



Recent results from Belle and Belle II



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on behalf of the Belle and Belle II Collaborations

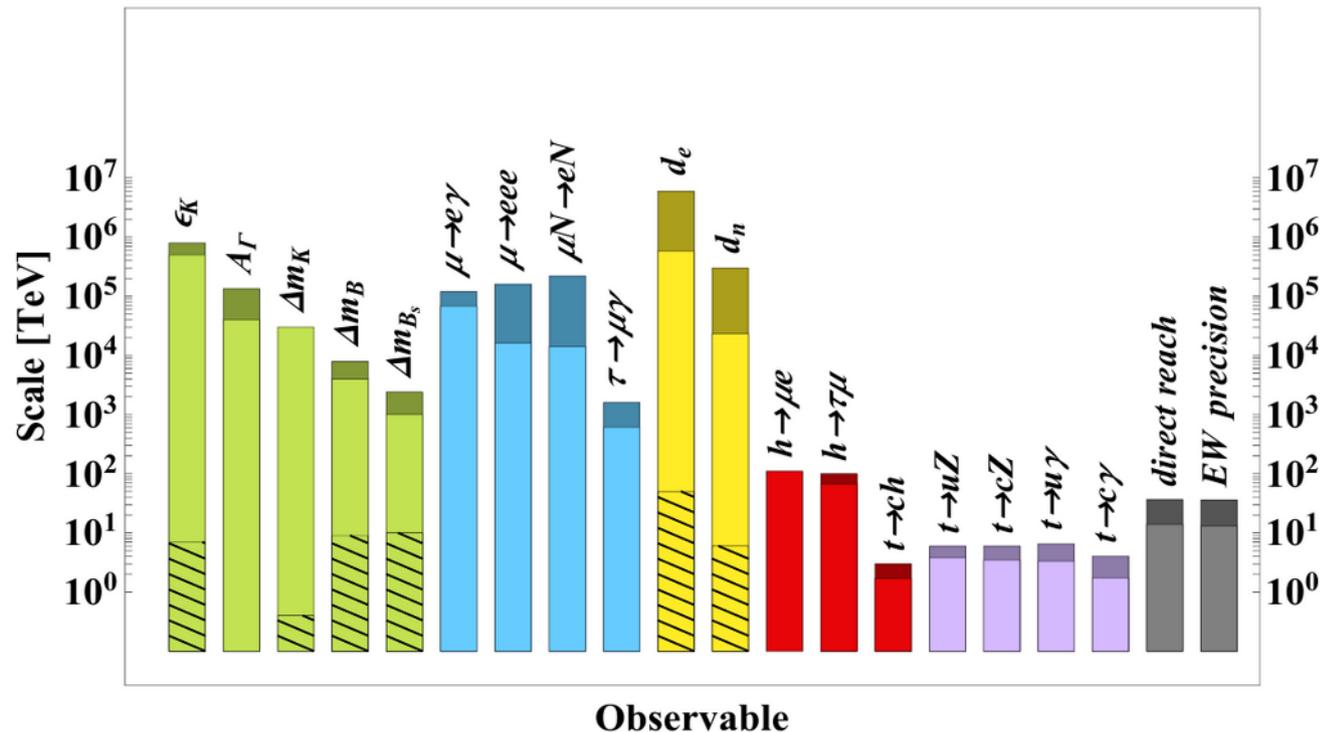
"XXX Cracow EPIPHANY Conference"

Krakow, January 8th 2024

Our mission

- Finding evidence of physics beyond the standard model, **especially looking at indirect effects** signaling the presence of new particles, interactions, coupling, phases...;
- Enormous reach for many observables in flavor physics, probing scales of new physics orders of magnitude beyond the current limits for direct production:

European Strategy for Particle Physics Preparatory Group,
arXiv:1910.11775 [hep-ex]

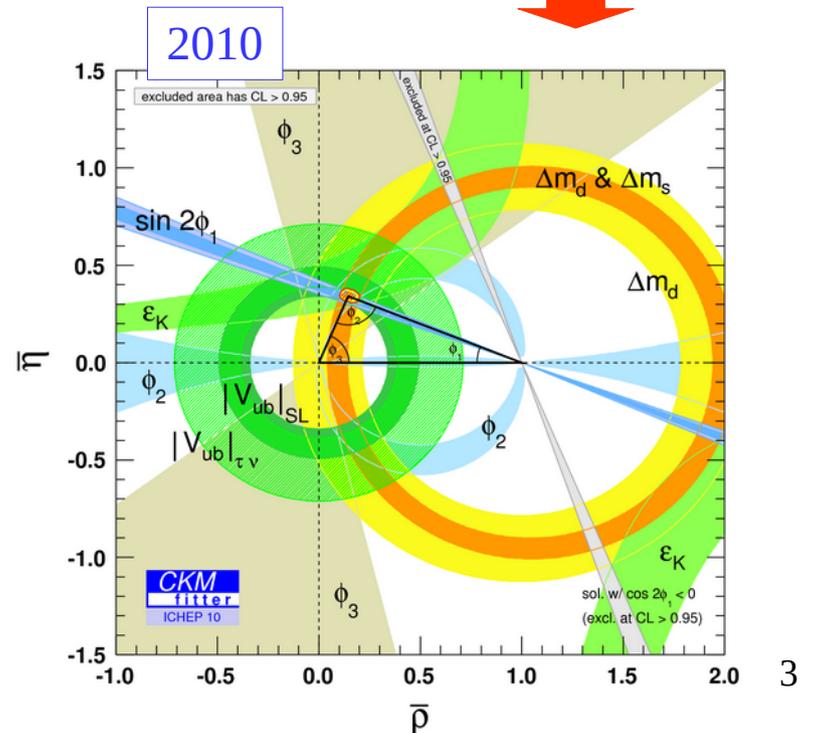
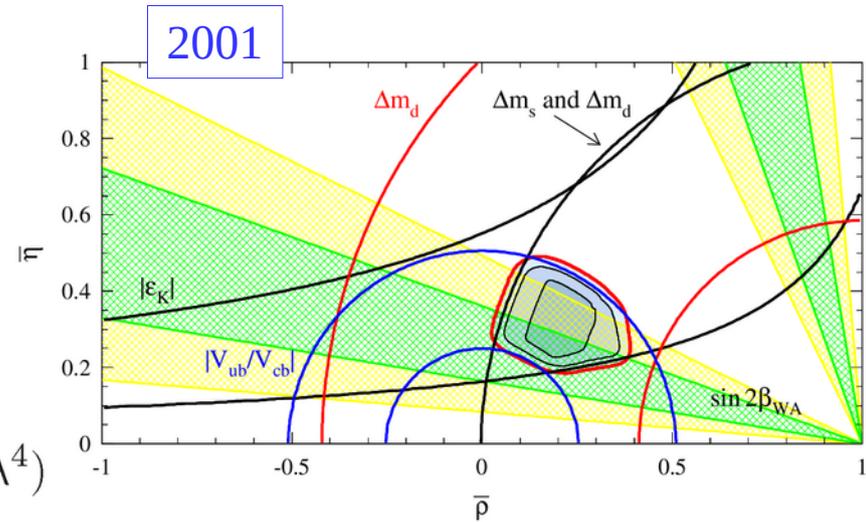


The first generation of B factories

- Spectacular confirmation of the CKM paradigm, all CP violation phenomena can be accounted for by the nontrivial phase in the CKM quark mixing matrix:

$$V_{CKM} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- But we know that the standard model cannot be the full story, it cannot explain the matter/anti-matter imbalance, the dark matter/energy, neutrino masses, etc... ;
- There must be something else, hopefully within our reach of the running or planned experiments.



Flavor physics at e^+e^- colliders

- The first generation of B-factories integrated $\sim 1.5 \text{ ab}^{-1}$;
- For the past 15 years the LHC experiments enjoyed the very large cross sections and luminosity of the World's most powerful accelerator;
- Is it worth continuing along the e^+e^- path?
- Many of the interesting modes are unique to B factories:
 - channels with π^0 , K_L , $\eta(\prime)$, ... ;
 - final states with one or more ν 's (or other elusive particles);
 - modes affected by “difficult” backgrounds, where the full knowledge of the kinematics in the event is the only way to control them;
 - τ and dark sector low multiplicity final states;
 - ... ;
- In general: a wider spectrum of measurements allows for a better understanding (or highlights our lack of...).

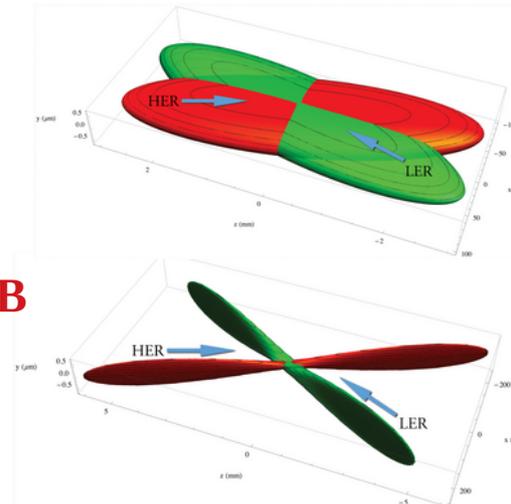
The SuperKEKB Collider



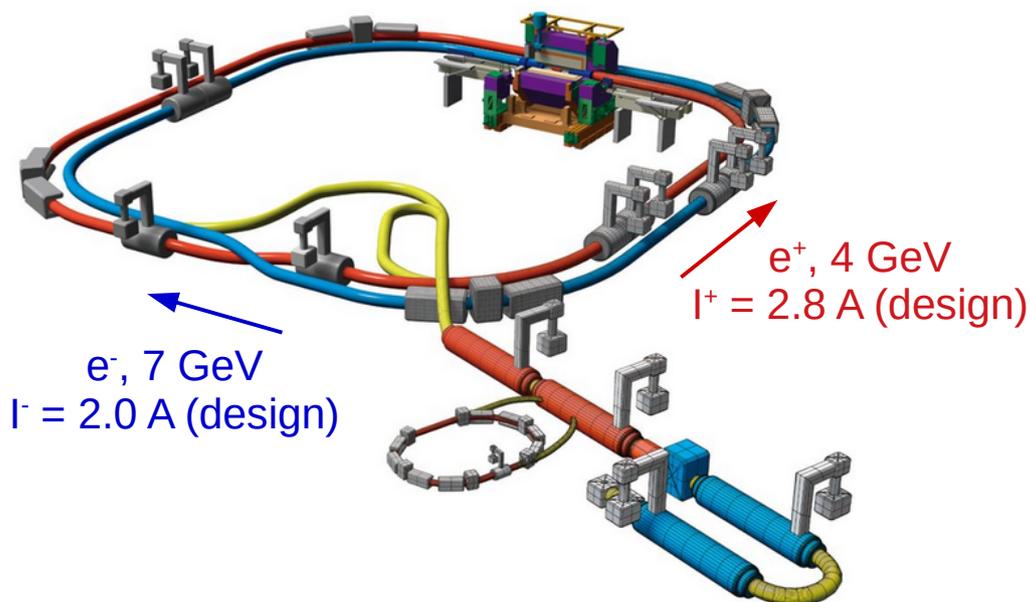
KEKB



SuperKEKB



$$L = \frac{N_+ N_- n_b f_0}{4\pi \sigma_{x,\text{eff}}^* \sqrt{\epsilon_y \beta_y^*}}$$



Improvements over KEKB:

- x20 by 'nanobeam scheme';
- x1.5 by increasing beam currents.

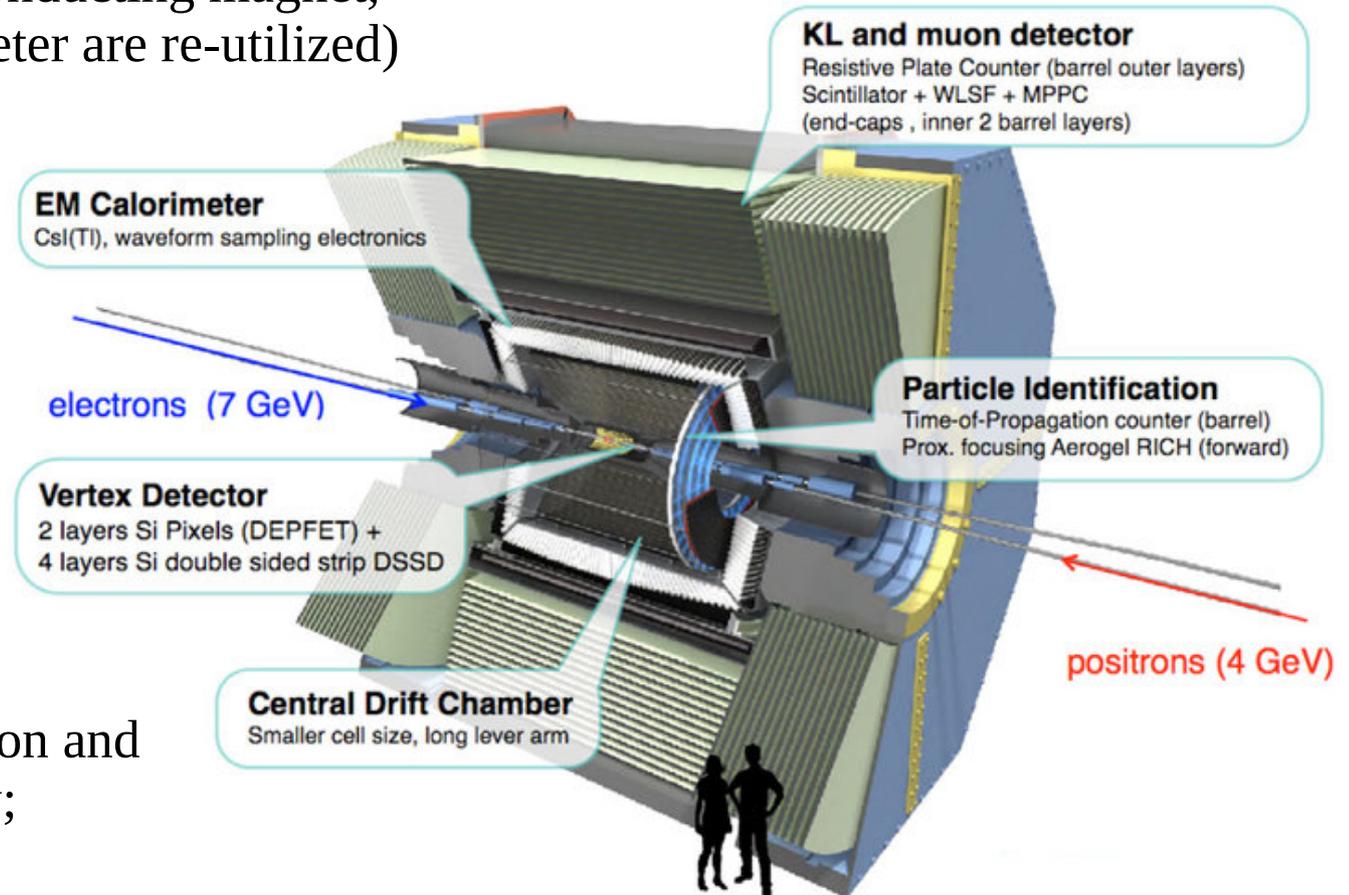
Goals:

- Instantaneous lumi: $\sim 6 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- Integrated lumi: 50 ab^{-1}

The Belle II Detector

It looks like the old Belle, but practically it is a brand new detector!

(only the structure, the superconducting magnet, and the crystals of the calorimeter are re-utilized)

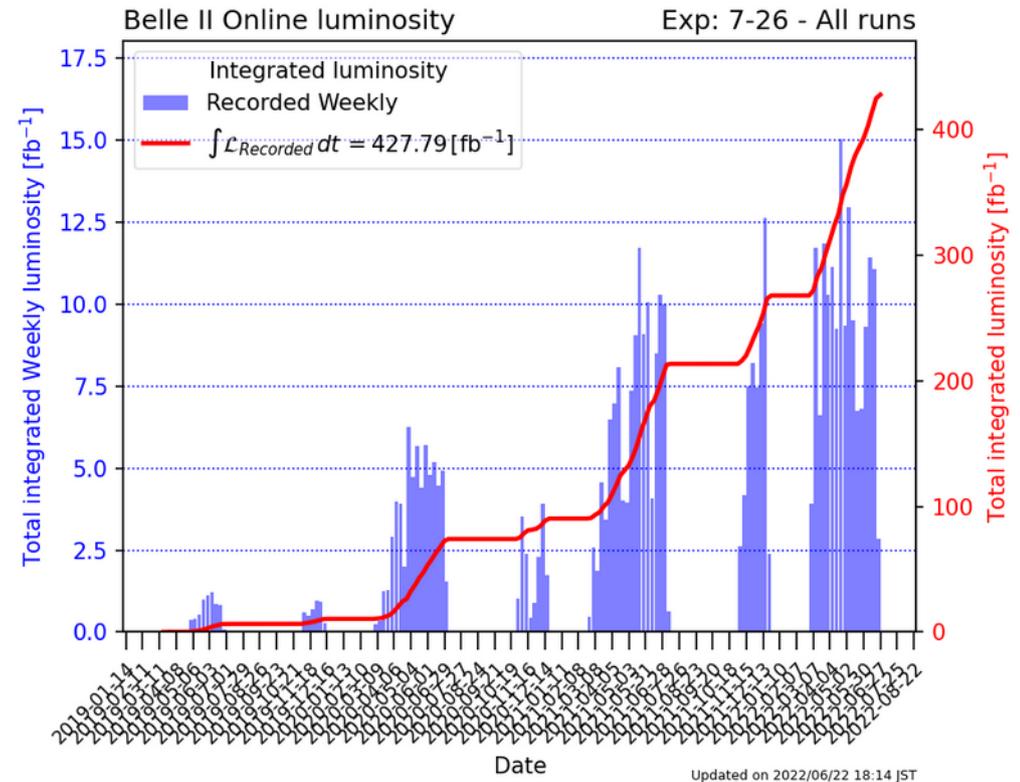


Upgrade highlights:

- improved vertexing resolution and K_S reconstruction efficiency;
- enhanced K/π separation;
- new trigger lines for Dark Sector searches, first Neural Network single track trigger;
- more efficient analysis tools, thanks to widespread use of machine learning techniques.

Belle II data taking

- Thanks to the dedication of people based at KEK, we could keep taking data even during the worst of the pandemic;
- Record instantaneous luminosity (of any collider): $4.71 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$;
- Recorded in total **$\sim 424 \text{ fb}^{-1}$** , of which:
 - **$\sim 362 \text{ fb}^{-1}$** taken at a CM energy of 10.58 GeV, corresponding to the mass of the $Y(4S)$, which dominantly decays to BB;
 - **$\sim 42 \text{ fb}^{-1}$** taken 60 MeV below the $Y(4S)$ peak (for continuum background studies);
 - **$\sim 19 \text{ fb}^{-1}$** taken around 10.75 GeV for exotic hadron searches.



In June 2022 we started the Long Shutdown 1 period, dedicated to maintenance and upgrade work. We plan to resume operations at the end of this month!

Many of the results I will show today are based on the full statistic, plus in some cases we also add the Belle data (still Belle II x 2)!

Outline

I will not be able to show all the results, I will focus on:

- time dependent CP violation on $B^0 \rightarrow J/\psi K_S$ and $\eta' K_S$;
- measurements of ϕ_3/γ ;
- evidence for $B^+ \rightarrow K^+ \nu \nu$;
- $R(D^*) = BR(B \rightarrow D^* \tau \nu) / BR(B \rightarrow D^* l \nu)$;
- dark sector searches;

Please also attend the talks from my Belle (II) colleagues:

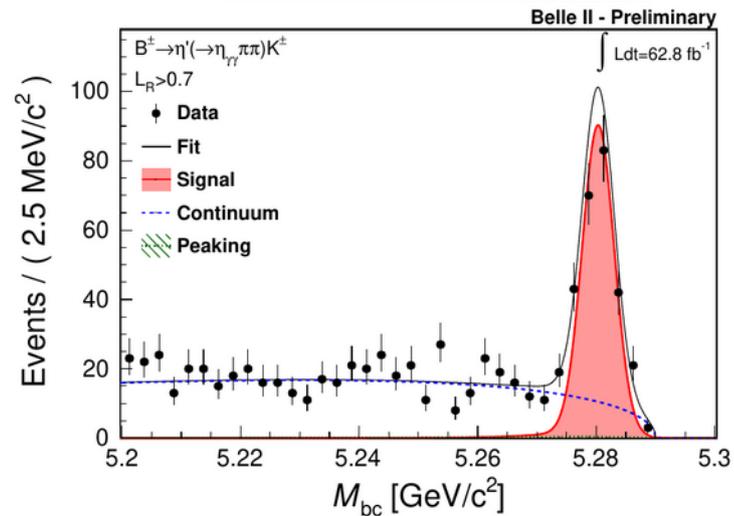
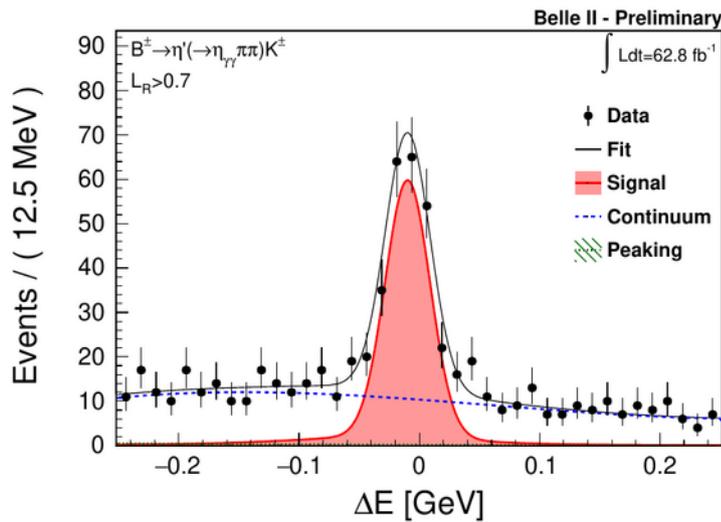
- **K. Lautenbach, “ τ physics at Belle and Belle II”, today at 15:45;**
- **M. Bauer, “ V_{cb} and V_{ub} measurements at Belle and Belle II”, Friday at 9:30.**

B factory variables

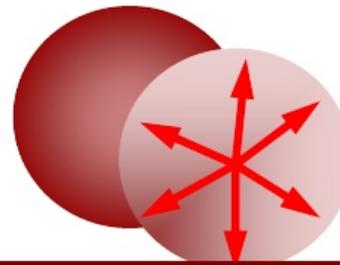
Two key variables discriminate against background for fully reconstructed (hadronic) final states:

$$\Delta E = E_B^* - \frac{\sqrt{s}}{2}$$

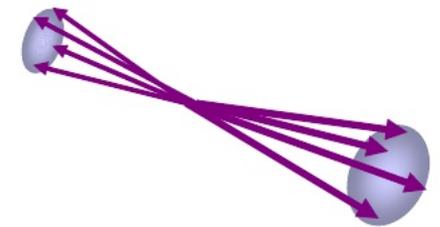
$$M_{bc} = \sqrt{\frac{s}{4} - p_B^{*2}}$$



For many final states, the dominant source of background is the ‘qq continuum’, which is suppressed based on the different topology with respect to $B\bar{B}$ events:

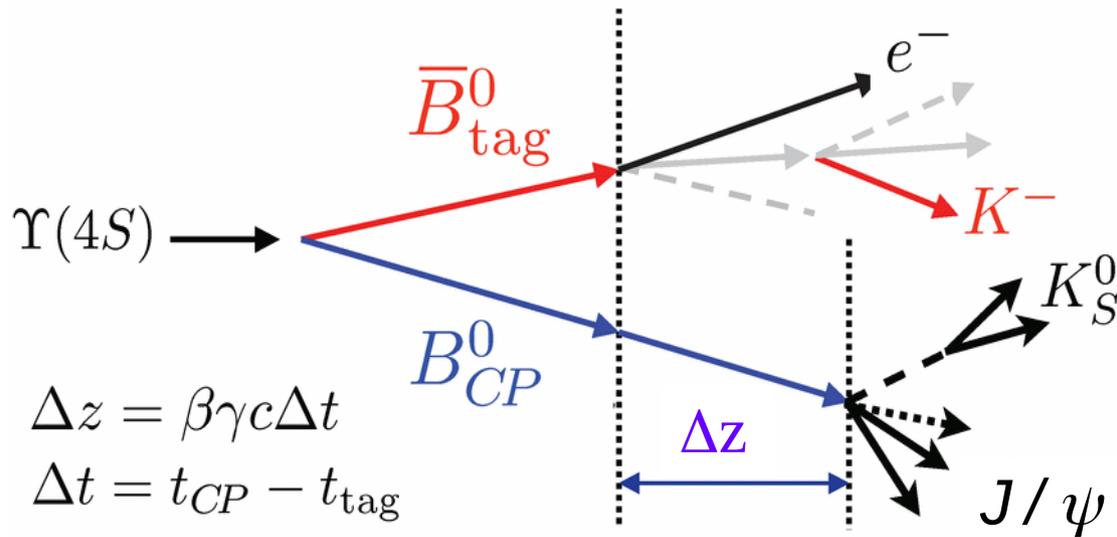


Spherical BB events



Jet-like qq events

Time dependent analyses



$\langle \Delta z \rangle \sim 130 \mu\text{m}$ at Belle II

Flagship measurement of the B Factories, still very important at Belle II;

$$\begin{aligned}
 \mathcal{A}_f(\Delta t) &= \frac{\Gamma(\bar{B}^0(\Delta t) \rightarrow f) - \Gamma(B^0(\Delta t) \rightarrow f)}{\Gamma(\bar{B}^0(\Delta t) \rightarrow f) + \Gamma(B^0(\Delta t) \rightarrow f)} \\
 &= S_f \sin(\Delta m_B \Delta t) - C_f \cos(\Delta m_B \Delta t)
 \end{aligned}$$

S_f : time dependent asymmetry

C_f : time integrated (or direct) asymmetry

Quite complicated analysis, several ingredients must be in place:

- 1) ability to identify the flavor (B^0 or \bar{B}^0) of the unreconstructed B (flavor tagging);
- 2) B-decay vertices resolution;
- 3) signal side efficiency, background modeling.

Fully exploiting the quantum entanglement of the two B mesons!

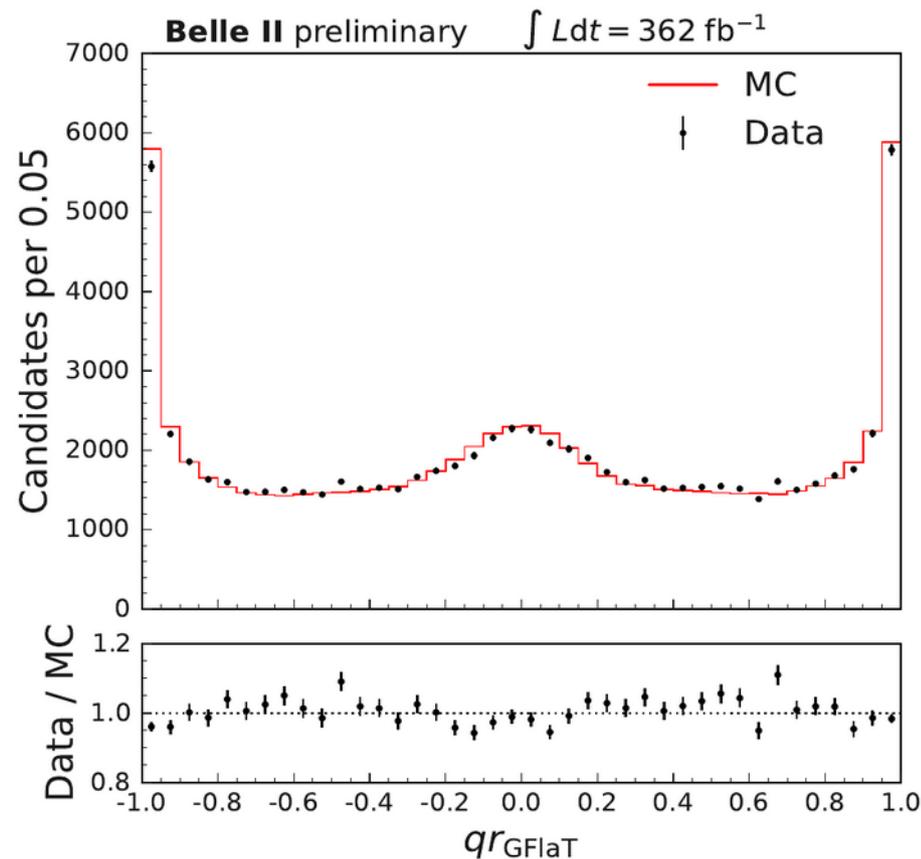
Progress in B flavor tagging

- The first CP violation analyses in Belle II relied on a category-based (CB) algorithm [[Eur. Phys. J 82, 283 \(2022\)](#)];
- We explored a more advanced algorithm, GFlaT, based on a **graph convolutional neural network**, exploiting 25 variables for each track from the unreconstructed B decay (for up to 16 tracks);
- The performance is evaluated from a time dependent analysis of self-tagging $B^0 \rightarrow D^{(*)-}\pi^+$ decays;
- We measure an impressive increase in the effective tagging efficiency, compared to the previous algorithm:

$$\varepsilon_{\text{tag,CB}} = (31.7 \pm 0.5 \pm 0.4)\%$$

$$\varepsilon_{\text{tag,GFlaT}} = (37.4 \pm 0.4 \pm 0.3)\%$$

Y. Uematsu, CKM 2023



This corresponds to $\sim 18\%$ more luminosity available for CP violation analyses!

$\sin 2\phi_1 / \sin 2\beta$ from $B^0 \rightarrow J/\psi K_S$

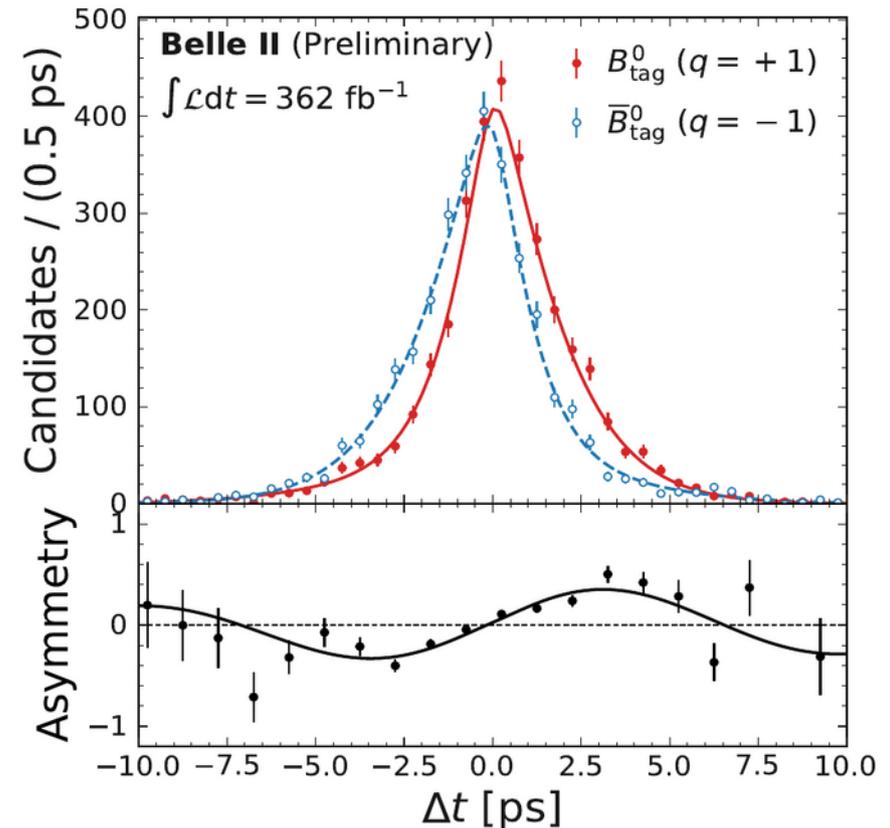
- We update the flagship measurement of the B factories using the full Belle II data set and the GFlaT flavor tagger;
- We fit the ΔE distribution of the selected candidates in order to subtract the backgrounds;
- We then fit the background subtracted Δt distributions and measure the CP violating parameters:

$$S = 0.724 \pm 0.035 \pm 0.014$$

$$C = -0.035 \pm 0.026 \pm 0.013$$

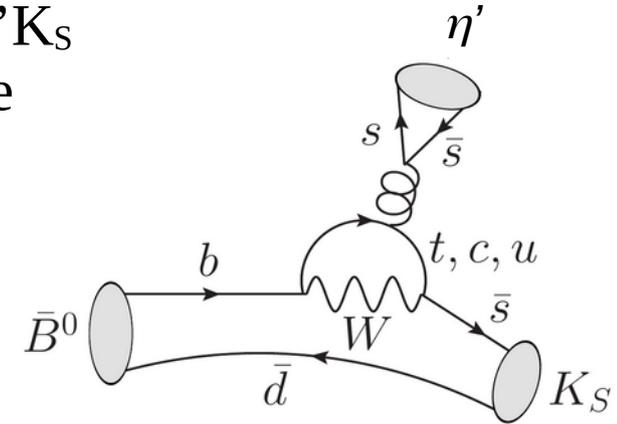
- This is well compatible with the world averages and the latest LHCb result (which is a factor ~ 2 more precise).

Y. Uematsu, CKM 2023



$\sin 2\phi_1 / \sin 2\beta$ from $B^0 \rightarrow \eta' K_S$

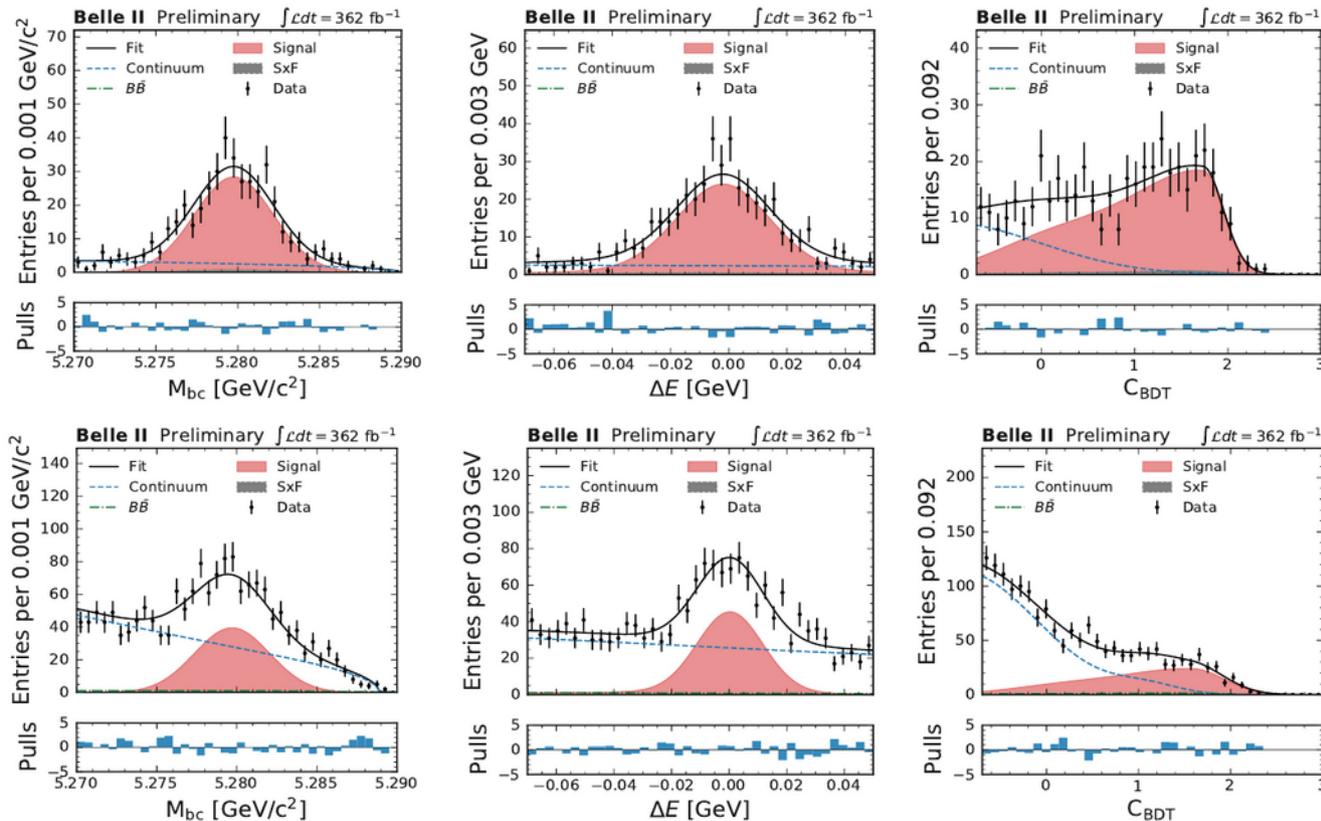
- Motivations: the time dependent CP violation in $B^0 \rightarrow \eta' K_S$ (proceeding through loop diagrams) is expected to be the same observed in $B^0 \rightarrow J/\psi K_S$ (tree);
- Any significant deviation would be an indication of new physics;
- We reconstruct the sub-channels: $\eta' \rightarrow \eta(\rightarrow \gamma\gamma)\pi^+\pi^-$ and $\eta' \rightarrow \rho^0\gamma$, and determine their yields with a three dimensional fit:



$$\eta' \rightarrow \eta(\rightarrow \gamma\gamma)\pi^+\pi^-$$

$$\eta' \rightarrow \rho^0\gamma$$

Y. Uematsu, CKM 2023



$\sin 2\phi_1 / \sin 2\beta$ from $B^0 \rightarrow \eta' K_S$

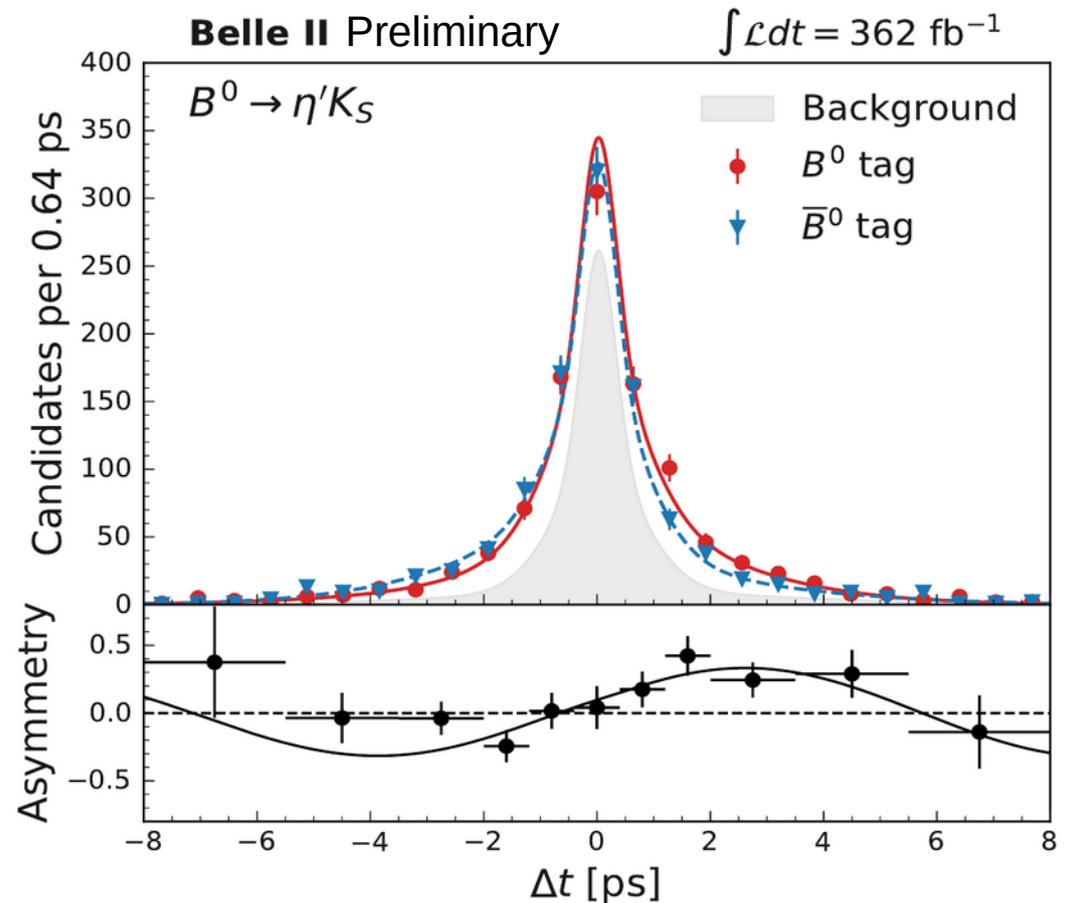
- With the yields (~ 800 signal events in total) fixed from the previous step, we perform the time dependent fit:

- We find:

$$C_{\eta' K_S^0} = -0.19 \pm 0.08 \pm 0.03$$

$$S_{\eta' K_S^0} = 0.67 \pm 0.10 \pm 0.04$$

which is in good agreement with both the world average and the $B^0 \rightarrow J/\psi K_S$ result.

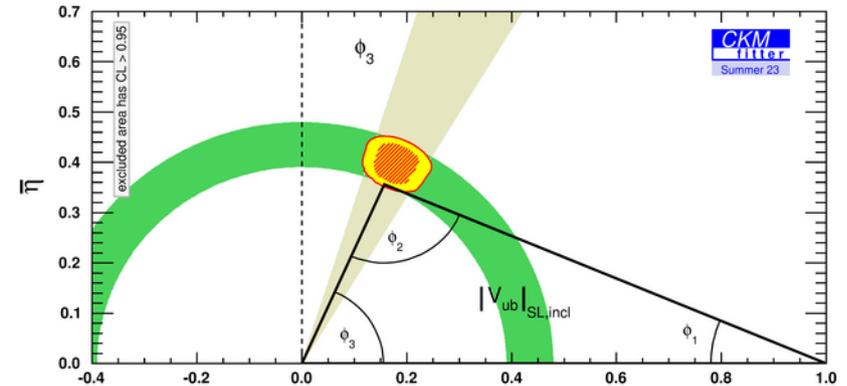
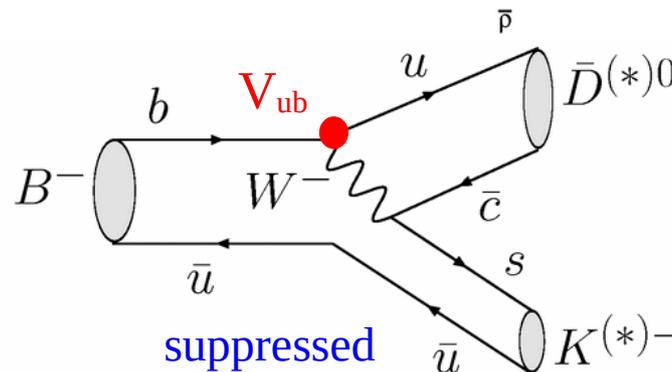
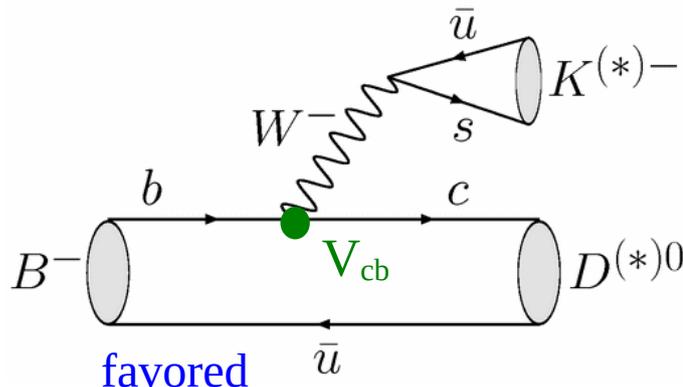


Measurements of ϕ_3/γ

- ϕ_3/γ is one of the fundamental inputs of the CKM Unitarity Triangle fit, as it comes from the interference of tree level amplitudes;

$$\gamma = \phi_3 \equiv \arg \left[-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right]$$

Current precision: $\sim 3.5^\circ$



- The precision of LHCb will be out of reach for quite a few years, but the importance of the parameters calls for a substantial effort from **Belle + Belle II**. There are many methods to access ϕ_3/γ , some unique to LHCb, some in which Belle (II) will have an edge.

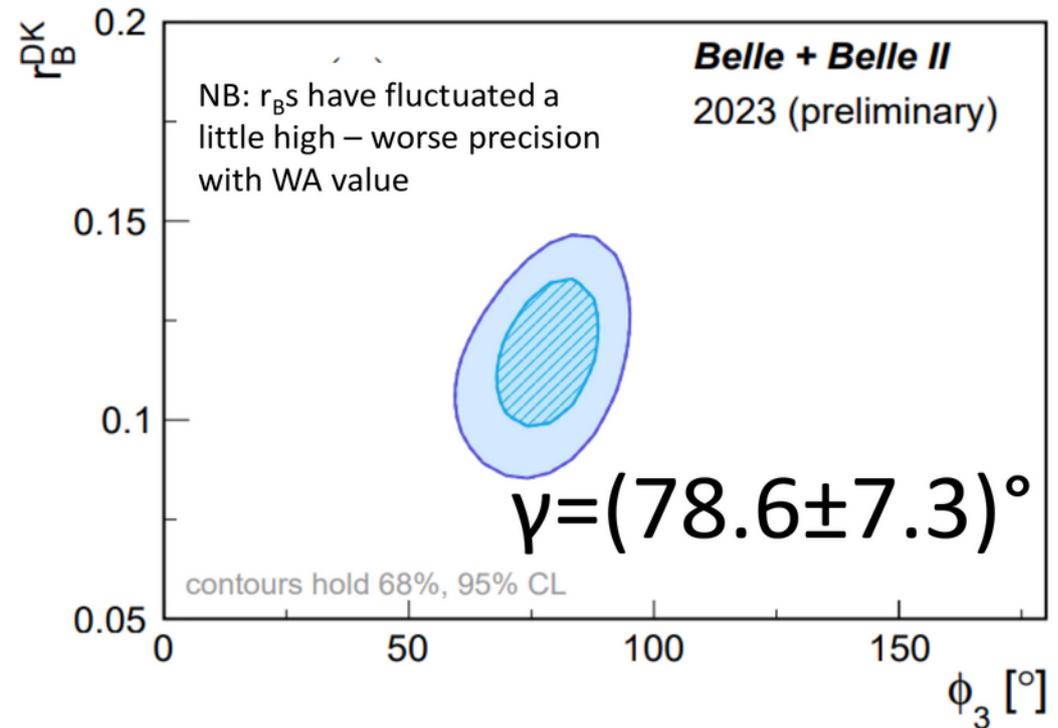
Measurements of ϕ_3/γ

- Several papers based on the full Belle + a fraction of Belle II data sets:

→ (BPGGSZ) $D^0 \rightarrow K_S h^+ h^-$
[J. High Energ. Phys. 2022, 63 \(2022\)](#)

→ (GLS) $D^0 \rightarrow K_S K \pi$
[arXiv:2306.02940 \[hep-ex\]](#)

→ (GLW) $D^0 \rightarrow K K, K_S \pi^0$
[arXiv:2308.05048 \[hep-ex\]](#)



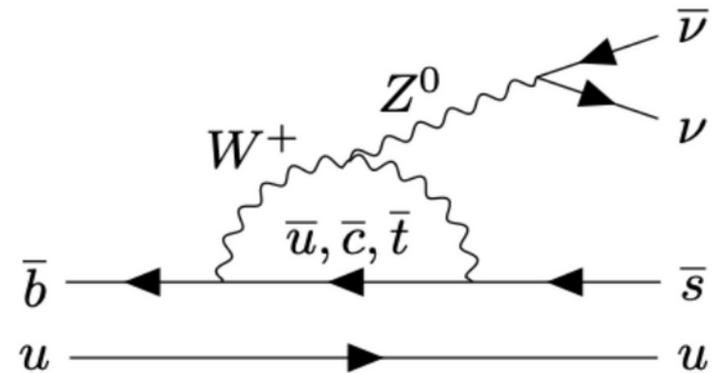
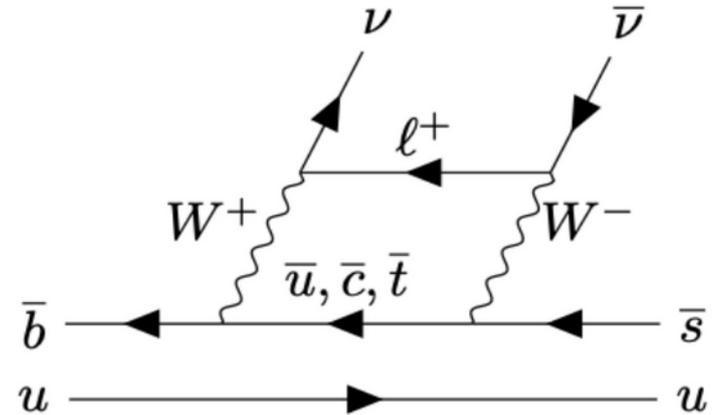
- Current LHCb precision:

$$\phi_3/\gamma = (63.8 \pm 3.6)^\circ \quad \text{LHCb-CONF-2022-003}$$

We need a few ab^{-1} in order to have a meaningful comparison

$B^+ \rightarrow K^+ \nu \nu$ – motivations

- Very suppressed in the SM, proceeding only through box/loop diagrams;
- Expected BR: $(5.6 \pm 0.4) \times 10^{-6}$
[[Phys. Rev. D 107, 014511 \(2023\)](#)];
- It could be enhanced by new physics contributions, and be connected to other anomalies seen in $b \rightarrow s l^+ l^-$, $R(D^{(*)})$, $(g-2)_\mu, \dots$;
- Very challenging from the experimental point of view. At least two ν 's in the final state, controlling the backgrounds is crucial;
- Upper limits provided by BaBar [[HAD, SL](#)] and Belle [[HAD, SL](#)], exploiting the reconstruction of the other B in the event in a hadronic or semileptonic final state.

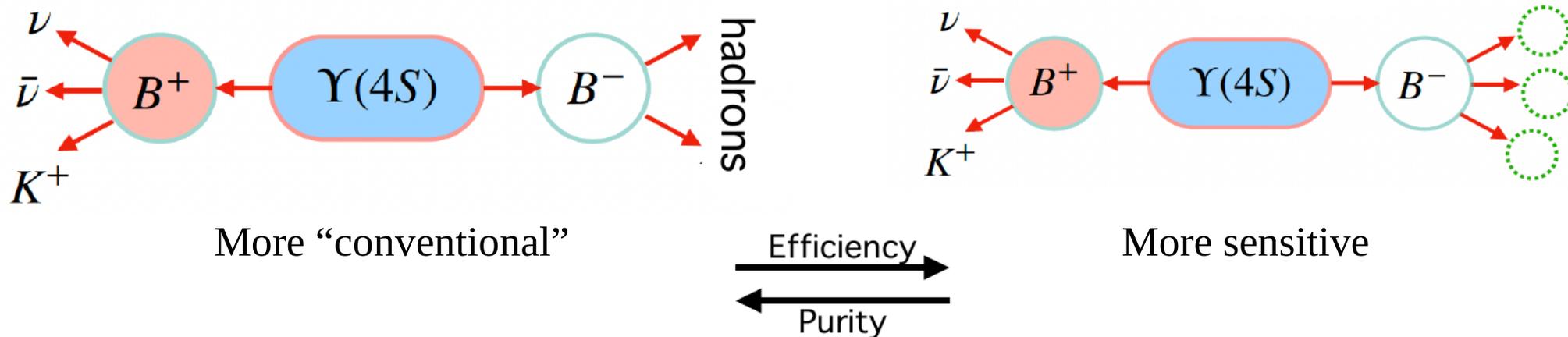


Diagrams for short distance contributions
(long distance: 10% of the total branching fraction)

$B^+ \rightarrow K^+ \nu \nu$ – experimental approaches

Two techniques utilized in parallel at Belle II:

[arXiv:2311.14647 \[hep-ex\]](https://arxiv.org/abs/2311.14647)



Hadronic Tag Analysis (HTA):
stronger control of the backgrounds,
but lower efficiency.
Relying on the Full Event
Interpretation (FEI) algorithm
[[Comput. Softw. Big Sci 3, 6 \(2019\)](#)]

Inclusive Tag Analysis (ITA): first tried
at Belle II, background suppression
relies on the properties of the *Rest Of
the Event (ROE)*, which should
correspond to the other B in the event

The two analyses are (almost) statistically independent

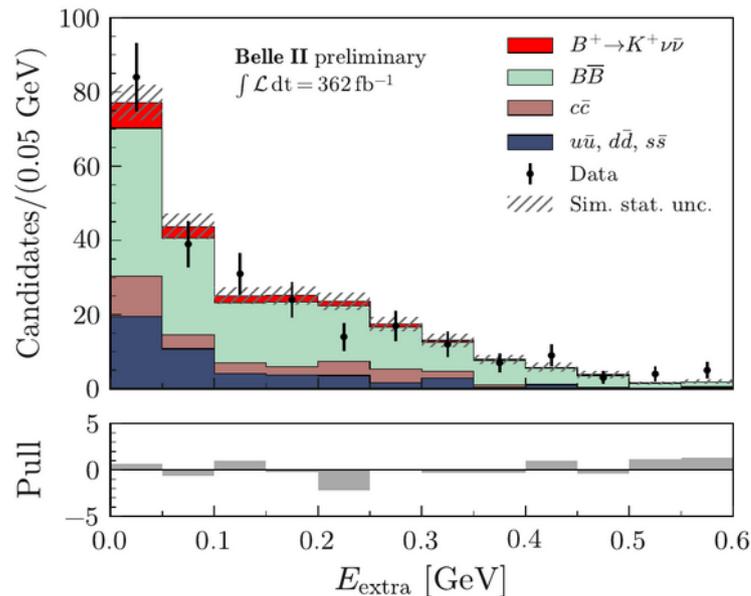
$B^+ \rightarrow K^+ \nu \nu$ – selection

- We select a kaon candidate track (PID efficiency $\sim 68\%$, $\pi \rightarrow K$ mis-ID rate 1.2%);
- If two K candidates are present in the ITA, we select that with the lowest q^2 :

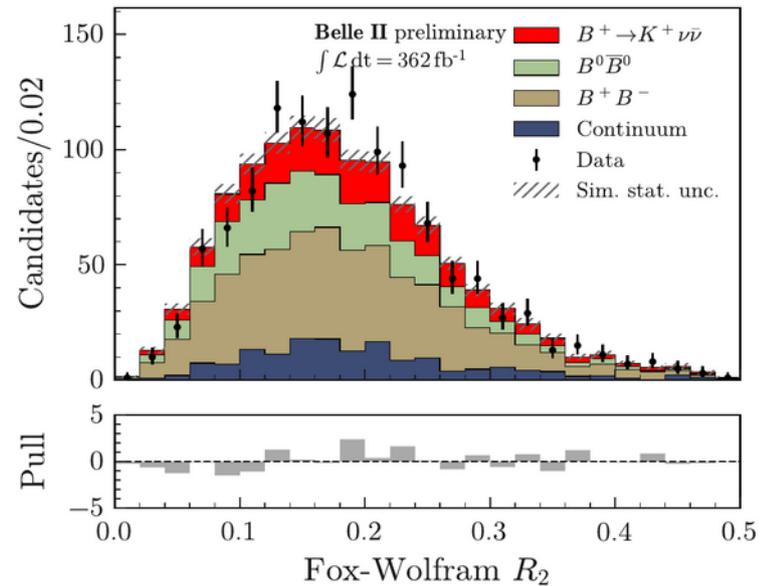
$$q_{\text{rec}}^2 = s/(4c^4) + M_K^2 - \sqrt{s}E_K^*/c^4$$
 (the choice is correct in $\sim 96\%$ of the cases)
- Variables sensitive to the signal properties, event shape, extra particles in the event, ... , are combined in one (for HTA) or two successive (for ITA) BDT's;

arXiv:2311.14647 [hep-ex]

HTA

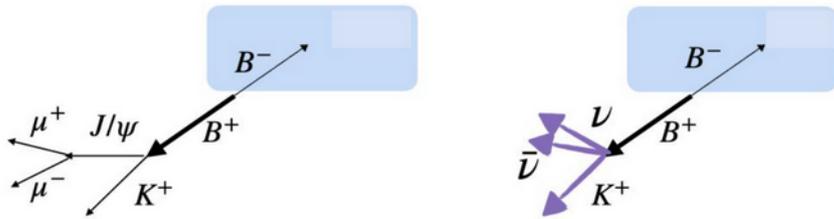


ITA



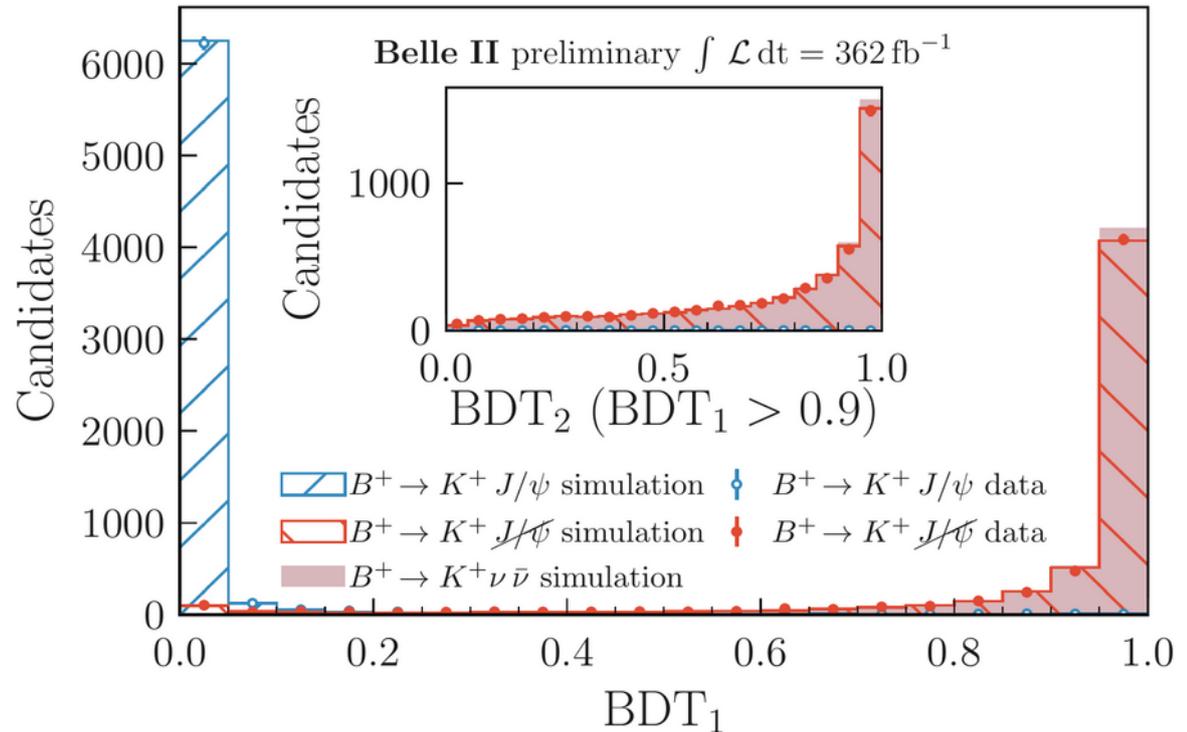
$B^+ \rightarrow K^+ \nu \bar{\nu}$ – validation

- We validate the ITA procedure and signal efficiency using $B^+ \rightarrow K^+ J/\psi(\rightarrow \mu^+ \mu^-)$;



- We see very good agreement in the BDT output between data and signal simulation;

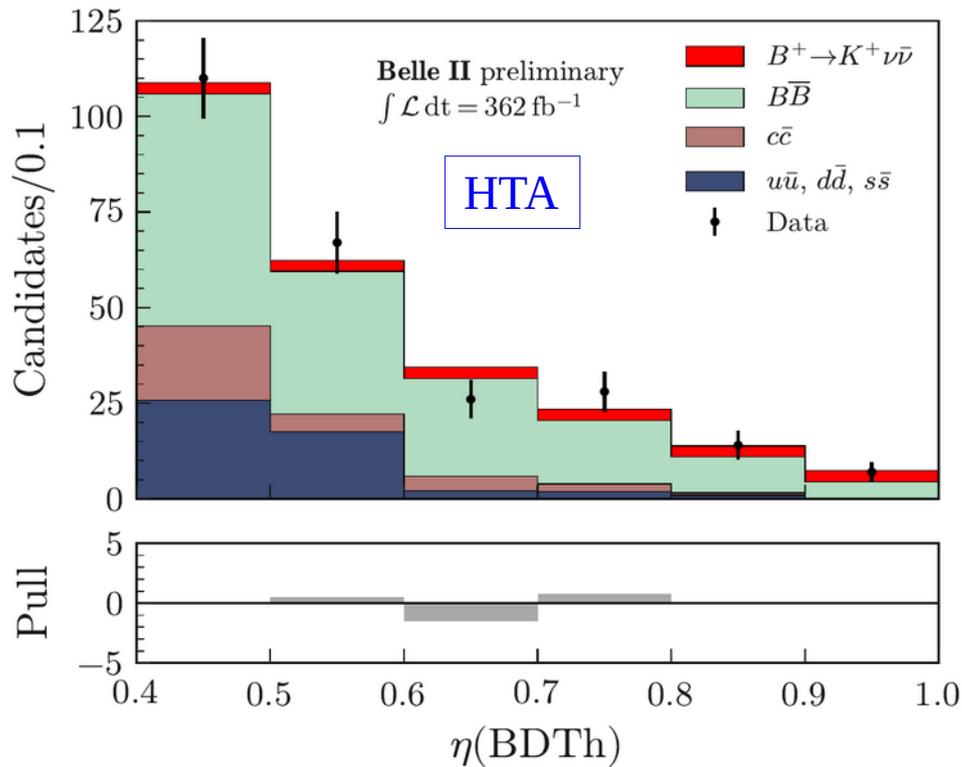
- Other checks from:
 - study of off-resonance data;
 - pion enriched control samples;
 - measurement of $B^+ \rightarrow \pi^+ K^0$;
 - ... ;



Data/MC differences observed in the normalization of the control samples contribute to the systematic uncertainties

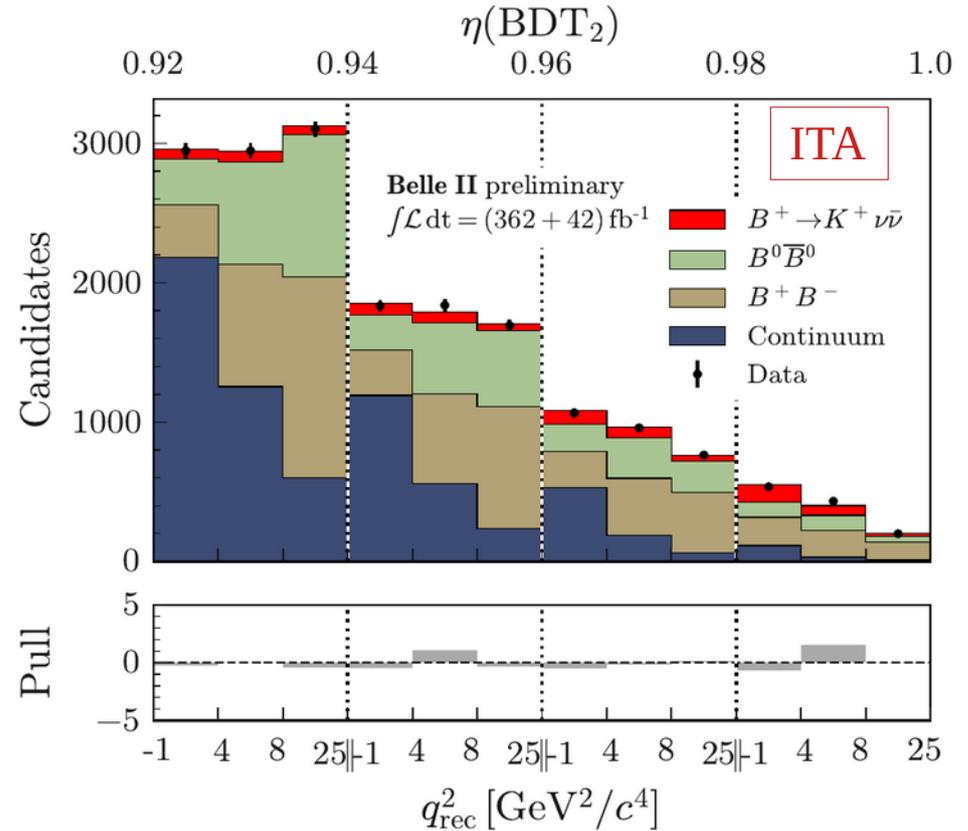
$B^+ \rightarrow K^+ \nu \nu$ – results

The signal is extracted in bins of the transformed (flat in efficiency) output η of the BDT (and q^2 for ITA):



$$\mu_{\text{HTA}} = 2.2^{+1.8}_{-1.7}(\text{stat})^{+1.6}_{-1.1}(\text{syst})$$

1.1 σ above the background only hypothesis
0.6 σ above the SM expectation



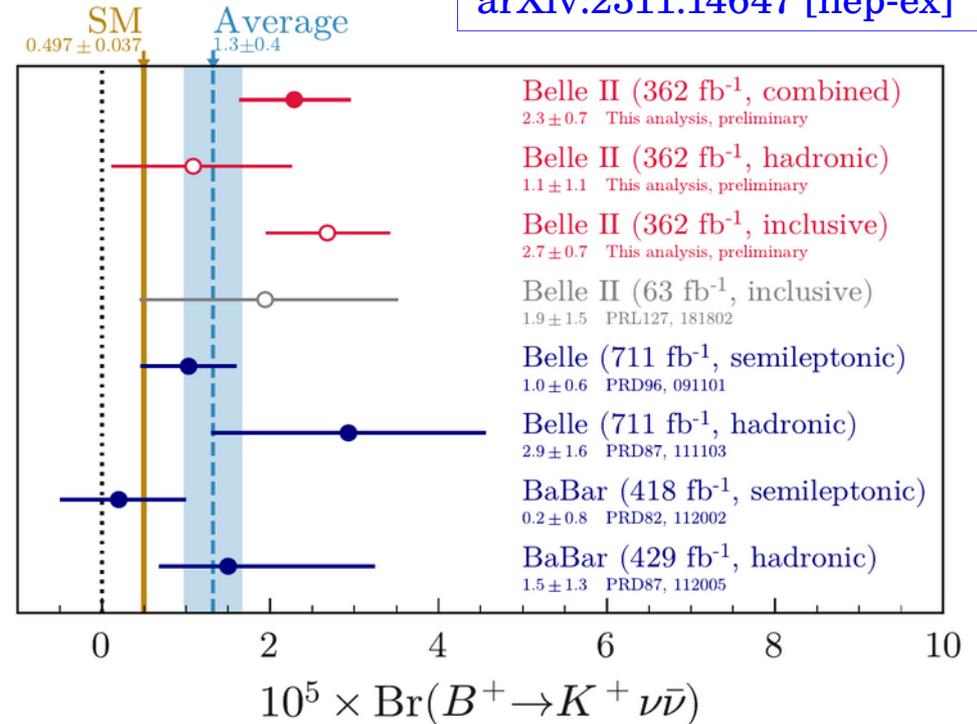
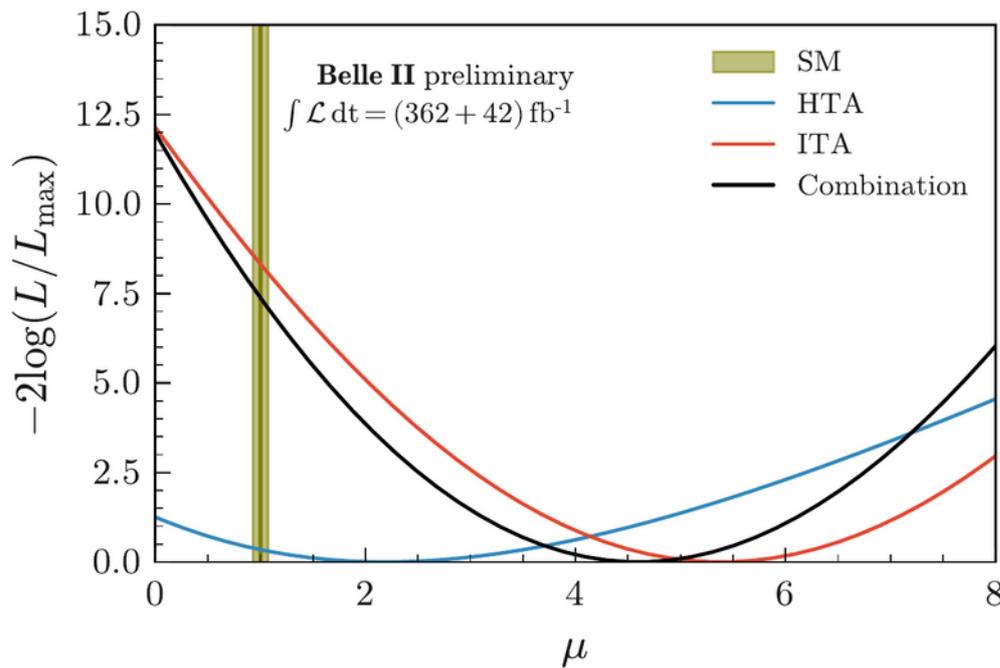
$$\mu_{\text{ITA}} = 5.4 \pm 1.0(\text{stat}) \pm 1.1(\text{syst})$$

3.5 σ above the background only hypothesis
2.9 σ above the SM expectation

$B^+ \rightarrow K^+ \nu \nu$ – results

Combining the results of **ITA** and **HTA**:

arXiv:2311.14647 [hep-ex]



$$\mu = 4.6 \pm 1.0(\text{stat}) \pm 0.9(\text{syst})$$

$$BR(B^+ \rightarrow K^+ \nu \nu) = [2.4 \pm 0.5(\text{stat})_{-0.4}^{+0.5}(\text{syst})] \times 10^{-5}$$

3.5 σ above the background only hypothesis
 2.7 σ above the SM expectation

Exciting result, to be confirmed with **Belle ITA**, semileptonic tagged analysis and the investigation of more $B \rightarrow K^{(*)} \nu \nu$ modes.

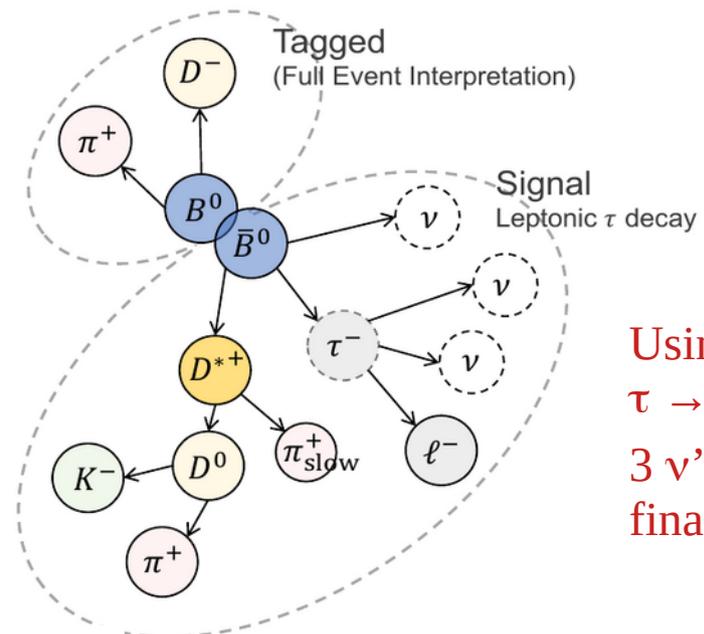
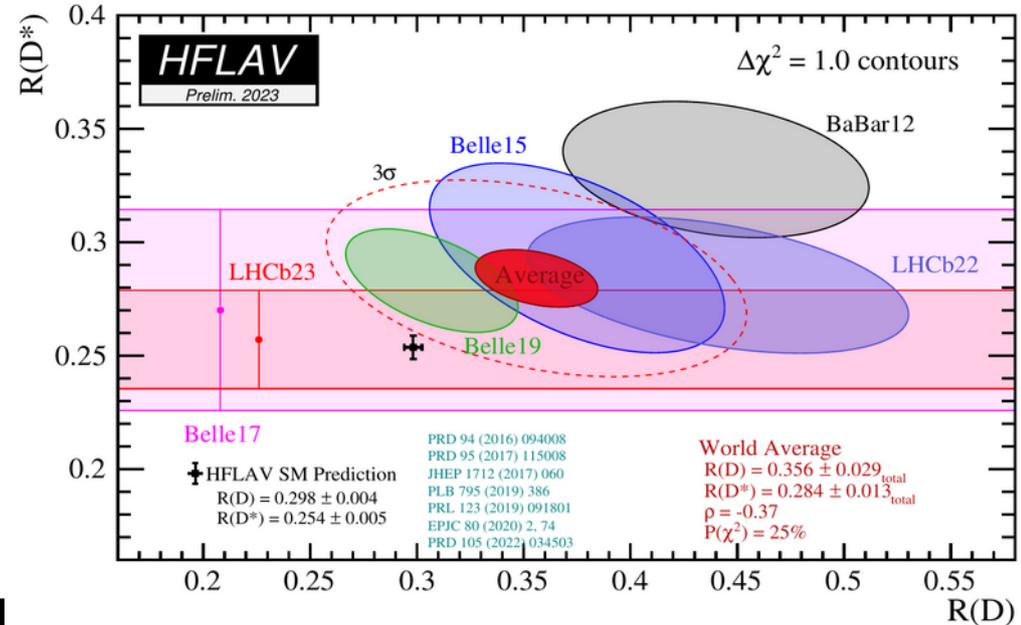
First $R(D^*)$ measurement at Belle II

- One of the outstanding anomalies, pointing towards a violation of the Lepton Flavor Universality:

$$R(D^{(*)}) = \frac{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^{(*)} \ell^- \bar{\nu}_\ell)}$$

- Experimental challenges: backgrounds are difficult to control, due to at least two ν 's in the final state, no clear signal peak;
- First Belle II measurement of $R(D^*)$: we use the **Full Event Interpretation** (same as $B \rightarrow K \nu \nu$ HTA), to have the strongest control of the backgrounds, at the price of reducing the statistics.

[arXiv:2401.02840 \[hep-ex\]](https://arxiv.org/abs/2401.02840)



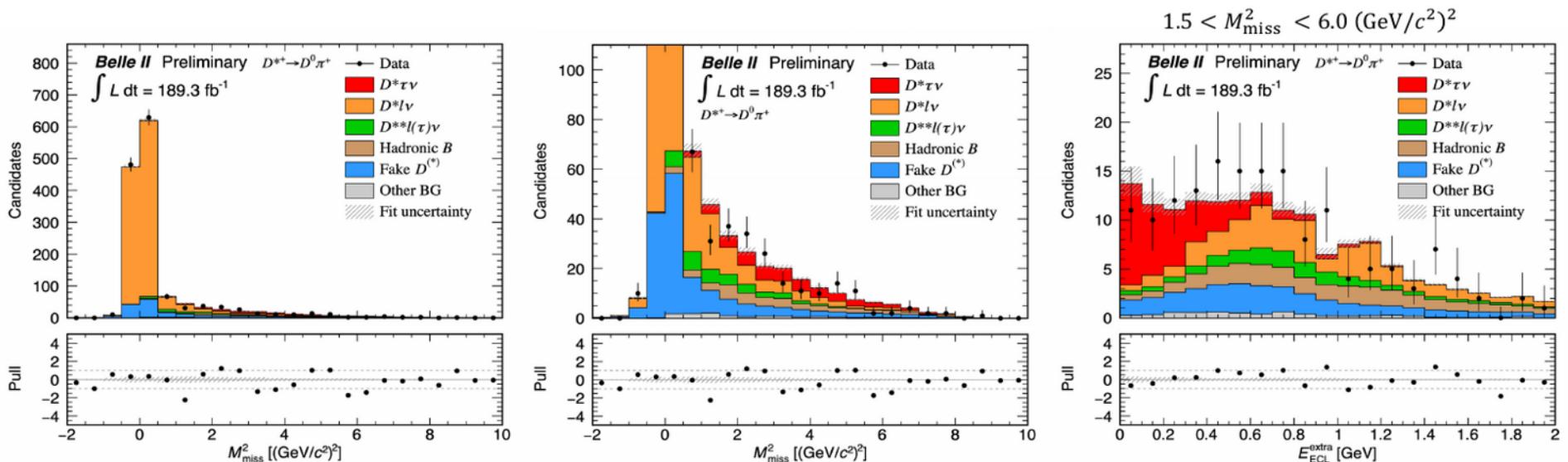
Using only $\tau \rightarrow l \nu \nu$,
 3 ν 's in the final state!

First R(D^{*}) measurement at Belle II

- Analysis strategy: we extract the signal from a 2D fit on the variables:

- missing mass squared: $M_{\text{miss}}^2 = (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_{\ell})^2$
- extra energy on the calorimeter: $E_{\text{ECL}}^{\text{extra}}$

arXiv:2401.02840 [hep-ex]



- The major backgrounds are validated on data sidebands:

- low q^2 sideband ($D^* l \nu$ enhanced);
- extra π^0 selection ($D^{**} l \nu$ enriched);
- $\Delta m = m(D^*) - m(D)$ sideband (fake D^*).

Using only ~50%
of the statistics
available at Belle II

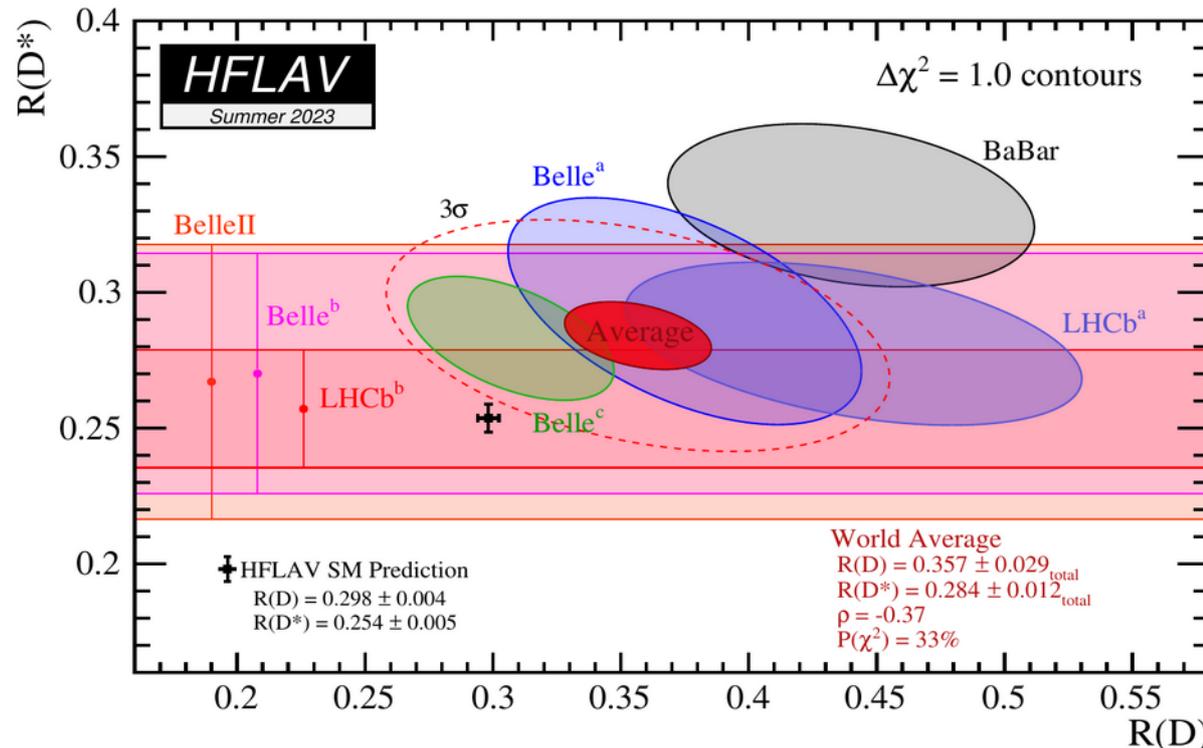
First $R(D^*)$ measurement at Belle II

Result:

$$R(D^*) = 0.262 \begin{matrix} +0.041 \\ -0.039 \end{matrix} (\text{stat.}) \begin{matrix} +0.035 \\ -0.032 \end{matrix} (\text{syst.})$$

[arXiv:2401.02840 \[hep-ex\]](https://arxiv.org/abs/2401.02840)

40% improvement in the statistical precision compared to Belle with the same luminosity



Performed also the first inclusive measurement of:

$$R(X) = \frac{BF(B \rightarrow X\tau\nu)}{BF(B \rightarrow Xl\nu)}$$

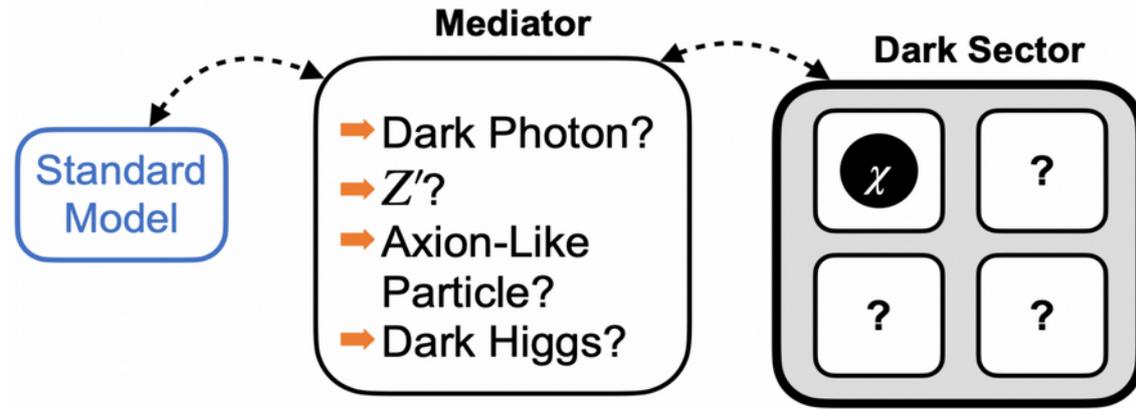
Results consistent with both SM and $R(D^*)$ world average

[arXiv:2311.07248 \[hep-ex\]](https://arxiv.org/abs/2311.07248)

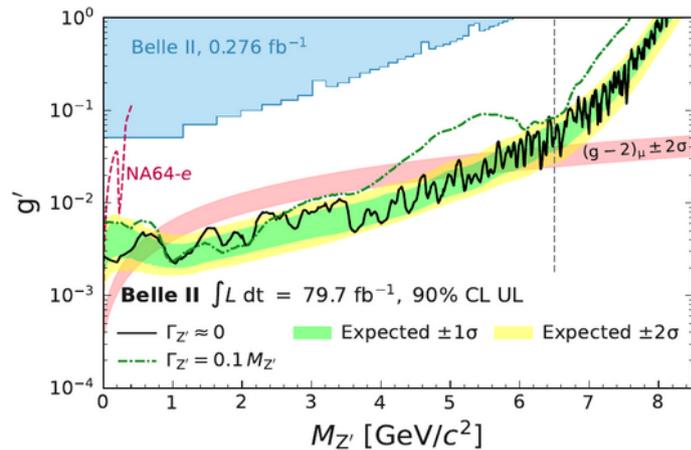
Compatible with both the SM predictions and the World average, we need more data, and also the measurement of $R(D)$, to shed more light on this problem.

Dark sector searches

- In many extensions of the SM, there exist a dark sector, that interacts with the SM particles via a weakly coupled mediator;
- If the mass of the mediator is in the $[0.01 - 10]$ GeV range, this could be accessible to Belle II;
- Belle II implements trigger strategies that were not available to Belle, thus opening new territories even with smaller luminosity:

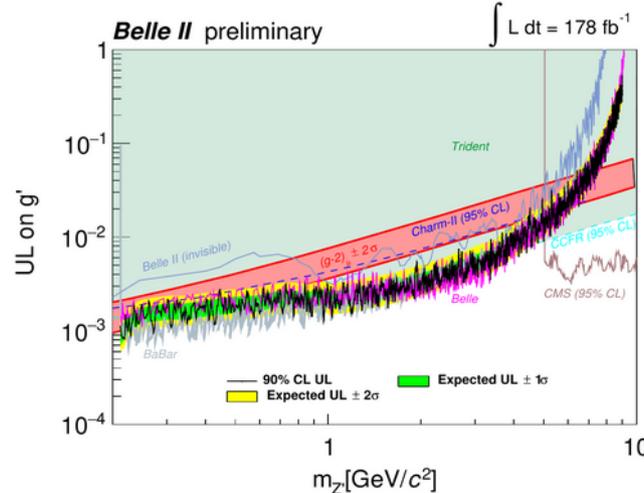


Search for $Z' \rightarrow$ invisible



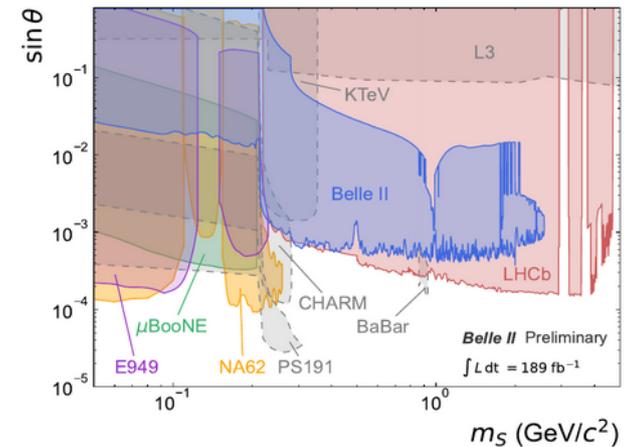
Phys. Rev. Lett. 130, 231801 (2023)

Search for $Z' \rightarrow \mu\mu$



M. Laurenza, DMNET 2023

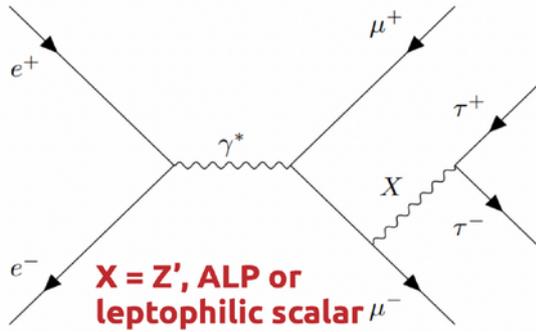
Search for Long Lived Particles



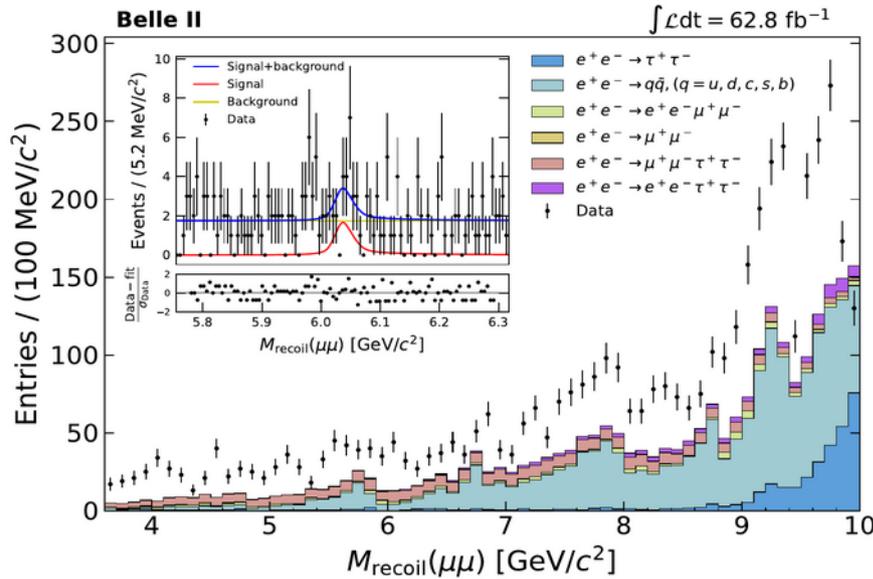
Phys. Rev. D 108, L111104 (2023)

Dark sector searches

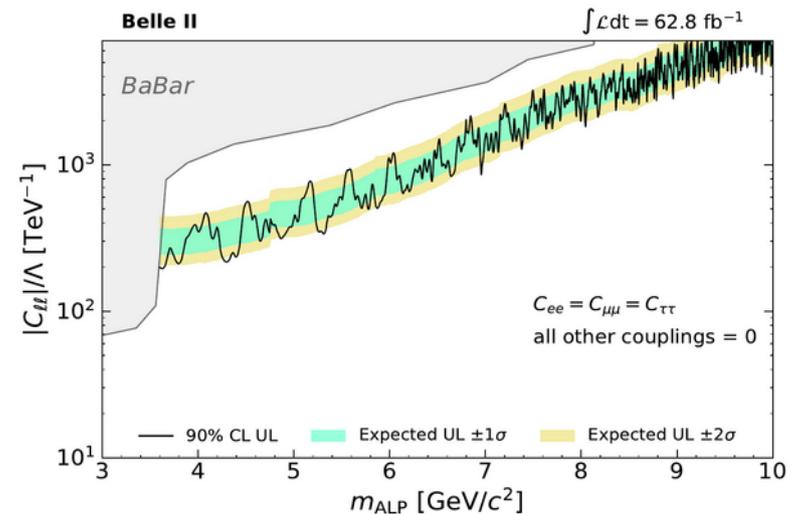
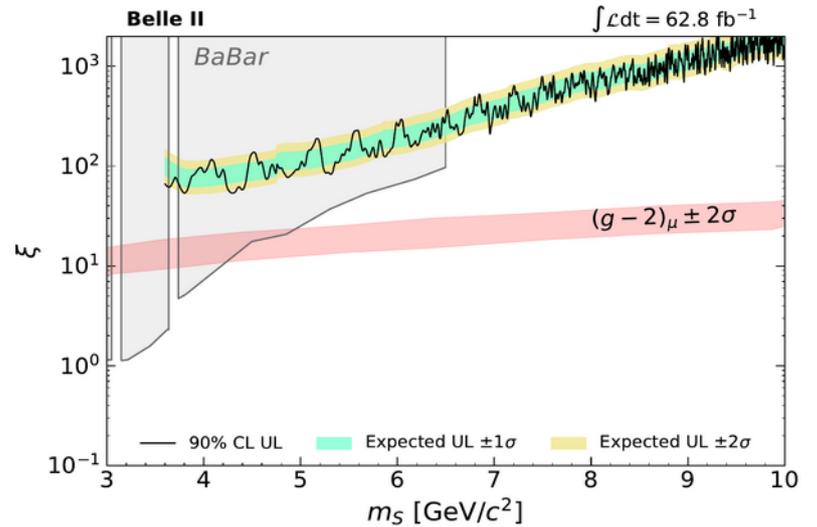
- Search for a $\tau\tau$ resonance in $e^+e^- \rightarrow \mu^+\mu^-X, X \rightarrow \tau^+\tau^-$;



- Looking for a narrow peak in the mass recoiling against the dimuons:



Part of the $\gamma\gamma \rightarrow q\bar{q}$ backgrounds are not covered by the simulation



Conclusions

- After many years from the beginning, the e^+e^- path to flavor physics continues to bear fruits;
- Belle II successfully concluded Run1 and the first results show significant better performance compared to its predecessor;
- Not a lot of integrated luminosity (yet), but we are also exploring new analysis techniques, ideas, final states, ... ;
- Belle II Run2 is about to start, expect many more results to come!

Backup slides

$\sin(2\beta/\phi_1)$ outlook

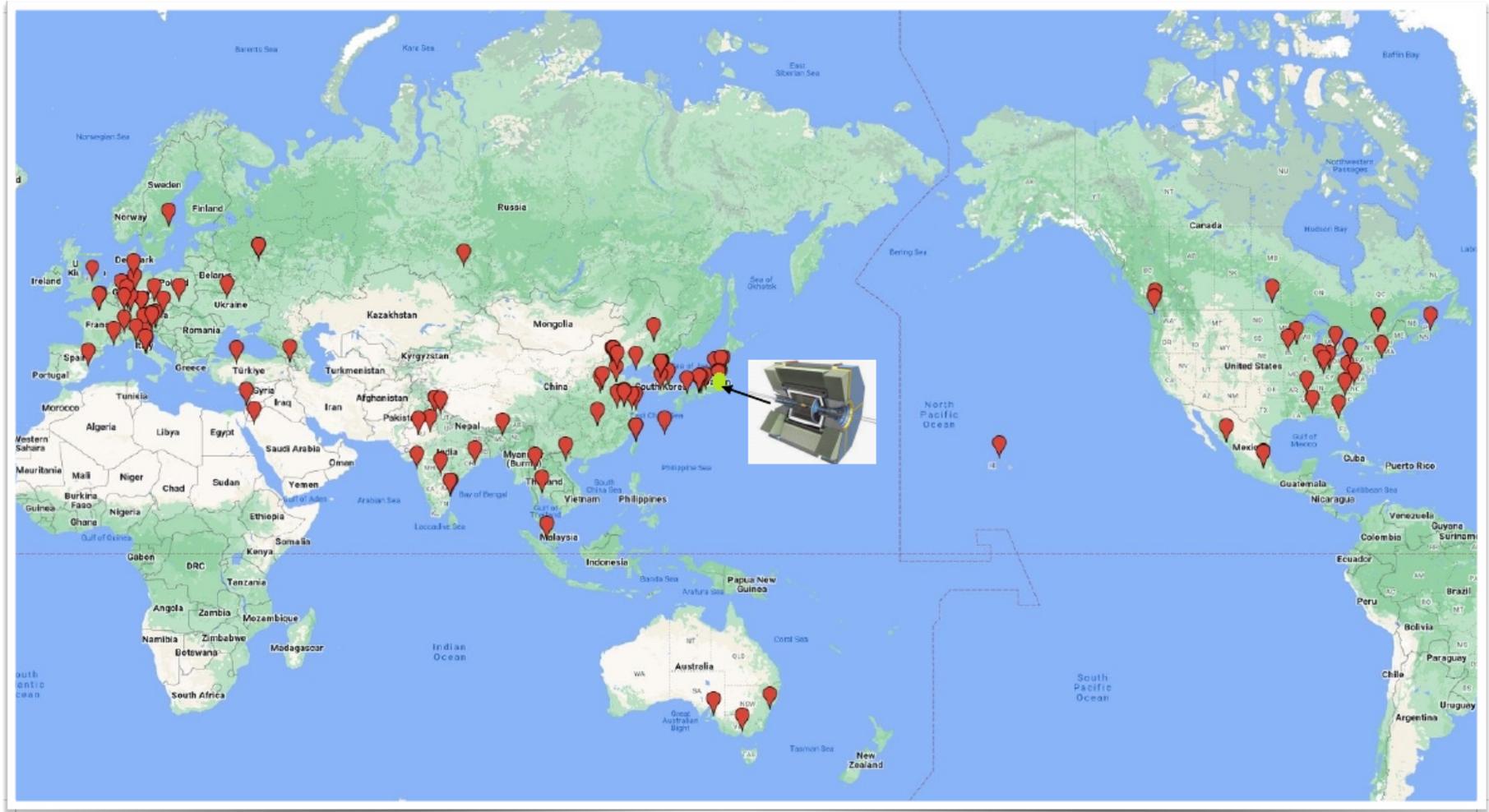
- $\sin(2\beta)$ from $J/\psi K^0$ will be systematics dominated @50 ab⁻¹;
- Irreducible systematic uncertainties from alignment of the vertex detector and Doubly Cabibbo Suppressed Decays on the tag side;

Belle II Physics Book

	No improvement	Vertex improvement	Leptonic categories
$S_{c\bar{c}s}$ (50 ab ⁻¹) time dependent CP parameter			
stat.	0.0027	0.0027	0.0048
syst. reducible	0.0026	0.0026	0.0026
syst. irreducible	0.0070	0.0036	0.0035
$A_{c\bar{c}s}$ (50 ab ⁻¹) direct CP asymmetry			
stat.	0.0019	0.0019	0.0033
syst. reducible	0.0014	0.0014	0.0014
syst. irreducible	0.0106	0.0087	0.0035

- *Penguin pollution* can no longer be ignored and must be constrained from $B \rightarrow J/\psi \pi^0$ and other SU(3) related channels.

The Belle II Collaboration

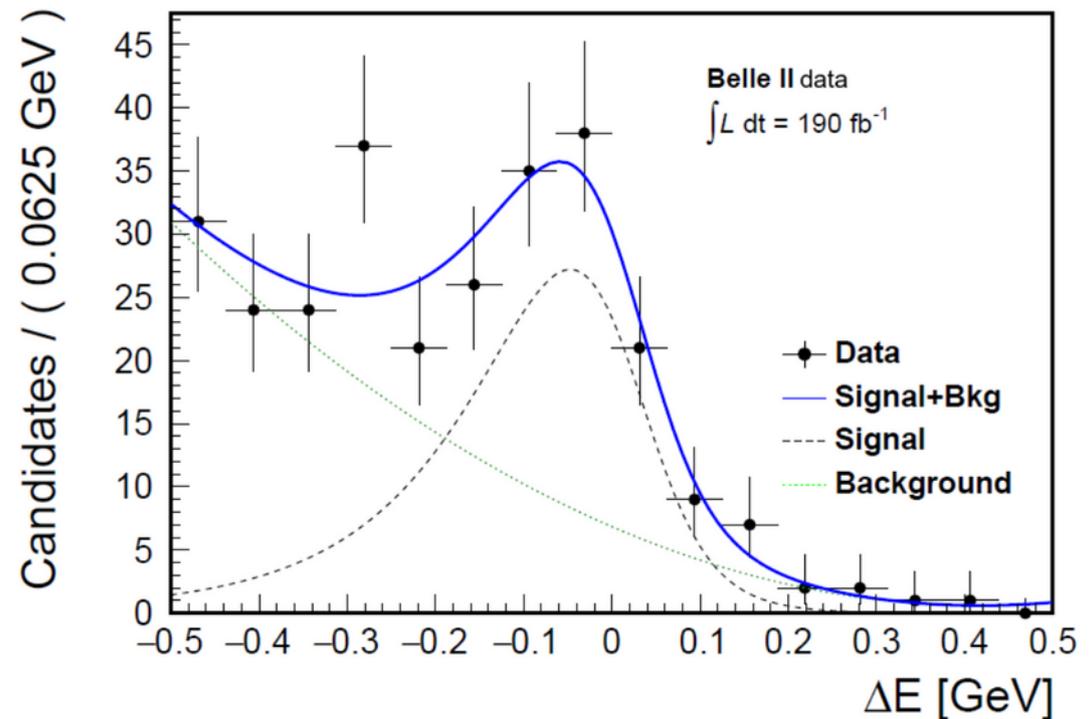


- 28 countries/regions;
- 122 institutions;
- ~1200 active members.

$B \rightarrow K_S \pi^0 \gamma$

arXiv:2206.08280 [hep-ex]

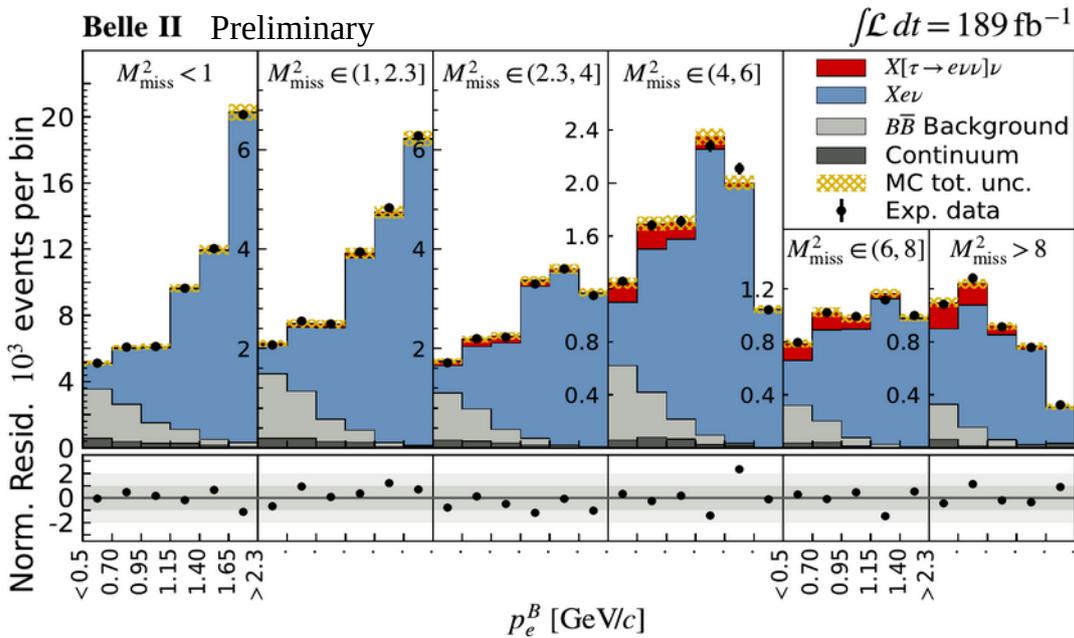
- In the $B \rightarrow K_S \pi^0 \gamma$ decay, the SM predicts the photon to be $\sim 100\%$ polarized;
- A sizable time dependent CP asymmetry, would be a sign of New Physics;
- We measure the branching ratio of this decay, selecting events with:
 $1.4 < E(\gamma) < 4.0$ GeV
 $M(K_S \pi^0) < 1.1$ GeV/ c^2
- We fit the ΔE distribution, and find ~ 120 signal events;
- This gives:



$$\mathcal{B}(B^0 \rightarrow K_S^0 \pi^0 \gamma) = (7.3 \pm 1.8 (\text{stat}) \pm 1.0 (\text{syst})) \times 10^{-6}$$

Measurement of inclusive $R(X)$

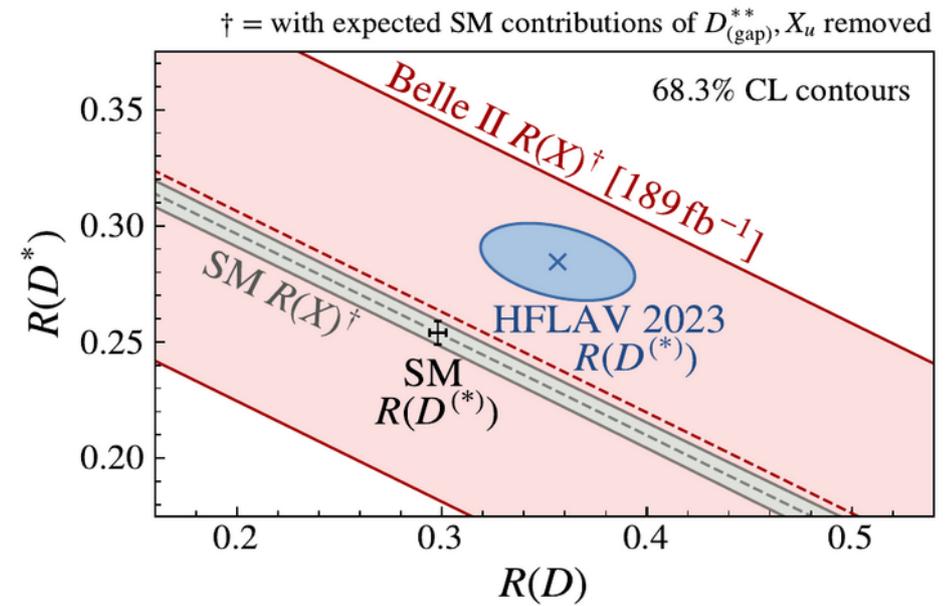
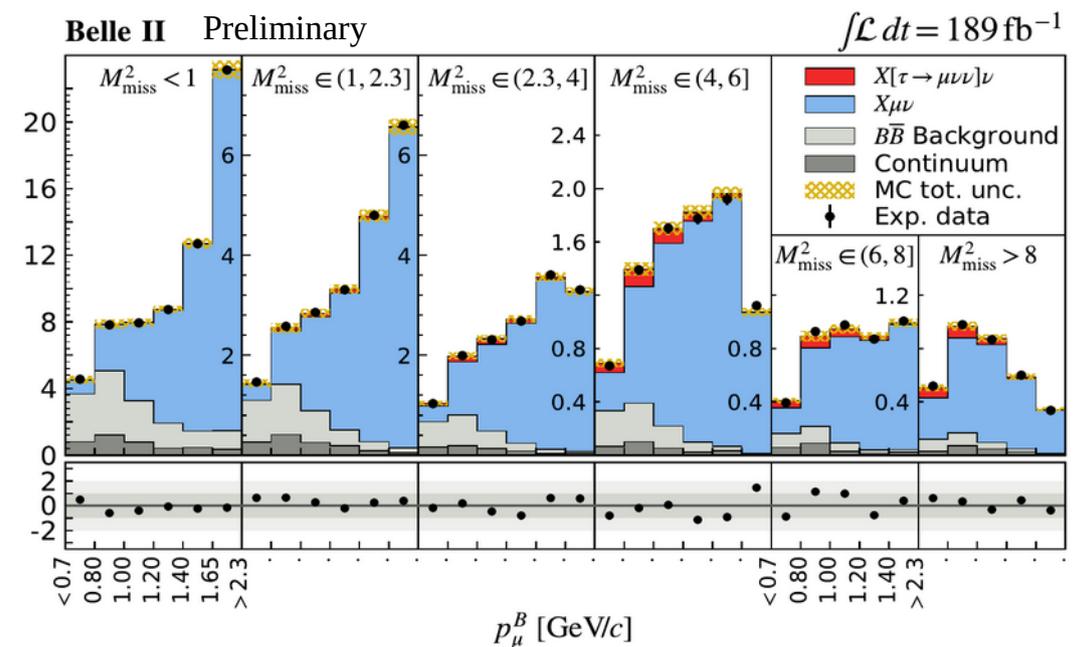
arXiv:2311.07248 [hep-ex]



$$R_{\tau/\ell}(X) = 0.228 \pm 0.016(\text{stat}) \pm 0.036(\text{sys})$$

$$R_{\tau/e}(X) = 0.232 \pm 0.020(\text{stat}) \pm 0.037(\text{sys})$$

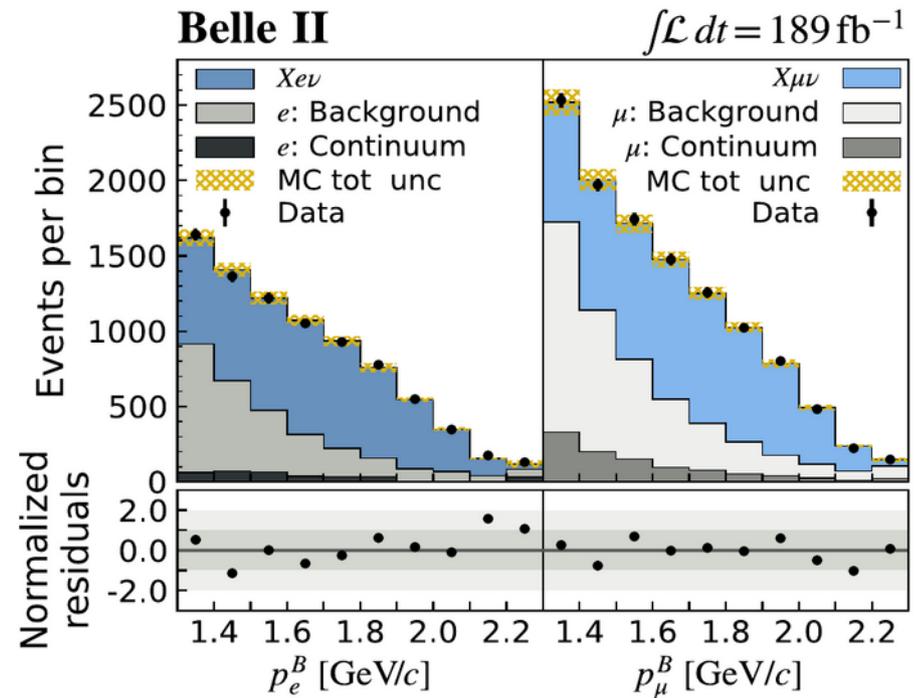
$$R_{\tau/\mu}(X) = 0.222 \pm 0.027(\text{stat}) \pm 0.050(\text{sys})$$



Test of LFU

Phys. Rev. Lett. 131, 051804 (2023)

- We measure: $R(X_{e/\mu}) = \mathcal{B}(B \rightarrow X e \nu) / \mathcal{B}(B \rightarrow X \mu \nu)$ in semileptonic B decays;
- Template fit on CM frame lepton momentum p^*_1 , with $p^*_1 > 1.3 \text{ GeV}$;
- Two main sources of background:
 - 1) continuum, constrained with off-resonance data;
 - 2) other B decays (fake leptons, leptons arising from decay of charmed hadrons, ...), constrained from background enriched control regions;



- Result:

$$R(X_{e/\mu}) = 1.007 \pm 0.009(\text{stat}) \pm 0.019(\text{syst})$$

To date the most precise measurement, in good agreement with the SM. Dominant systematic uncertainty from lepton identification (1.8%).

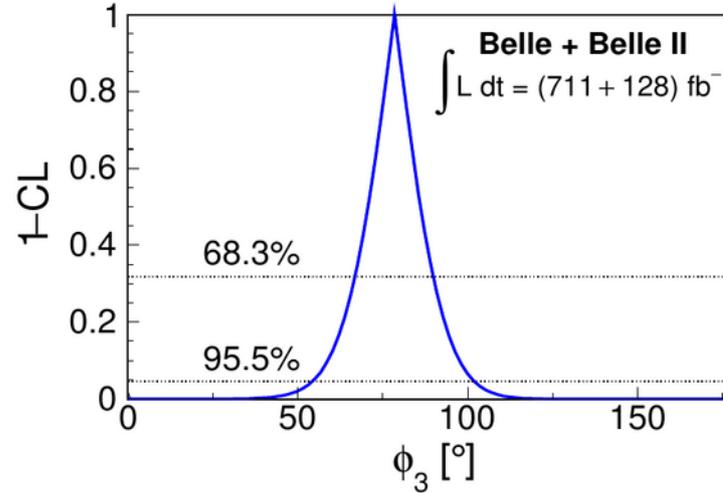
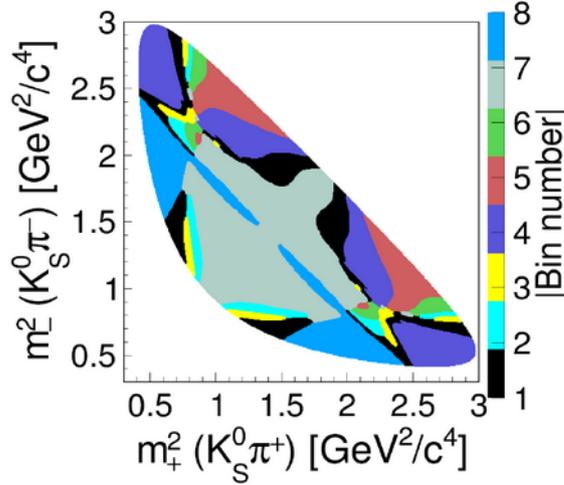
- This paves the way to the first measurement of:

$$R(X) = \frac{\mathcal{B}(B \rightarrow X \tau \nu)}{\mathcal{B}(B \rightarrow X \ell \nu)}$$

Measurements of ϕ_3 / γ

- Best sensitivity from the BPGGSZ method, exploiting the interference in the $D^0 \rightarrow K_S \pi^+ \pi^-$ Dalitz plot:

J. High Energ. Phys. 2022, 63 (2022)



$$\begin{aligned} \phi_3 &= (78.4 \pm 11.4 \pm 0.5 \pm 1.0)^\circ, \\ r_B^{DK} &= 0.129 \pm 0.024 \pm 0.001 \pm 0.002, \\ \delta_B^{DK} &= (124.8 \pm 12.9 \pm 0.5 \pm 1.7)^\circ, \\ r_B^{D\pi} &= 0.017 \pm 0.006 \pm 0.001 \pm 0.001, \\ \delta_B^{D\pi} &= (341.0 \pm 17.0 \pm 1.2 \pm 2.6)^\circ. \end{aligned}$$

- GLW method [Phys.Lett.B 253 (1991) 483-488, Phys.Lett.B 265 (1991) 172-176]: consider decays of the D^0 to odd (-) and even (+) CP eigenstates and measure the observables:

$$\mathcal{A}_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) - \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)} \quad \mathcal{R}_{CP\pm} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{CP\pm} K^-) + \mathcal{B}(B^+ \rightarrow D_{CP\pm} K^+)}{\mathcal{B}(B^- \rightarrow D_{\text{flav}} K^-) + \mathcal{B}(B^+ \rightarrow D_{\text{flav}} K^+)}$$

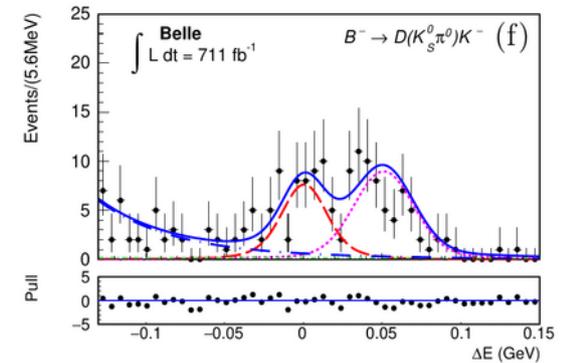
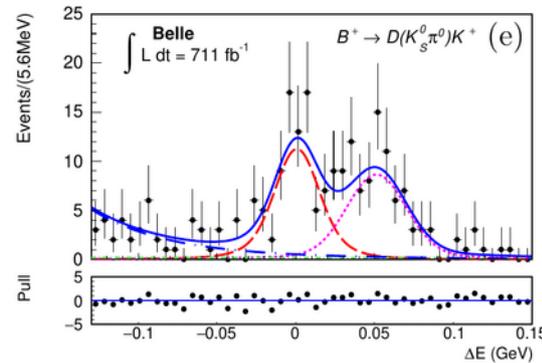
which are related to ϕ_3 :

$$\begin{aligned} \mathcal{R}_{CP\pm} &= 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \phi_3 \\ \mathcal{A}_{CP\pm} &= \pm 2r_B \sin \delta_B \sin \phi_3 / \mathcal{R}_{CP\pm} \end{aligned}$$

Measurements of ϕ_3 / γ

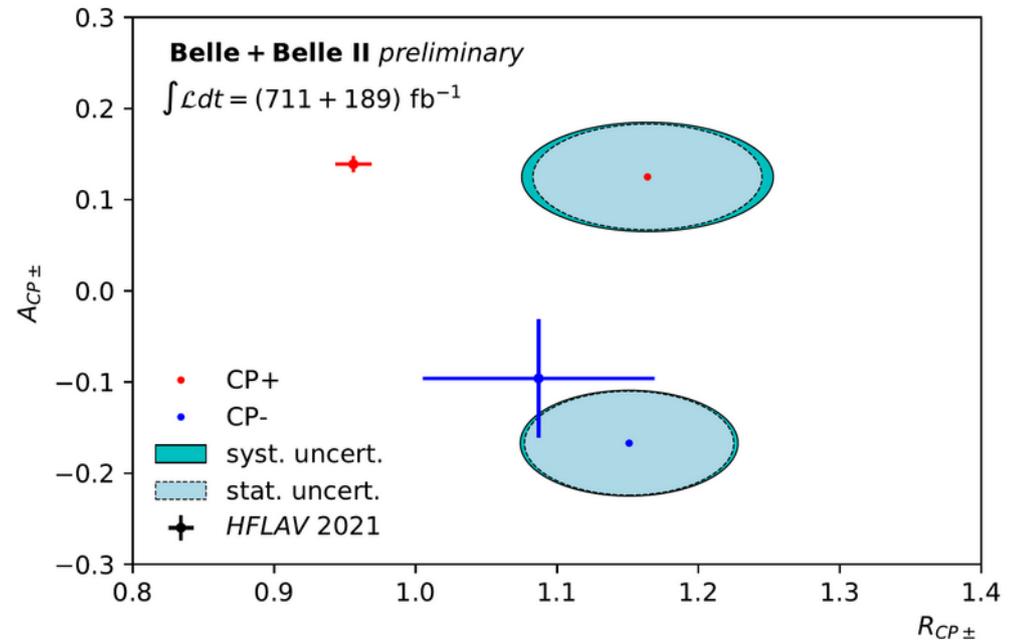
- Considering $D^0 \rightarrow K^+K^-$ as CP+, $D^0 \rightarrow K_s^0\pi^0$ as CP-, and $D^0 \rightarrow K^-\pi^+$ as flavor specific final state, we measure (on the **Belle + Belle II data set**):

$$\begin{aligned} \mathcal{R}_{CP+} &= 1.164 \pm 0.081 \pm 0.036, \\ \mathcal{R}_{CP-} &= 1.151 \pm 0.074 \pm 0.019, \\ \mathcal{A}_{CP+} &= (+12.5 \pm 5.8 \pm 1.4)\%, \\ \mathcal{A}_{CP-} &= (-16.7 \pm 5.7 \pm 0.6)\%. \end{aligned}$$



- The \mathcal{A}_{CP} 's differ from each other at $\sim 3.5\sigma$;
- This translates into constraints on ϕ_3 :

	68.3% CL	95.4% CL
	[8.7, 20.5]	
ϕ_3 ($^\circ$)	[83.8, 96.1]	[4.7, 175.8]
	[163.4, 173.1]	
r_B	[0.282, 0.489]	[0.069, 0.560]

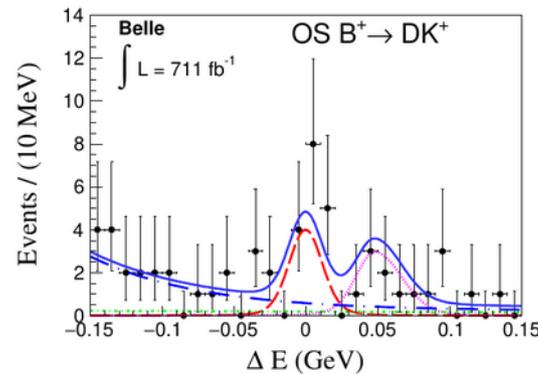
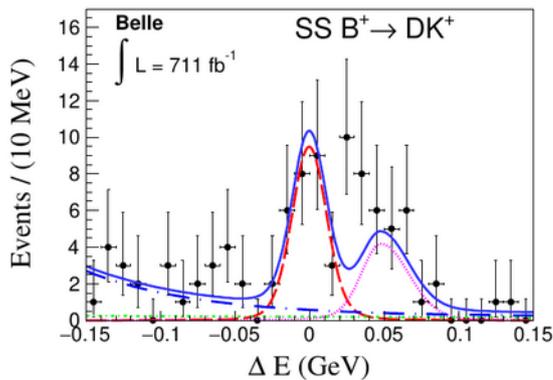


Measurements of ϕ_3/γ

- Other constraints on ϕ_3 can come with the GLS method [[Phys. Rev. D 67, 071301\(R\) \(2003\)](#)];
- We use the Belle + Belle II data sets to reconstruct $B^\pm \rightarrow D^0[K_S K^\pm \pi^\mp] h^\pm$ events;
- Events are split into SS (K and h have same charge) and OS (K and h have opposite charge). We reconstruct the observables:

$$A_m^{Dh} \equiv \frac{N_m^{Dh^-} - N_m^{Dh^+}}{N_m^{Dh^-} + N_m^{Dh^+}} \quad \mathcal{R}_m^{DK/D\pi} \equiv \frac{N_m^{DK^-} + N_m^{DK^+}}{N_m^{D\pi^-} + N_m^{D\pi^+}} \quad \mathcal{R}_{SS/OS}^{D\pi} \equiv \frac{N_{SS}^{D\pi^-} + N_{SS}^{D\pi^+}}{N_{OS}^{D\pi^-} + N_{OS}^{D\pi^+}}$$

$m = SS, OS$



ϕ_3 determination requires also input from BESIII on D decay parameters (work in progress)

$$A_{SS}^{DK} = -0.089 \pm 0.091 \pm 0.011,$$

$$A_{OS}^{DK} = 0.109 \pm 0.133 \pm 0.013,$$

$$A_{SS}^{D\pi} = 0.018 \pm 0.026 \pm 0.009,$$

$$A_{OS}^{D\pi} = -0.028 \pm 0.031 \pm 0.009,$$

$$R_{SS}^{DK/D\pi} = 0.122 \pm 0.012 \pm 0.004,$$

$$R_{OS}^{DK/D\pi} = 0.093 \pm 0.013 \pm 0.003,$$

$$R_{SS/OS}^{D\pi} = 1.428 \pm 0.057 \pm 0.002.$$

$B^+ \rightarrow K^+ \nu \nu$ – HTA systematics

Source	Correction	Uncertainty type, parameters	Uncertainty size	Impact on σ_μ
Normalization of $B\bar{B}$ background	—	Global, 1	30%	0.91
Normalization of continuum background	—	Global, 2	50%	0.58
Leading B -decay branching fractions	—	Shape, 3	$O(1\%)$	0.10
Branching fraction for $B^+ \rightarrow K^+ K_L^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1	20%	0.20
Branching fraction for $B \rightarrow D^{**}$	—	Shape, 1	50%	< 0.01
Branching fraction for $B^+ \rightarrow K^+ n\bar{n}$	q^2 dependent $O(100\%)$	Shape, 1	100%	0.05
Branching fraction for $D \rightarrow K_L^0 X$	+30%	Shape, 1	10%	0.03
Continuum-background modeling, BDT _c	Multivariate $O(10\%)$	Shape, 1	100% of correction	0.29
Number of $B\bar{B}$	—	Global, 1	1.5%	0.07
Track finding efficiency	—	Global, 1	0.3%	0.01
Signal-kaon PID	p, θ dependent $O(10 - 100\%)$	Shape, 3	$O(1\%)$	< 0.01
Extra-photon multiplicity	$n_{\gamma\text{extra}}$ dependent $O(20\%)$	Shape, 1	$O(20\%)$	0.61
K_L^0 efficiency	—	Shape, 1	17%	0.31
Signal SM form-factors	q^2 dependent $O(1\%)$	Shape, 3	$O(1\%)$	0.06
Signal efficiency	—	Shape, 6	16%	0.42
Simulated-sample size	—	Shape, 18	$O(1\%)$	0.60

$B^+ \rightarrow K^+ \nu \nu$ – ITA systematics

Source	Correction	Uncertainty type, parameters	Uncertainty size	Impact on σ_μ
Normalization of $B\bar{B}$ background	—	Global, 2	50%	0.90
Normalization of continuum background	—	Global, 5	50%	0.10
Leading B -decay branching fractions	—	Shape, 5	$O(1\%)$	0.22
Branching fraction for $B^+ \rightarrow K^+ K_L^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1	20%	0.49
p-wave component for $B^+ \rightarrow K^+ K_S^0 K_L^0$	q^2 dependent $O(100\%)$	Shape, 1	30%	0.02
Branching fraction for $B \rightarrow D^{**}$	—	Shape, 1	50%	0.42
Branching fraction for $B^+ \rightarrow K^+ n \bar{n}$	q^2 dependent $O(100\%)$	Shape, 1	100%	0.20
Branching fraction for $D \rightarrow K_L^0 X$	+30%	Shape, 1	10%	0.14
Continuum-background modeling, BDT _c	Multivariate $O(10\%)$	Shape, 1	100% of correction	0.01
Integrated luminosity	—	Global, 1	1%	< 0.01
Number of $B\bar{B}$	—	Global, 1	1.5%	0.02
Off-resonance sample normalization	—	Global, 1	5%	0.05
Track-finding efficiency	—	Shape, 1	0.3%	0.20
Signal-kaon PID	p, θ dependent $O(10 - 100\%)$	Shape, 7	$O(1\%)$	0.07
Photon energy	—	Shape, 1	0.5%	0.08
Hadronic energy	-10%	Shape, 1	10%	0.37
K_L^0 efficiency in ECL	-17%	Shape, 1	8%	0.22
Signal SM form-factors	q^2 dependent $O(1\%)$	Shape, 3	$O(1\%)$	0.02
Global signal efficiency	—	Global, 1	3%	0.03
Simulated-sample size	—	Shape, 156	$O(1\%)$	0.52

$R(D^*)$ – systematics

Source	Uncertainty
PDF shapes	+9.1% −8.3%
MC statistics	+7.5% −7.5%
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ branching fractions	+4.8% −3.5%
Fixed backgrounds	+2.7% −2.3%
Hadronic B decay branching fractions	+2.1% −2.1%
Reconstruction efficiency	+2.0% −2.0%
Kernel density estimation	+2.0% −0.8%
Form factors	+0.5% −0.1%
Peaking background on ΔM_{D^*}	+0.4% −0.4%
$\tau^- \rightarrow \ell^- \nu_\tau \bar{\nu}_\ell$ branching fractions	+0.2% −0.2%
$R(D^*)$ fit method	+0.1% −0.1%
Total systematic uncertainty	+13.5% −12.3%