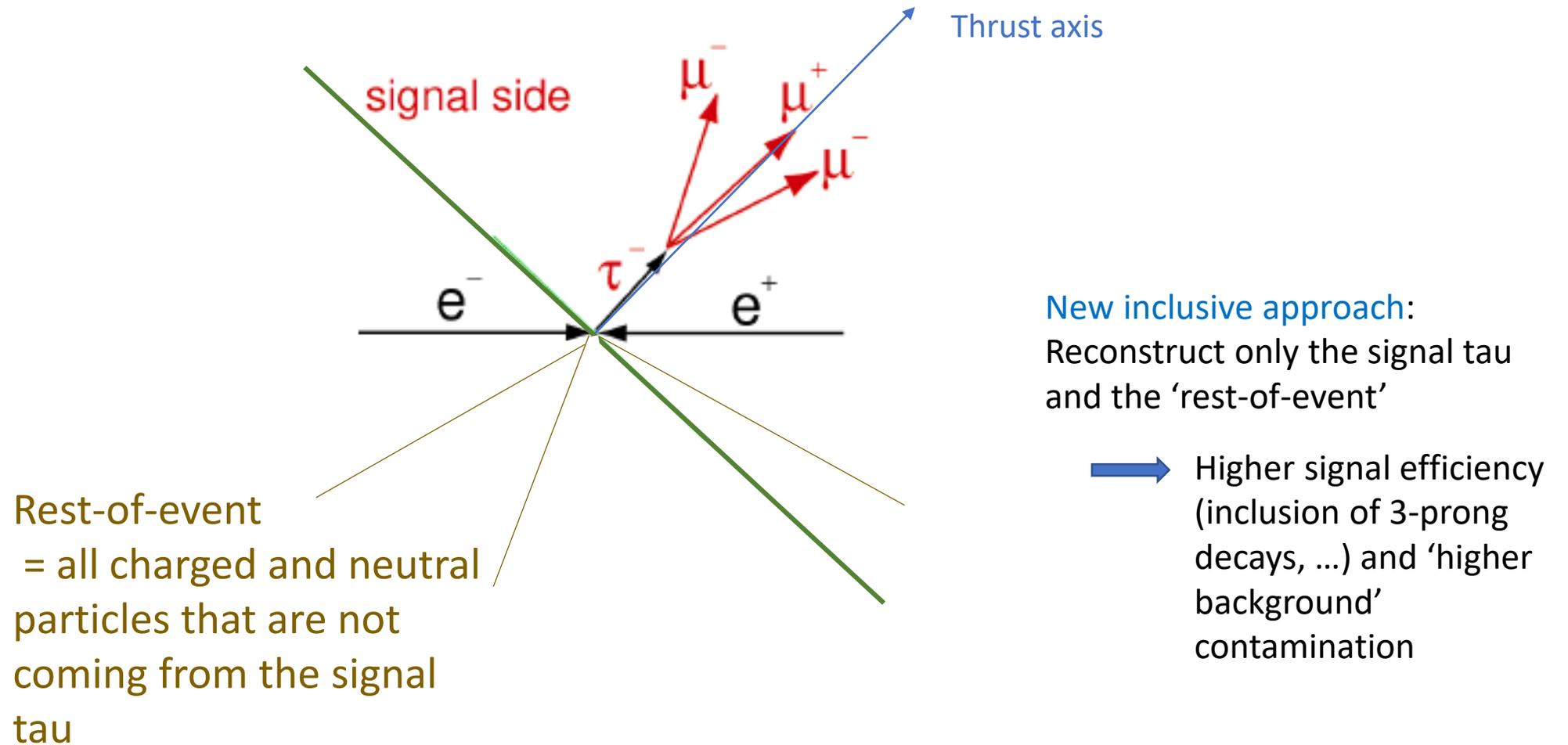
- Signal side $\tau \rightarrow 3l$
- Tag side: $\tau \rightarrow e/\mu/\pi/\rho (+\nu\text{'s})$

→ Require exactly 4 tracks in the event following the '3x1 topology'



$$T = \max_{\hat{n}_T} \left(\frac{\sum_i |\mathbf{p}_i^* \cdot \hat{n}_T|}{\sum_i |\mathbf{p}_i^*|} \right),$$

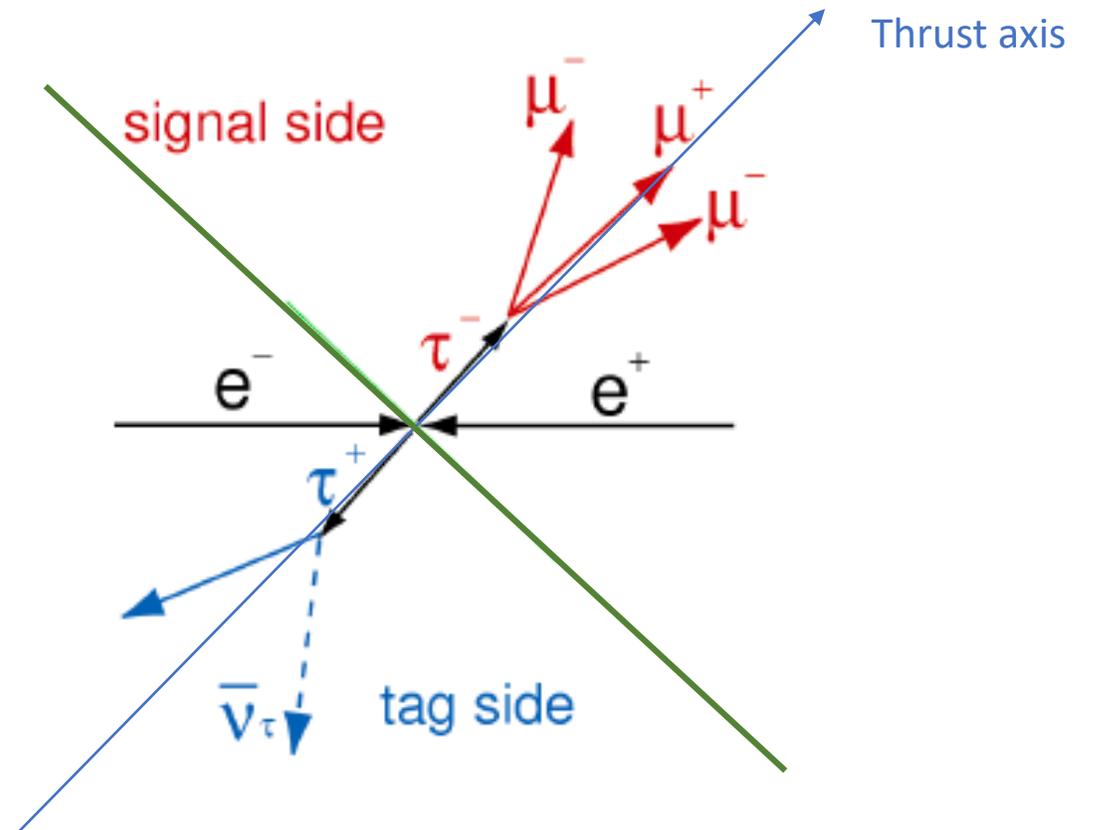
τ LFV searches at B factories



$\tau \rightarrow 3\mu$ selection

Signal selection:

- Require **3 muons** well identified in the same hemisphere
- They should come from the interaction point $|dz| < 3\text{cm}$, $|dr| < 1\text{ cm}$
- Events should pass the L1 triggers based on ECL or CDC (~95% efficiency)



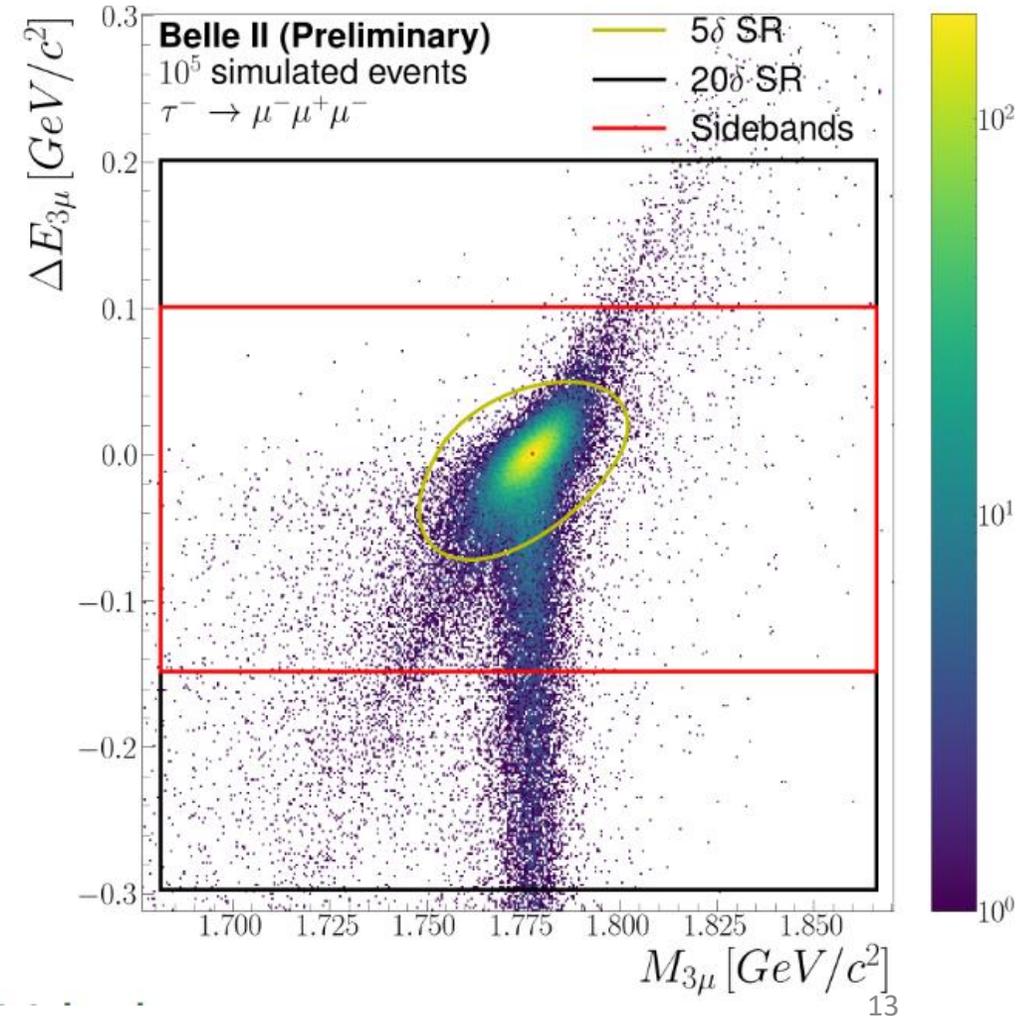
$\tau \rightarrow 3\mu$ selection

Signal selection:

- Require **3 muons** well identified in the same hemisphere
- They should come from the interaction point $|dz| < 3\text{cm}$, $|dr| < 1\text{cm}$
- Events should pass the L1 triggers based on ECL or CDC (~95% efficiency)

Define **2D plane** made of $M_{3\mu}$ and $\Delta E_{3\mu} = E_{\tau}^* - \sqrt{s}/2$

- Signal peaks in $M_{3\mu} = 1.777\text{ GeV}/c^2$ and $\Delta E_{3\mu} = 0$, with tails due to ISR and FSR
- Obtain resolutions δ fitting the signal simulation
- Define the **signal region** as ellipse of $\pm 5\delta$, **blinded**
- Define the **sideband region** as box of $\pm 10\delta$ in $\Delta E_{3\mu}$ and $\pm 20\delta$ in $M_{3\mu}$, used to check data/MC agreement



Backgrounds

Main background contributions :

- $e^+e^- \rightarrow qq$ ($q=u,d,c,s$)
- $e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, e^+e^-\mu^+\mu^-, \mu^+\mu^-\mu^+\mu^-$
- $e^+e^- \rightarrow \tau^+\tau^-$
- Other (non simulated) low multiplicity events

Backgrounds

Main background contributions :

- $e^+e^- \rightarrow qq$ ($q=u,d,c,s$)
- $e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, e^+e^-\mu^+\mu^-, \mu^+\mu^-\mu^+\mu^-$
- $e^+e^- \rightarrow \tau^+\tau^-$
- Other (non simulated) low multiplicity events

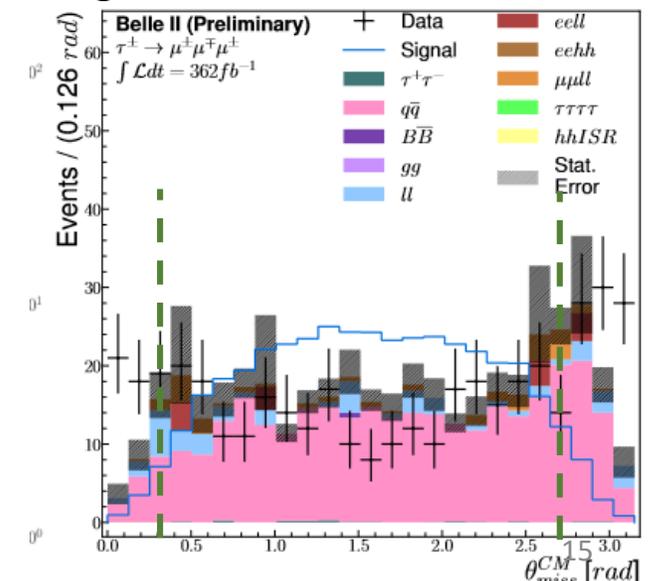
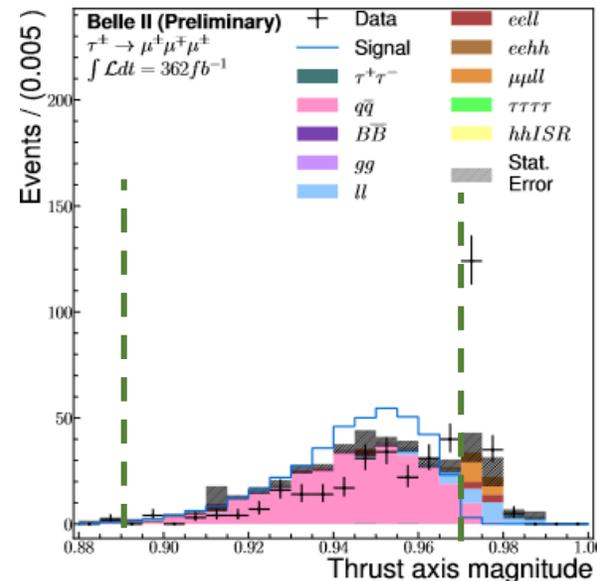
Most of backgrounds corresponds to pions/kaons/electrons misidentified as muons

➡ Tighten muon identification criteria for 2 muons out of the 3

Low multiplicity backgrounds have high thrust values and missing momentum pointing towards the beam axis:
 $0.89 < T < 0.97$ and $0.3 < \theta_{\text{miss}}^* < 2.7$

Main remaining background events after selection are $e^+e^- \rightarrow qq$

Data in SB region



BDT selection

Train a BDT against qq and $\tau\tau$ events using simulation equivalent to 4 ab-1 for the background (3400 events), and 176k signal events:

- Use **32 input variables** based on
 - Signal τ properties : muon p_T , flight time, isolation,...
 - ROE properties : mass, ΔE , thrust axis,...
 - Event properties: tracks and photons multiplicities, thrust, missing momentum related variables,...
- BDT based on XGBoost library, hyperparameters optimized with Optuna
- Use k-folding to reduce sensitivity to fluctuations

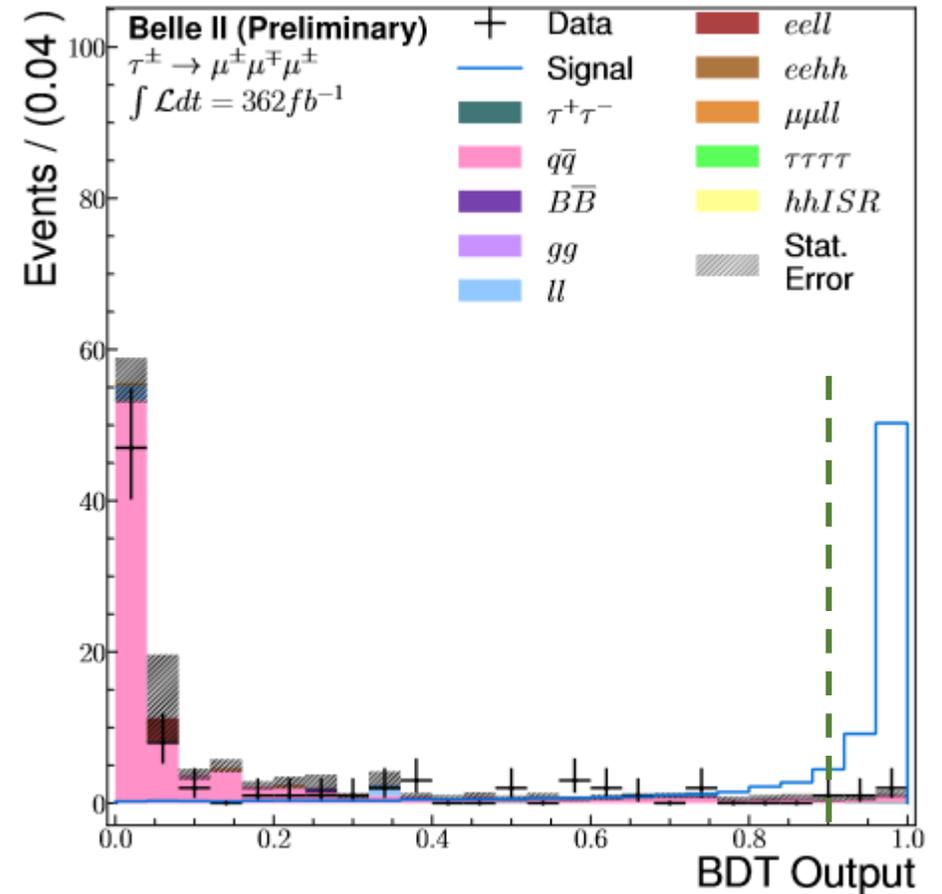
Final selection on BDT output optimize according to Punzi FOM :
BDT > 0.9

$$\frac{\epsilon_{3\mu}}{\alpha/2 + \sqrt{B}}$$

3σ significance $\alpha=3$

Number of expected background

Data in SB region



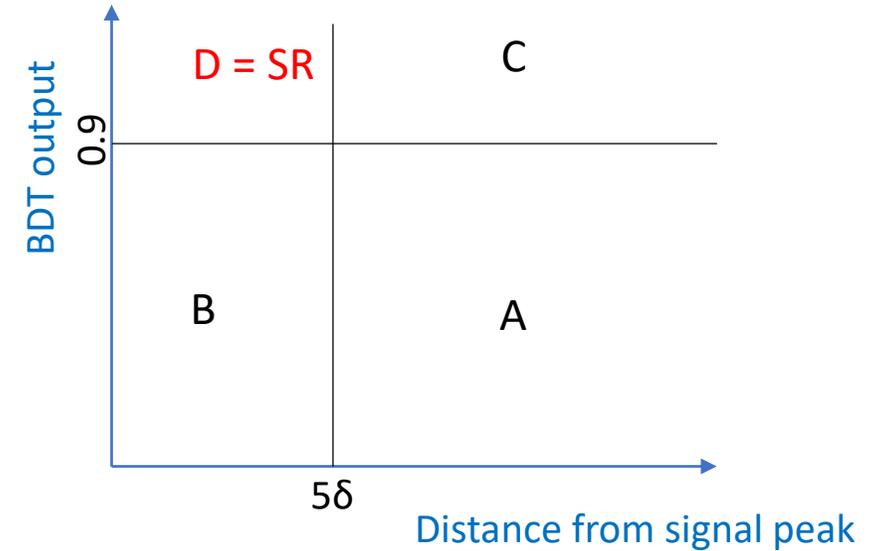
+ Final cut to require total charge=0

Expected background in SR and BR measurement

Use a data-driven method 'ABCD' based on 2 uncorrelated variables : BDT output and distance to the signal peak

$$ND = NB \times NC / NA = 0.5^{+1.4}_{-0.5}$$

Method validated with simulation

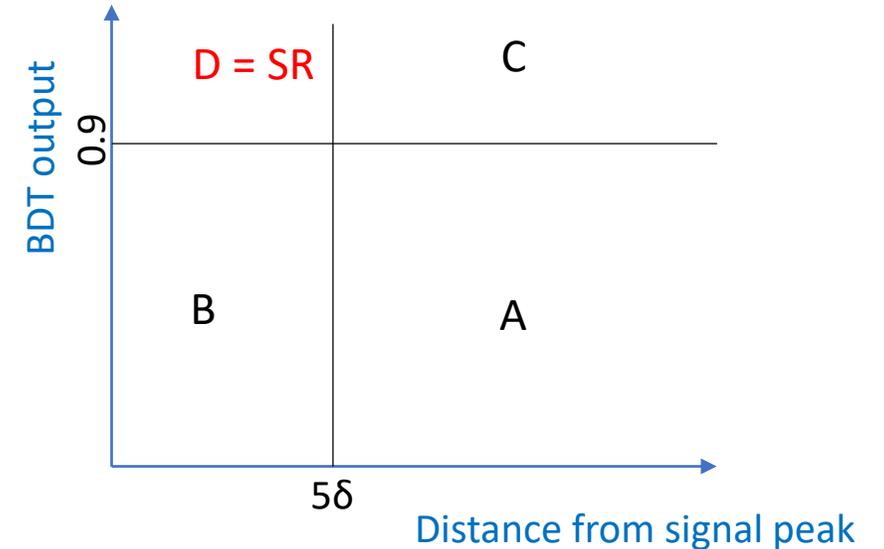


Expected background in SR and BR measurement

Use a data-driven method 'ABCD' based on 2 uncorrelated variables : BDT output and distance to the signal peak

$$ND = NB \times NC / NA = 0.5^{+1.4}_{-0.5}$$

Method validated with simulation



Systematic uncertainties:

Quantity	Source	Uncertainty (%)	
		Low	High
$\epsilon_{3\mu}$	PID	2.1	2.4
	Tracking	1.0	1.0
	Trigger	0.9	0.9
	BDT	1.5	1.5
	Signal region	3.9	2.9
N_{exp}	Momentum Scale	16	16
\mathcal{L}		0.6	0.6
$\sigma_{\tau\tau}$		0.3	0.3

Branching fraction is then measured as

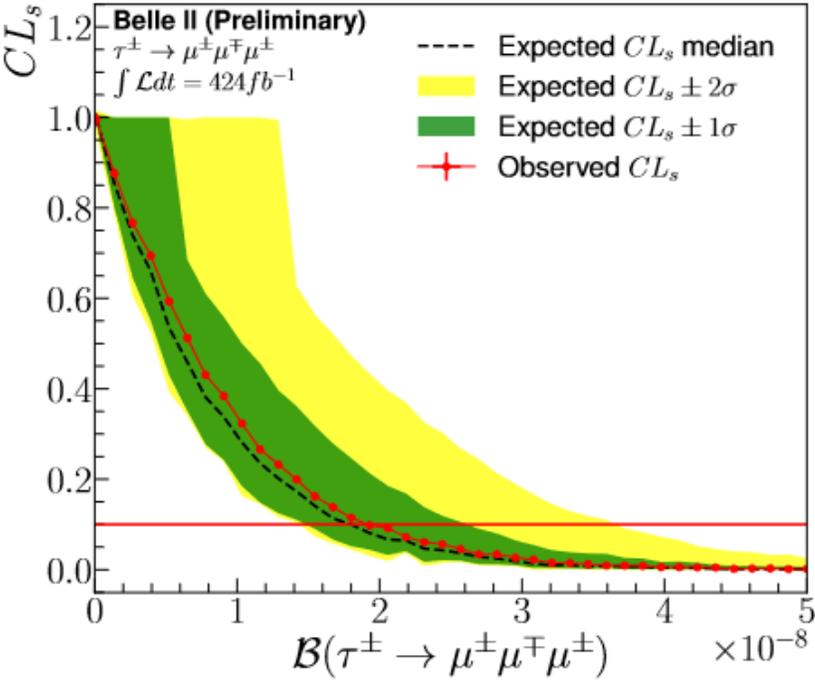
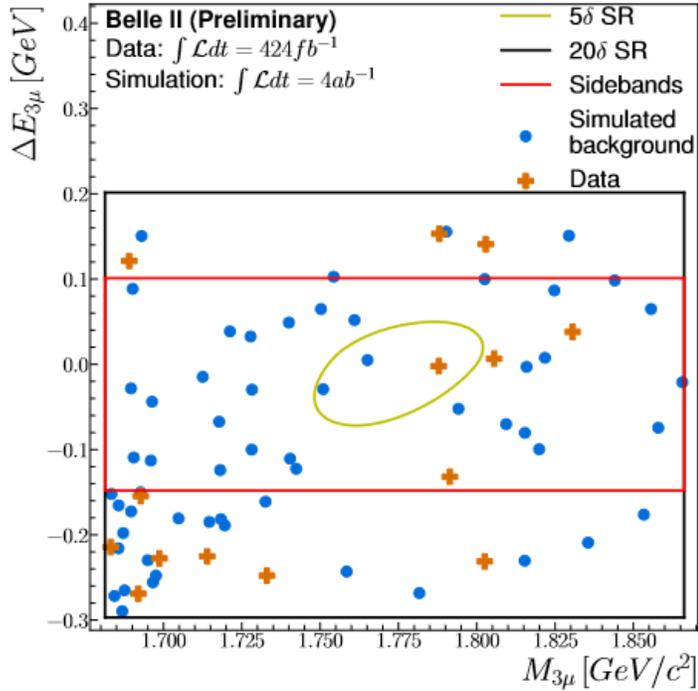
$$B(\tau^- \rightarrow \mu^- \mu^+ \mu^-) = \frac{N_{obs} - N_{exp}}{\mathcal{L} \times 2\sigma_{\tau\tau} \times \epsilon_{3\mu}}$$

$$N_{exp} = 0.5^{+1.4}_{-0.5}$$

$$\mathcal{L} = 424 \text{ fb}^{-1}, \sigma_{\tau\tau} = 0.919 \text{ nb}$$

$$\epsilon_{3\mu} = 20.4\% \text{ } 2.7x \text{ Belle efficiency}$$

Box opening and limit



We observe one event, compatible with bkg expectation

Limit at 90%CL:

Expected $B(\tau \rightarrow 3\mu) < 1.8 \times 10^{-8}$

Observed $B(\tau \rightarrow 3\mu) < 1.9 \times 10^{-8}$ **Most stringent limit!**

Belle with 782 fb ⁻¹			
B_{UL}	ϵ_{sig} (%)	N_{bkg}	N_{obs}
2.1×10^{-8}	7.6	0.13	0

Independent measurement with classical 3x1 selection

Signal selection:

- Require **3 muons** well identified in the same hemisphere and **1 prong** in the other hemisphere
- Cut-based selection optimized using the Punzi FOM

Signal efficiency: 14.9% (*2 x Belle efficiency*)

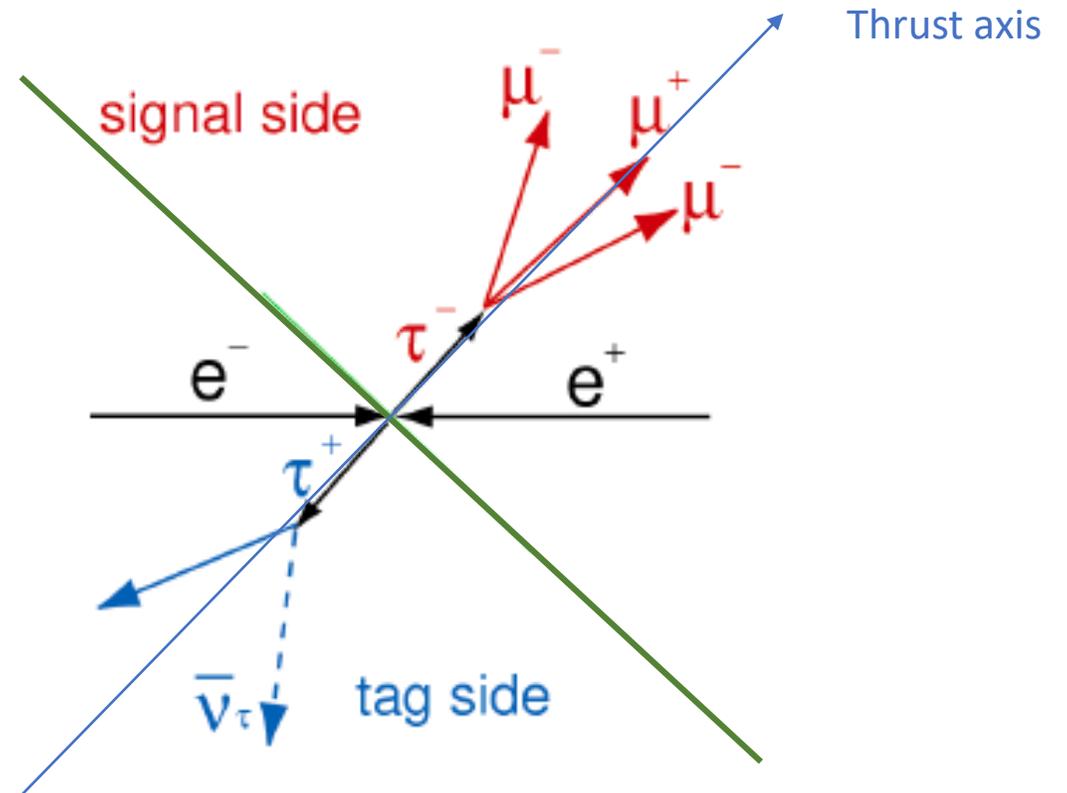
Number of expected background from simulation : 0.43

We observe 0 event, compatible with bkg expectation

Limit at 90%CL:

Expected $B(\tau \rightarrow 3\mu) < 2.0 \times 10^{-8}$

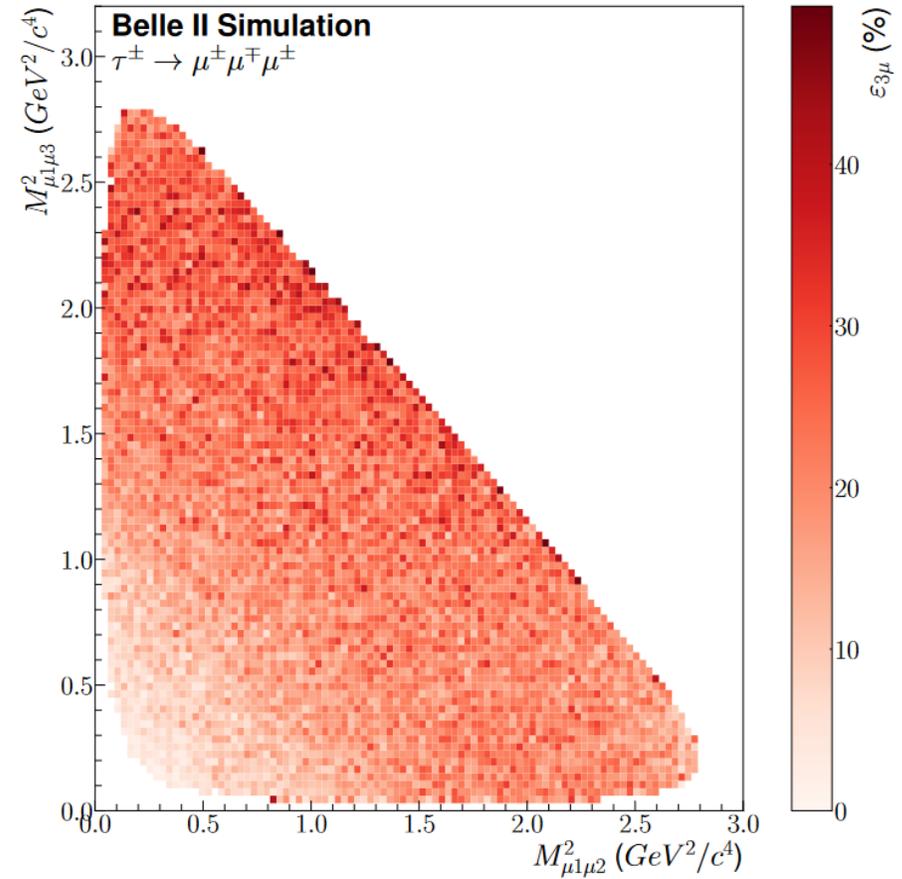
Observed $B(\tau \rightarrow 3\mu) < 2.0 \times 10^{-8}$



Additional information

We provide the efficiency as function of the Dalitz plane.

Is there anything else that can be useful to interpret the result ?



Summary and outlook

Belle II provided the most stringent limit on $B(\tau \rightarrow 3\mu)$ at 1.9×10^{-8} @90% CL

Improved performances wrt to Belle thanks to more optimal selection and use of inclusive tagging reconstruction

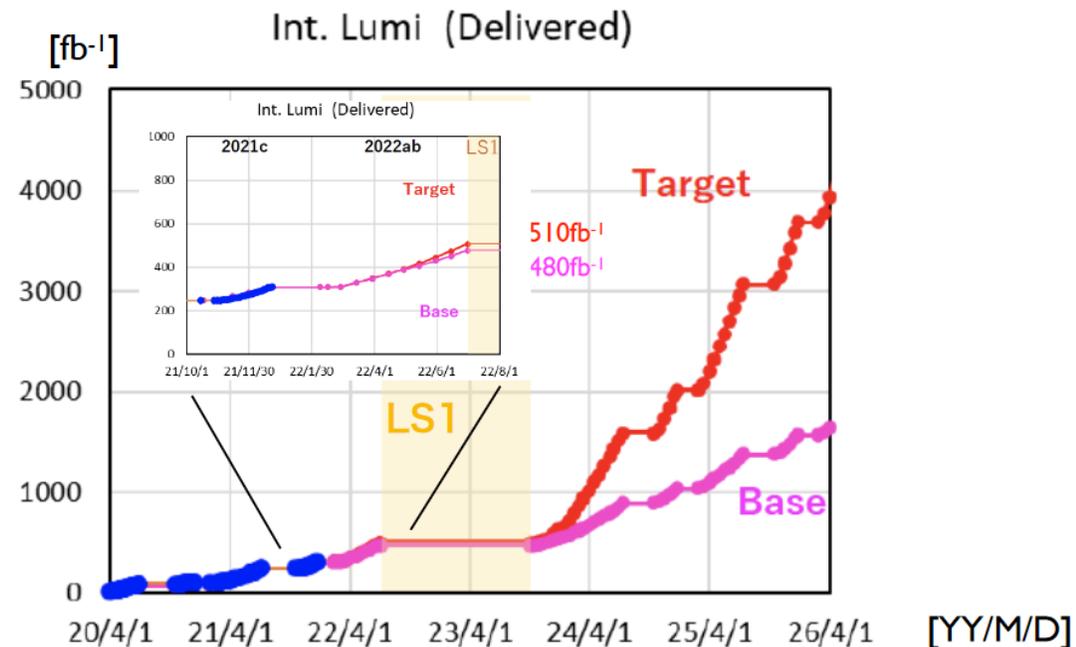
More results are coming based on Run1 data for the modes with electrons, stay tuned!

Belle II has recently resumed data taking, the goal is to reach an instantaneous luminosity of $10^{35}/\text{cm}^2/\text{s}$

Belle II dataset will increase up to few ab^{-1} in coming years

Target scenario: extrapolation from 2021 run including expected improvements.

Base scenario: conservative extrapolation of SuperKEKB parameters from 2021 run



Wide τ program at Belle II in the coming years

Precision test of SM

- Test of LFU: first result of $B(\tau \rightarrow \mu\nu\nu)/B(\tau \rightarrow e\nu\nu)$ shown at [TAU2023](#) using 1x1 topology, 3x1 on track
- CPV in hadronic τ decays
- V_{us} measurement
- τ lifetime measurement (τ mass already [published](#))
- Partial wave analysis of 3-prong decays

Search for non-SM processes

- Search for LFV and BNV decays

Any other idea ?

Beyond Run2

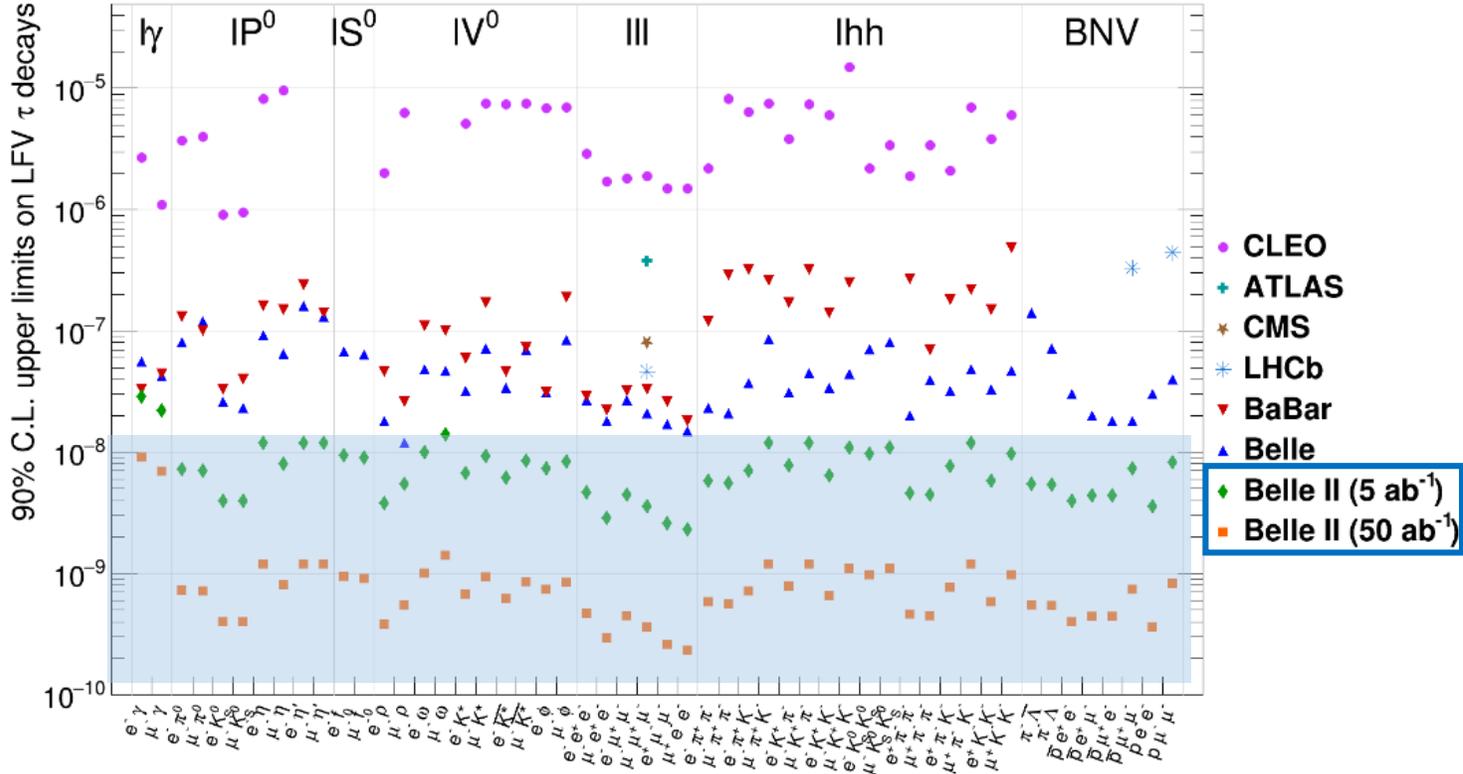
Discussions ongoing on a upgrade of the Belle II detector

- Improved robustness against backgrounds and performances
- CDR to be released soon

Studies ongoing to introduce polarization of the e- beam [arXiv:2205.12847](https://arxiv.org/abs/2205.12847)



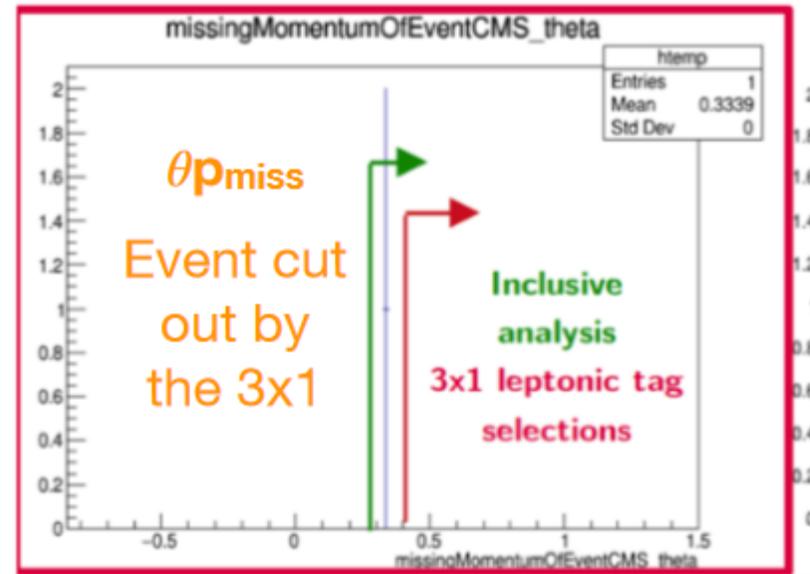
Snowmass 2021, arXiv: 2203.14919



Thanks for you attention!

Inclusive vs tagged

- Surviving event in SR does not pass the tagged requirement on missing momentum θ
- It looks compatible with
 - 4muons events with missed soft photon
 - $\tau+\tau^-$
 - continuum processes

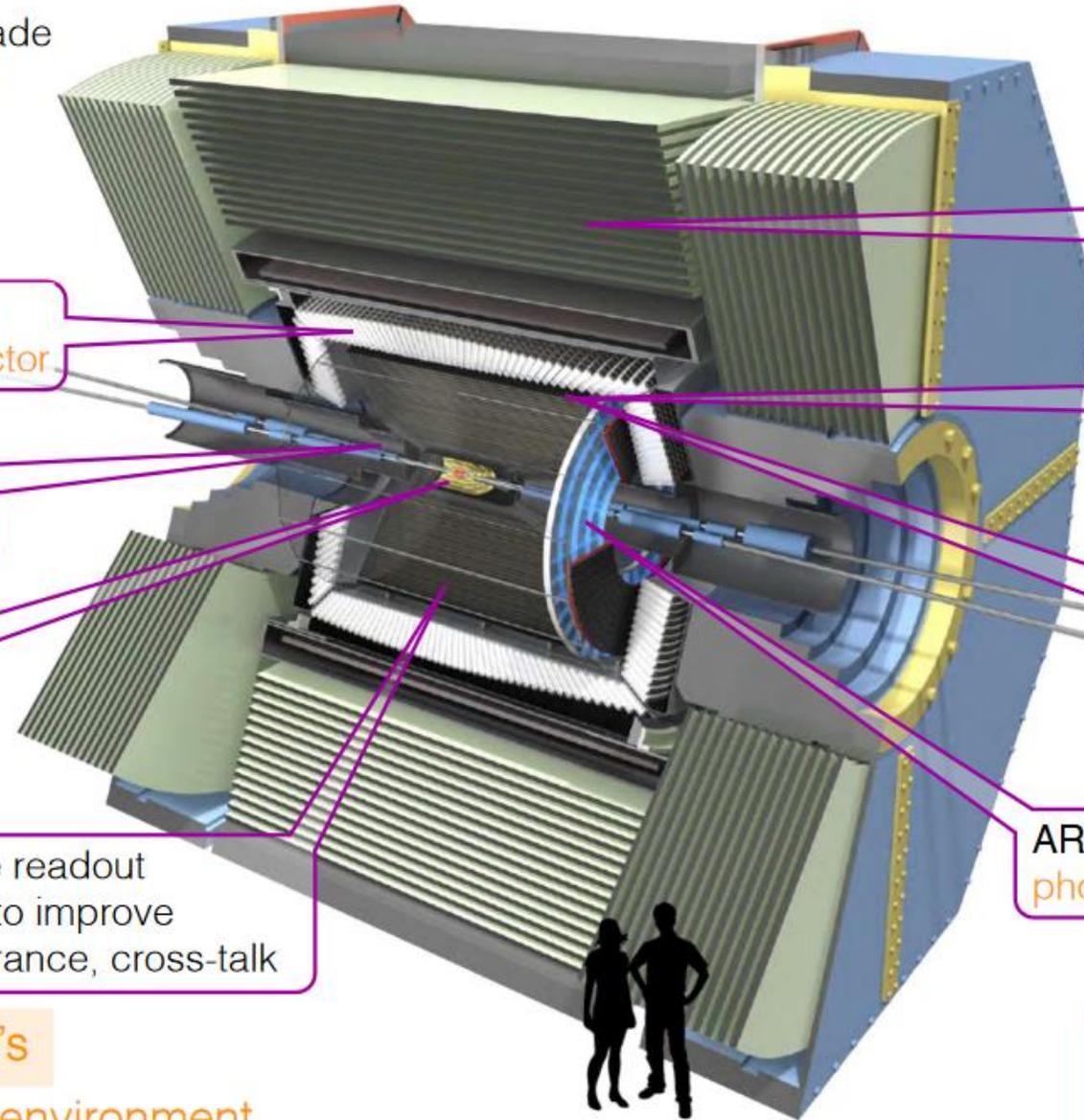


$\tau \rightarrow 3l$ experimental limits

Mode	Belle	Babar	LHCb	ATLAS	CMS
$\mu^- \mu^+ \mu^-$	2.1	3.3	4.6	3.8	2.9
$e^- e^+ e^-$	2.7	2.9	-	-	-
$e^- \mu^+ \mu^-$	2.7	3.2	-	-	-
$e^- e^+ \mu^-$	1.8	2.2	-	-	-
$e^+ \mu^- \mu^-$	1.7	2.6	-	-	-
$\mu^+ e^- e^-$	1.5	1.8	-	-	-

Detector upgrades during LS2 or beyond

See Snowmass white papers:
[arXiv:2203.11349](https://arxiv.org/abs/2203.11349) for detector upgrade
[arXiv:2207.06307](https://arxiv.org/abs/2207.06307) for physics reach
[arXiv:2203.05731](https://arxiv.org/abs/2203.05731) for backgrounds



ECL: replace crystals with pure CsI; APD readout; add pre-shower detector

IR: accommodate QCS replacement and repositioning

VXD: all pixels

- DMAPS
- SOI-DUTIP

CDC: replace readout ASIC+FPGA to improve radiation tolerance, cross-talk

KLM: replace RPCs with scintillators in barrel (some with fast timing for K_L time-of-flight); replace readout

TOP: replace readout to reduce size & power; replace all PMTs with extended-lifetime ALDs (or SiPMs?)

STOPGAP: close gaps between TOP quartz bars, provide timing layers for track trigger

ARICH: possible photosensor upgrade

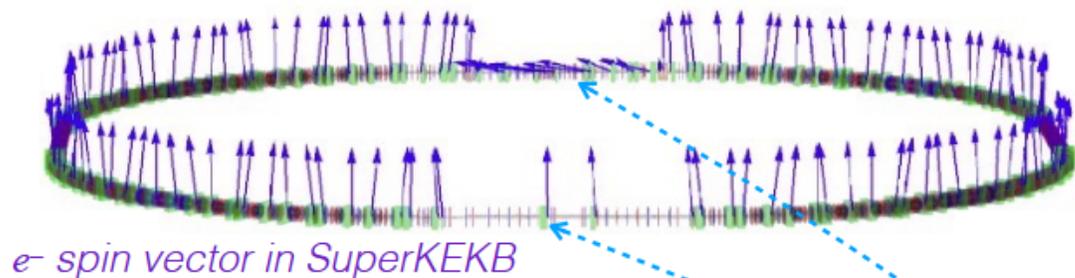
TRIGGER: replace with latest tech to increase bandwidth, allow for new trigger primitives

More distant future: ~mid-2030's

✓ Detector R&D for extreme- \mathcal{L} environment

Beam polarization & “Chiral Belle” beyond LS2 [or sooner?]

See Snowmass white paper [arXiv:2205.12847](https://arxiv.org/abs/2205.12847)



✓ Polarized electrons (70%)

- Transverse polarization at injection
- Rotate to longitudinal at interaction point
- Compton polarimeter for 0.5% precision

✓ with polarized electrons ...

- sensitivity to EW neutral vector current
- sensitivity to light Z_{dark} via $\sin^2\theta_W$
- left-right asymmetries with 5 fermions
- tau $g-2$: sensitivity of $\mathcal{O}(10^{-5})$ w/50 ab⁻¹
- background suppression in $\tau \rightarrow \ell \gamma$ using helicity distributions

