



New non-leptonic hadron decay
results at e^+e^- experiments

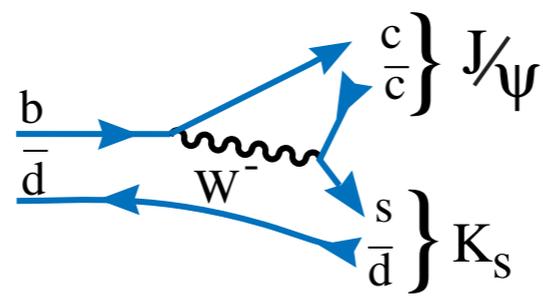
Angelo Di Canto



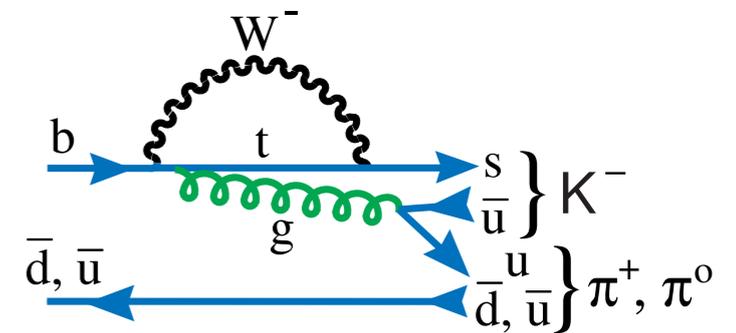
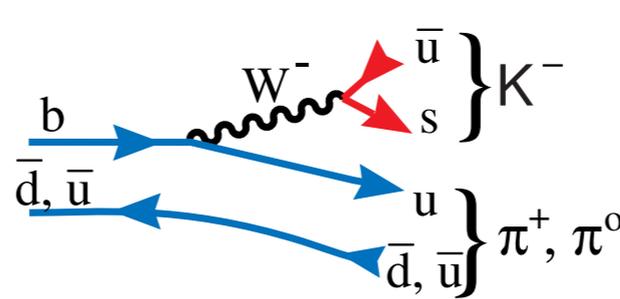
Non-leptonic hadron decays

- Non-leptonic b - and c -hadron decays offer plenty of ways to measure flavor and CP violation

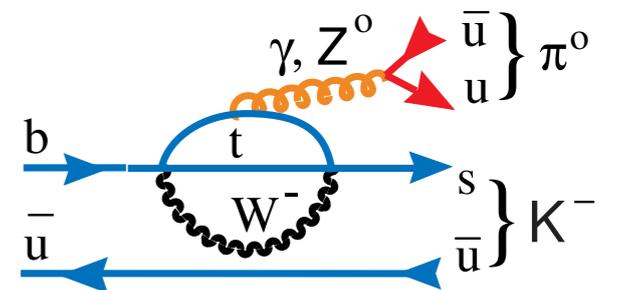
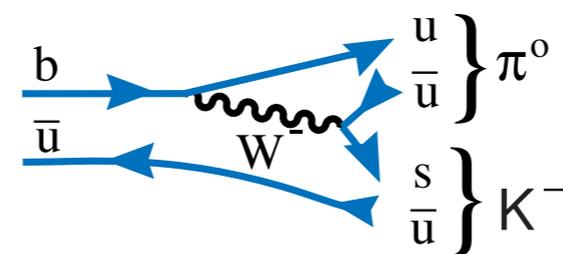
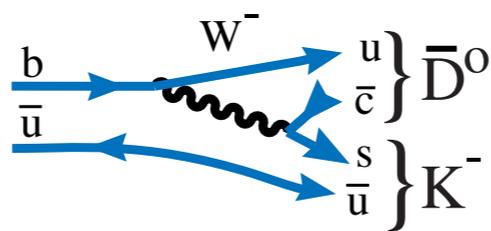
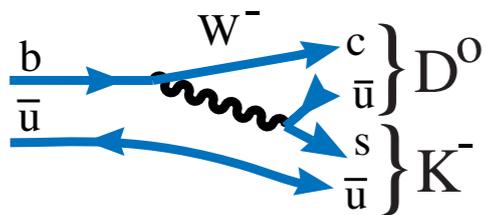
$$b \rightarrow c\bar{c}$$



$$b \rightarrow \text{no } c$$



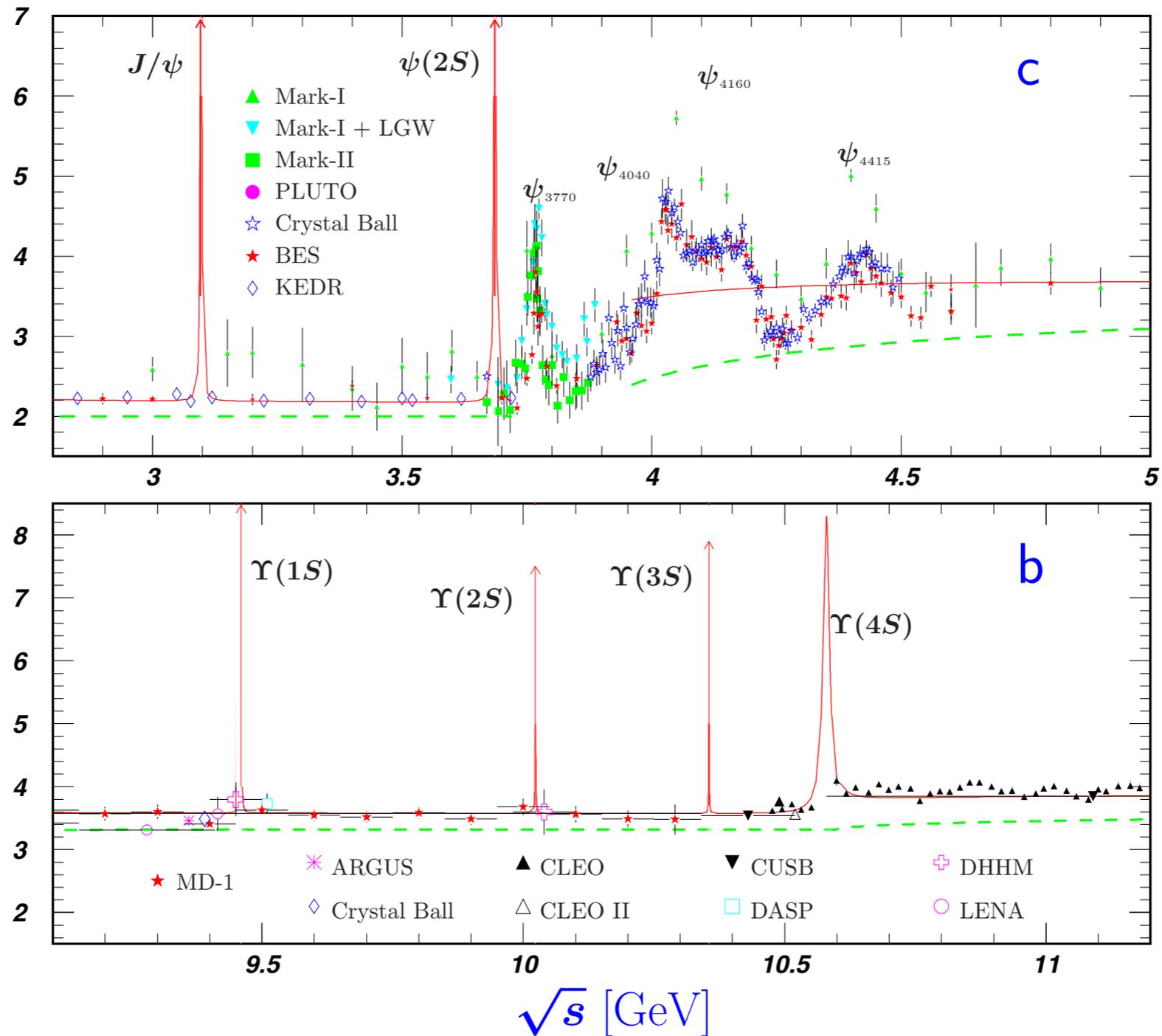
$$b \rightarrow c$$



[diagrams from PMC Physics A 2009, 3:3]

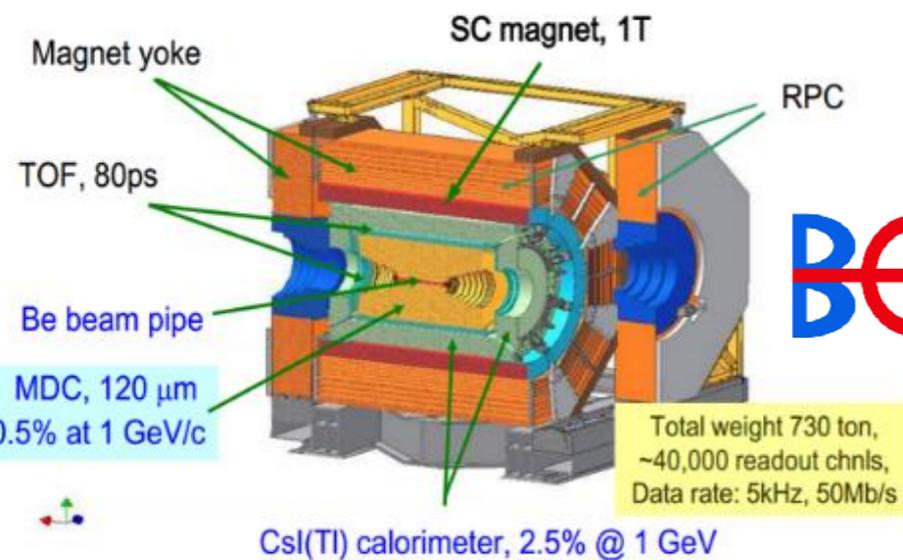
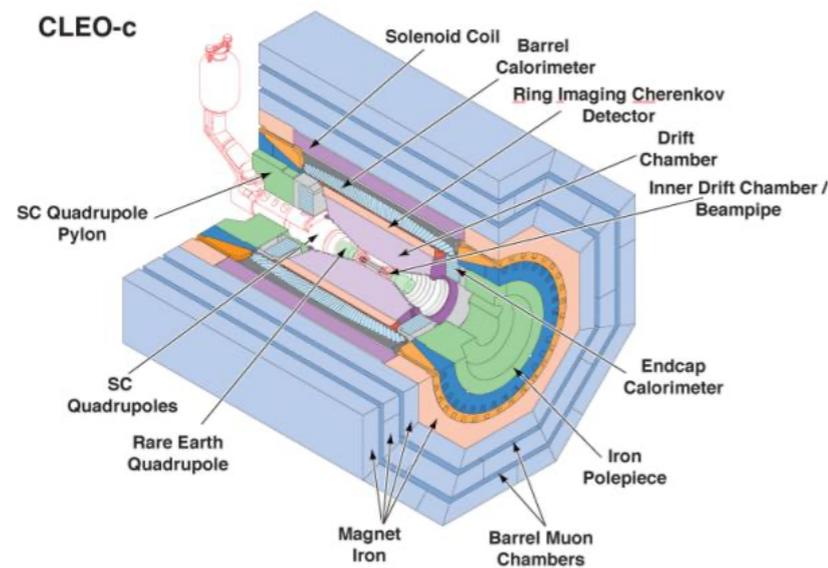
Experiments at e^+e^- colliders

$$R = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

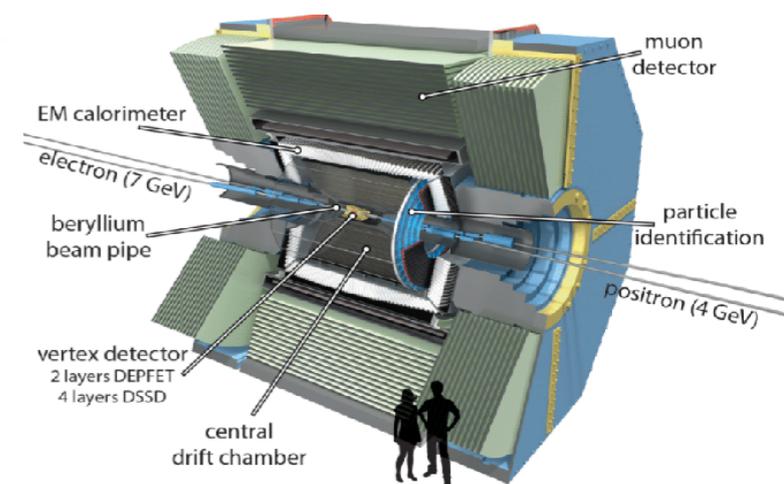
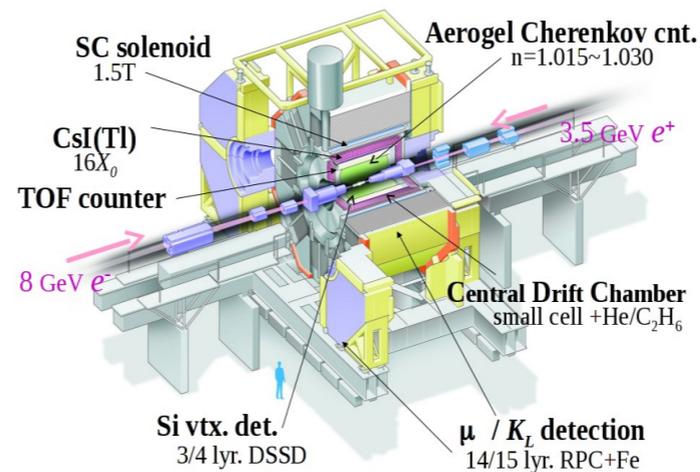
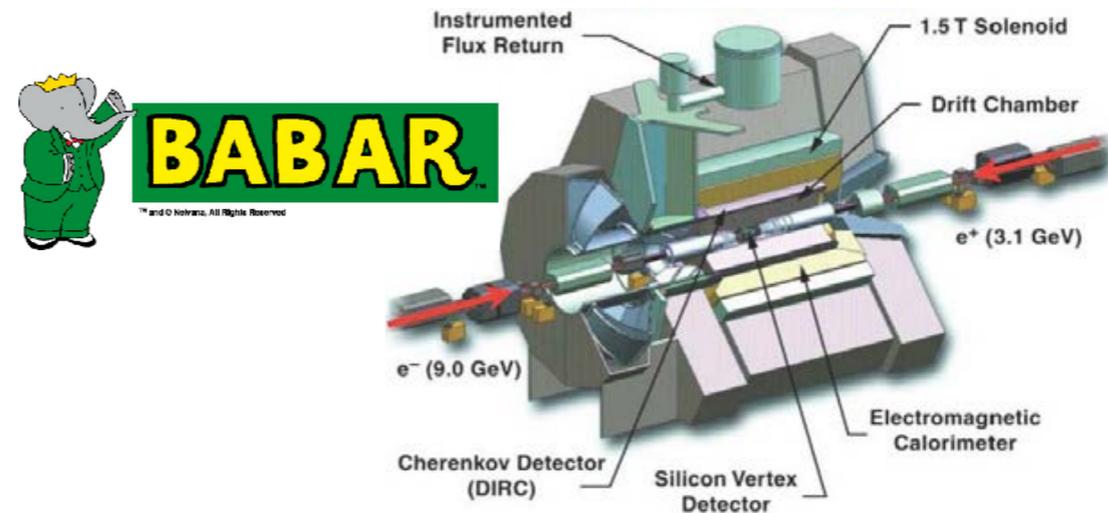


Experiments at e^+e^- colliders

Charm factories



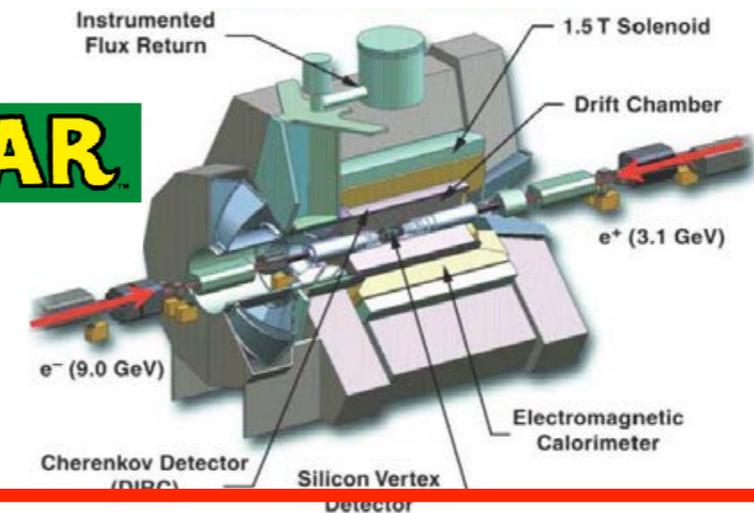
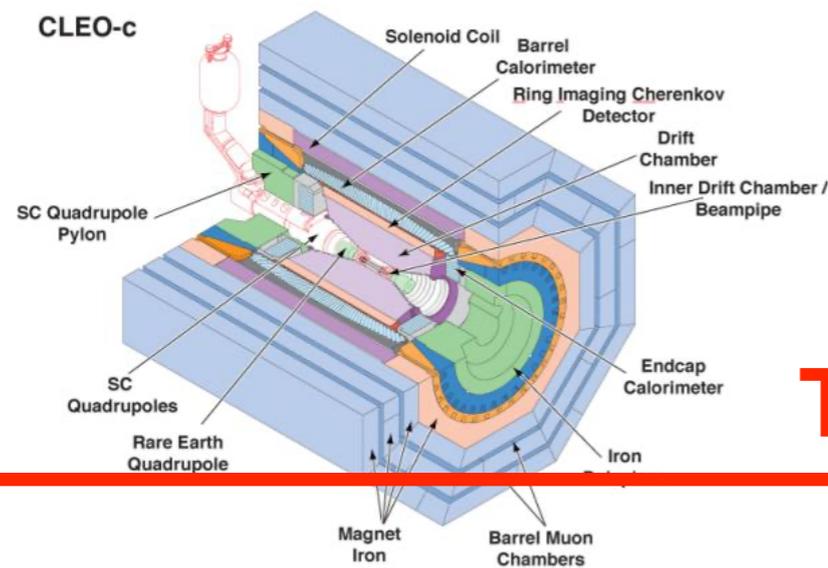
Beauty factories



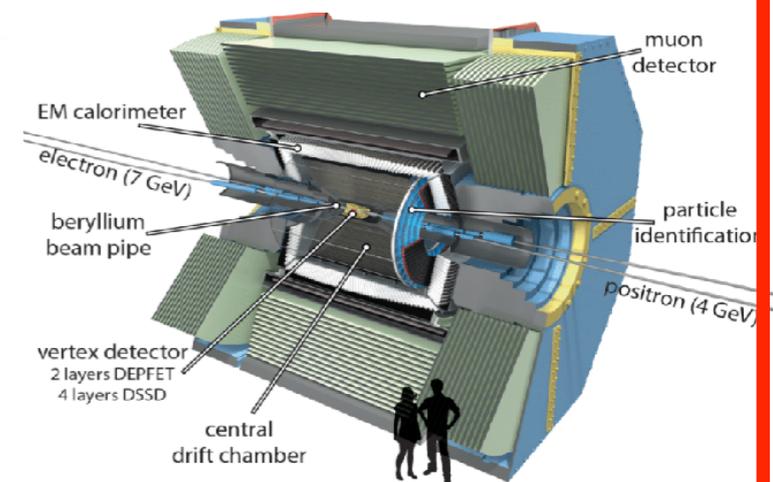
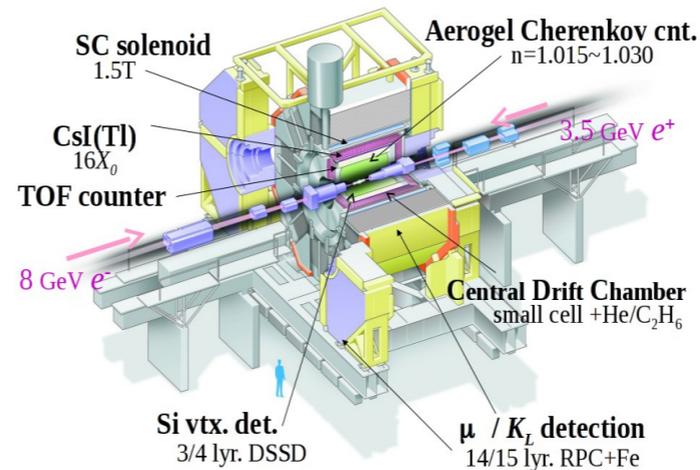
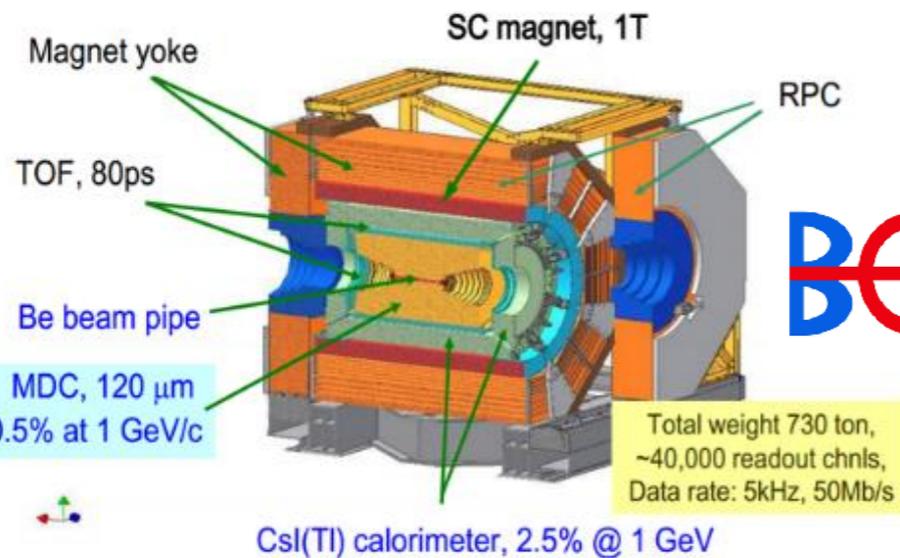
Experiments at e^+e^- colliders

Charm factories

Beauty factories



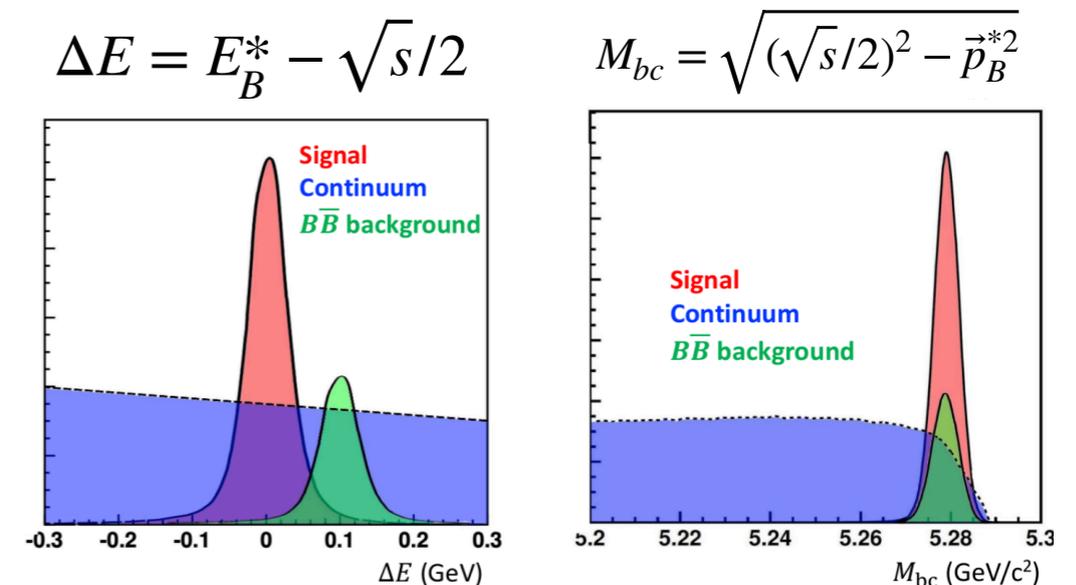
This talk



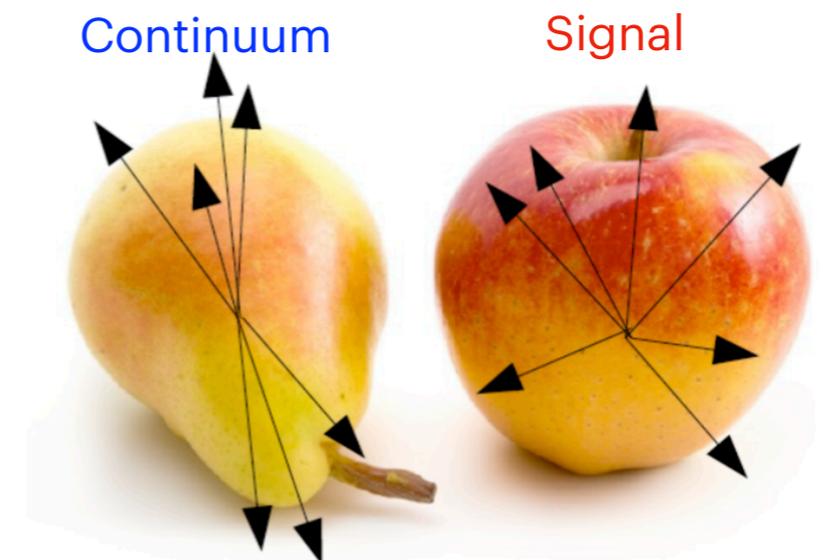
Non-leptonic hadron decays at e^+e^- colliders

- Coherent production of meson-antimeson pairs with kinematics constrained by precisely known collision energy
 - Efficient flavor tagging for CP violation measurements
- Simple and clean event topologies: hadronic events have typically $O(10)$ particles
- Asymmetric-energy colliders: boosted production for time-dependent measurements
- Hermetic detectors: excellent (and kinematically unbiased) efficiencies for all final states, including neutral hadrons such as π^0 , η , K_S^0 , K_L^0 , \bar{n}

Kinematics



Event topology



Disclaimer

Too much to cover,
selection of results
heavily biased by my
personal interests

Many more results will be
discussed by speakers in
the parallel sessions

Search for $B_s \rightarrow \pi^0 \pi^0$	PRD 107 (2023) L051101
Study of $B^+ \rightarrow \rho \bar{n} \pi^0$	2211.11251
Mass, width and BFs of $\Lambda_c(2625)^+ \rightarrow \Sigma_c^0 \pi^+$ and $\Sigma_c^{++} \pi^-$	PRD 107 (2023) 032008
BFs of $\Lambda_c^+ \rightarrow \rho K_S^0 K_S^0$ and $\rho K_S^0 \eta$	PRD 107 (2023) 032004
Evidence for the SCS decay $\Omega_c^0 \rightarrow \Xi^- \pi^+$ and search for $\Omega_c^0 \rightarrow \Xi^- K^+$ and $\Omega^- K^+$	JHEP 01 (2023) 055
BFs of $\Lambda_c^+ \rightarrow \Sigma^+ \eta^{(\prime)}$ and asymmetry parameters of $\Lambda_c^+ \rightarrow \Sigma^+ \pi^0$ and $\Sigma^+ \eta^{(\prime)}$	PRD 107 (2023) 012003
BFs, asymmetry parameters and CPV for $\Lambda_c^+ \rightarrow \Lambda h^+$ and $\Sigma^0 h^+$	Sci. Bull. 68 (2023) 583
First measurement of the $B^+ \rightarrow \pi^+ \pi^0 \pi^0$ BF and CP asymmetry	PRL 130 (2023) 181804
BF and CPV in $D^0 \rightarrow K_S^0 K_S^0 \pi^+ \pi^-$	PRD 107 (2023) 052001
Search for $D^+ \rightarrow K^- K_S^0 \pi^+ \pi^+ \pi^0$	2207.06595
BFs of $B^0 \rightarrow D^{*+} h^-$ and tests of QCD factorization	PRD 107 (2023) 012003
...	
Observation of $B \rightarrow D^{(*)} K^- K_S^0$	2305.01321
Novel method for charm flavor tagging	2304.02042
BF and CPV of $B^0 \rightarrow \pi^0 \pi^0$	2303.08354
Ω_c^0 lifetime	PRD 107 (2023) L031103
BF and longitudinal polarization of $B^0 \rightarrow \rho^+ \rho^-$	2208.03554
...	
CP-even fraction of $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	2305.03975
BF for $\Lambda_c^+ \rightarrow \Sigma^+ h^+ h^- (\pi^0)$	2304.09405
BF of $\psi(2S) \rightarrow \phi K_S^0 K_S^0$	2303.08317
BFs of $D^{0/+} \rightarrow K_S^0 X$	2302.14488
Observation of $D^0 \rightarrow \phi \omega$	PRL128(2022)011803
BFs of $D^{0/+} \rightarrow \pi^+ \pi^+ \pi^- X$	PRD 107 (2023) 032002
BF of $D_s^+ \rightarrow \pi^+ \pi^+ \pi^- X$	2212.13072
Observation of $\psi(3770) \rightarrow \eta J/\psi$	2212.12165
Amplitude analysis of $D^0 \rightarrow K_L^0 \pi^+ \pi^-$	2212.09048
CP-even fraction of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	PRD 107 (2023) 032009
...	



Hadronic decays as tools/inputs for other channels



$$D_{(s)} \rightarrow \pi^+ \pi^- \pi^+ X$$

- LHCb $R(D^*)$ measurement with the 3-prong τ channel suffers from limited knowledge of the leading and sub-leading backgrounds from $D_{s^+} \rightarrow \pi^+ \pi^- \pi^+ X$ and $D^{0/+} \rightarrow \pi^+ \pi^- \pi^+ X$ decays
- BESIII has measured these inclusive BFs for the first time

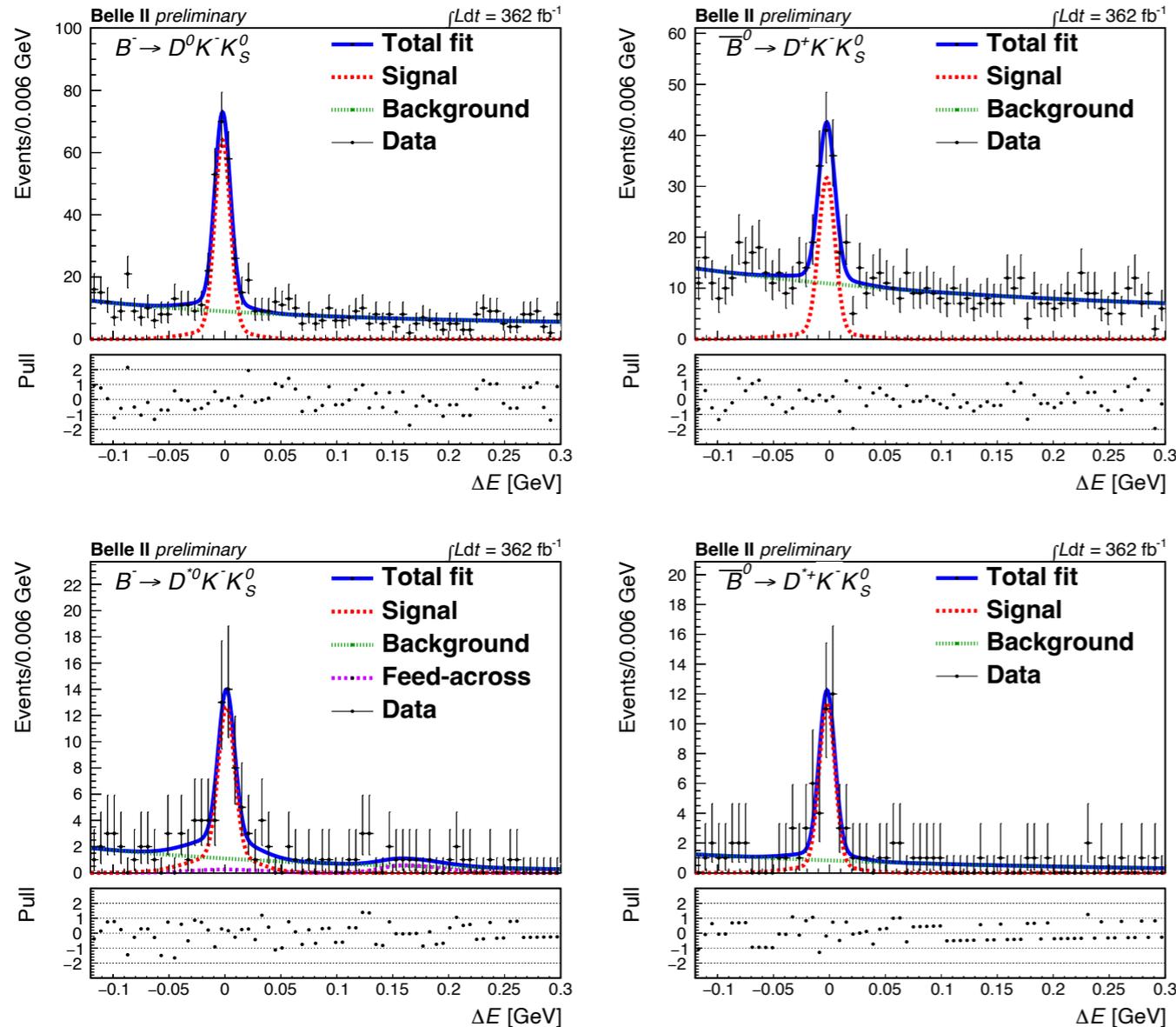
$$\mathcal{B}(D_s^+ \rightarrow \pi^+ \pi^+ \pi^- X) = (32.81 \pm 0.35 \pm 0.82)\%$$

$$\mathcal{B}(D^0 \rightarrow \pi^+ \pi^+ \pi^- X) = (17.60 \pm 0.11 \pm 0.22)\%$$

$$\mathcal{B}(D^+ \rightarrow \pi^+ \pi^+ \pi^- X) = (15.25 \pm 0.09 \pm 0.18)\%$$

- The result for the D_{s^+} channel is $\sim 25\%$ larger than the sum of the known exclusive BFs, implying that many exclusive D_{s^+} decays containing $\pi^+ \pi^- \pi^+$ are still unmeasured
- The results for the $D^{0/+}$ channels are instead consistent with the sum of the known exclusive BFs, indicating little room of unobserved exclusive decays

Observation of $B \rightarrow D^{(*)}K-K_S^0$ decays



- About 40% of the total B width is not measured in terms of exclusive branching fractions

- Limits the accuracy of the simulation and the performance of the hadronic tagging

- $\text{BF}(B \rightarrow DKK)$ could be as large as 6%, but only a small fraction of its exclusive modes is known

- Highly pure signal observed

- Improved $\text{BF}(B^- \rightarrow D^0 K^- K_S^0)$ by more than a factor 3 and discovery of three other channels

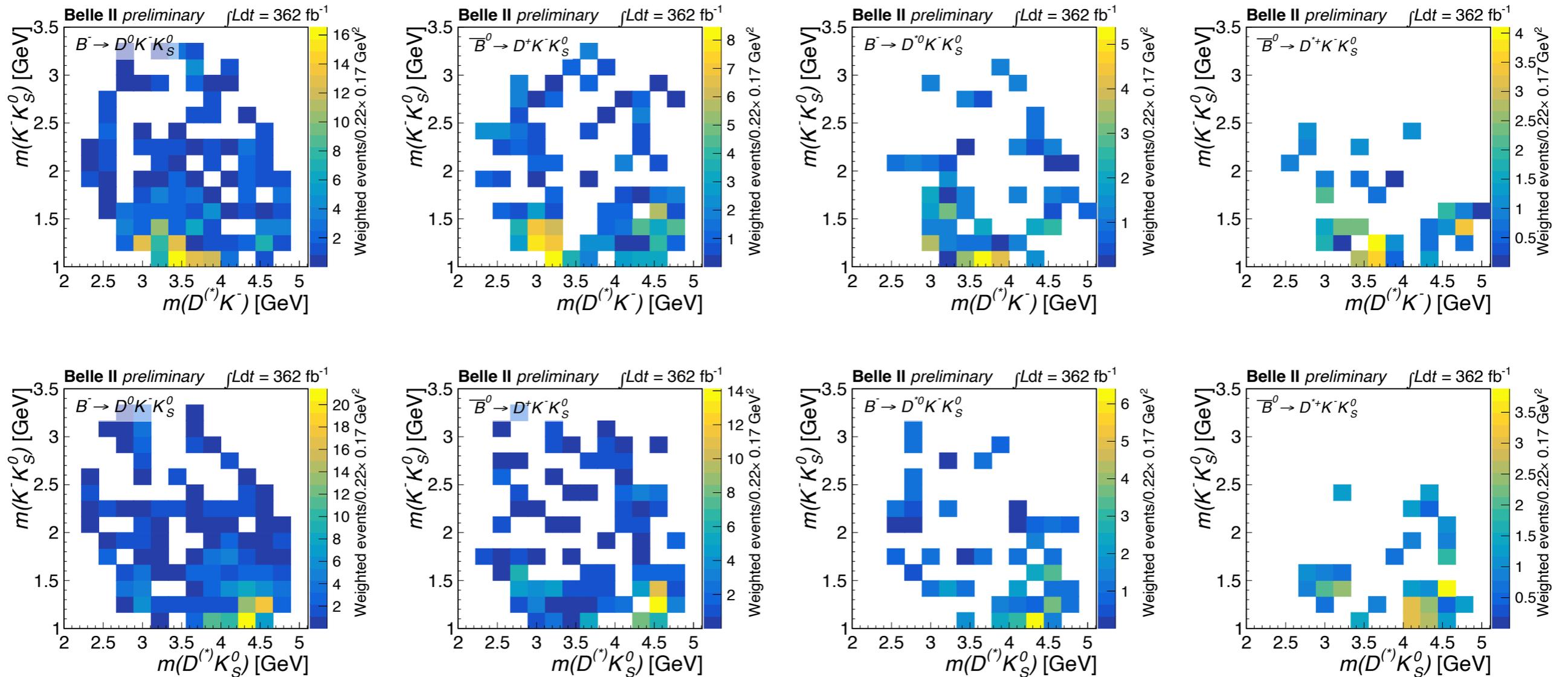
$$\mathcal{B}(B^- \rightarrow D^0 K^- K_S^0) = (1.89 \pm 0.16 \pm 0.10) \times 10^{-4}$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^- K_S^0) = (0.85 \pm 0.11 \pm 0.05) \times 10^{-4}$$

$$\mathcal{B}(B^- \rightarrow D^{*0} K^- K_S^0) = (1.57 \pm 0.27 \pm 0.12) \times 10^{-4}$$

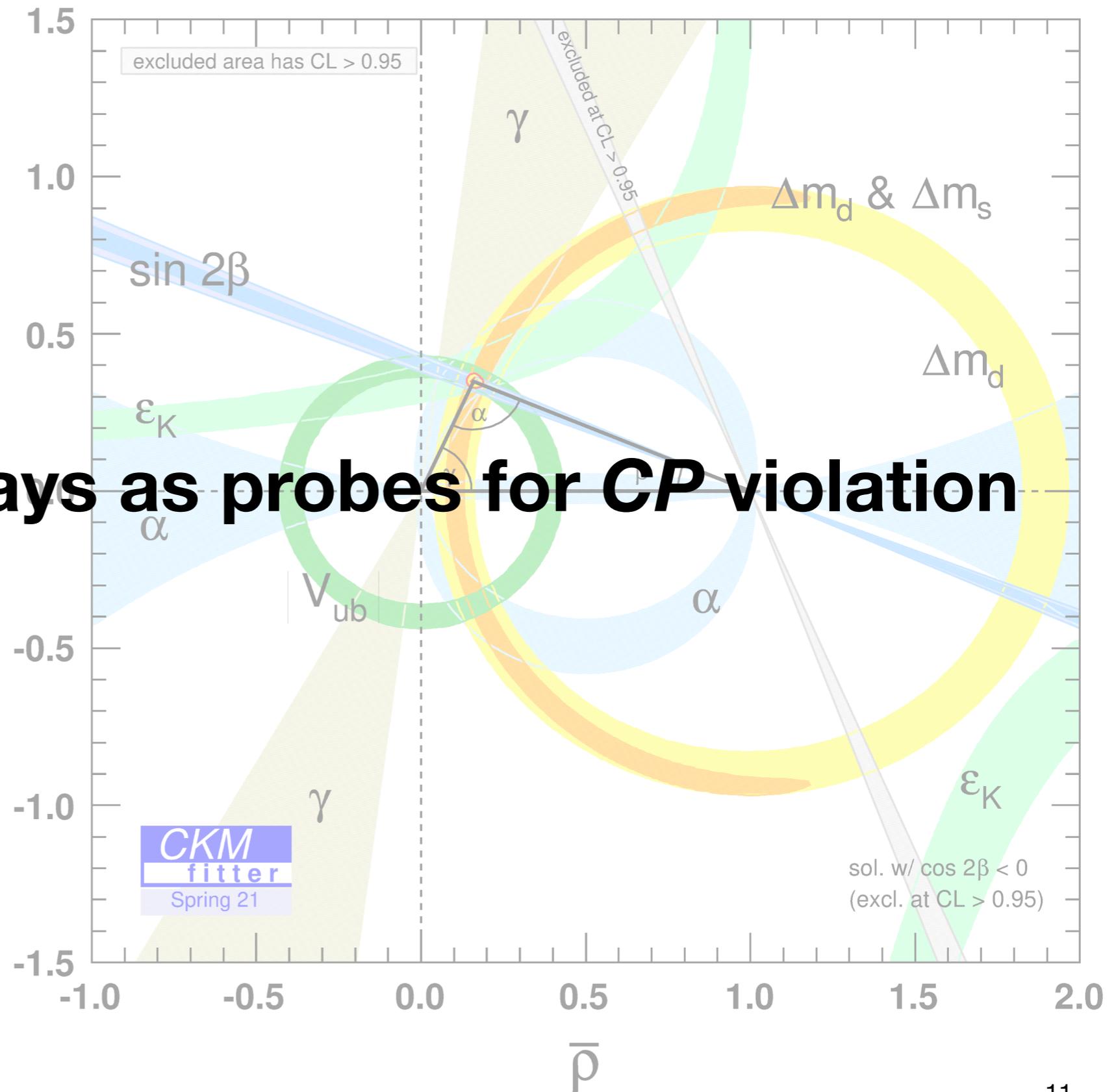
$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^- K_S^0) = (0.96 \pm 0.18 \pm 0.06) \times 10^{-4}$$

Observation of $B \rightarrow D^{(*)}K-K_S^0$ decays



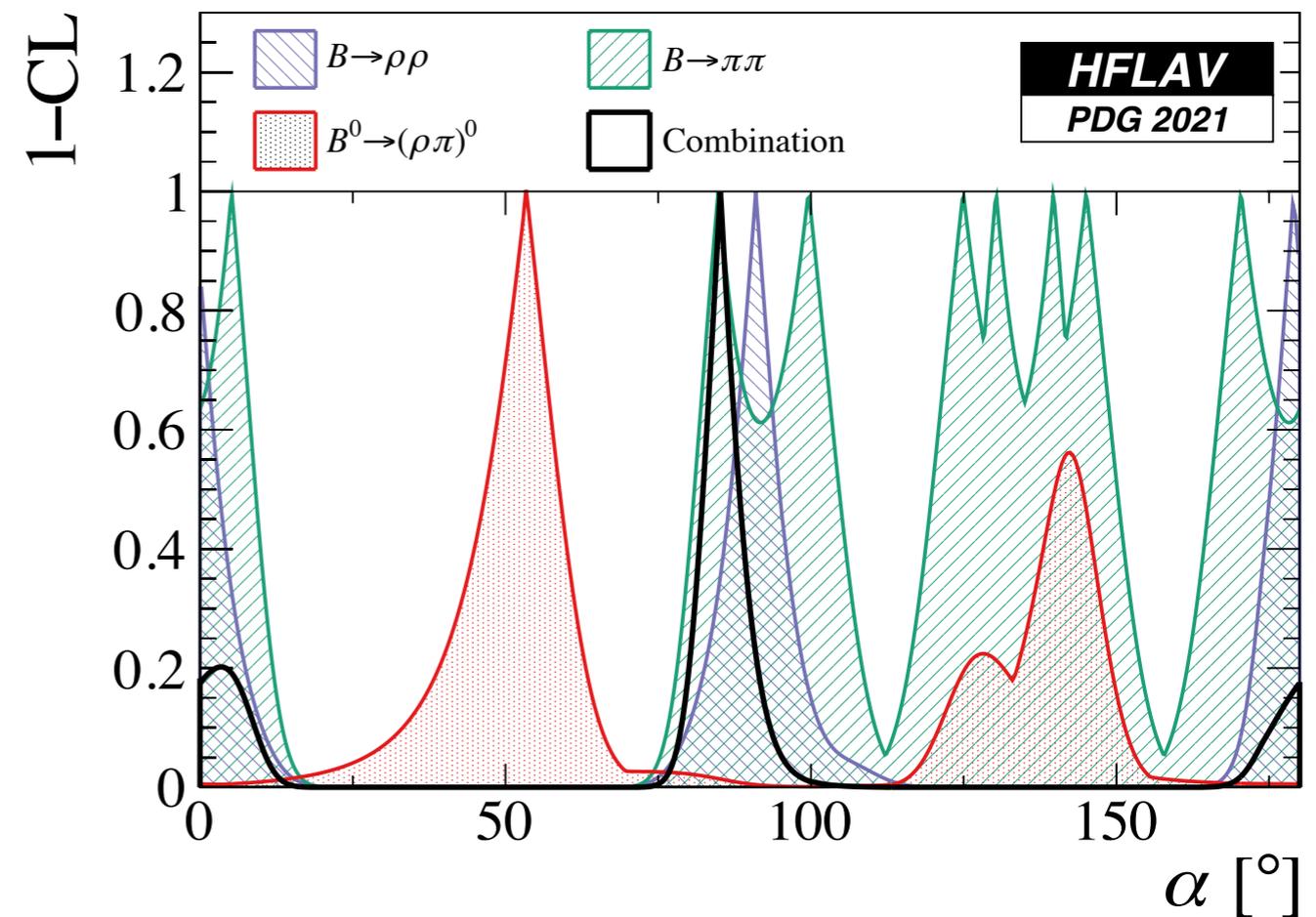
- Clear structures observed in the Dalitz plot of each decay (require further study)

Hadronic B decays as probes for CP violation



CKM angle α

- Charmless B decays give access to α , the least known angle of the CKM unitarity triangle
- Combinations of measurements from isospin-related decays reduce the impact of hadronic uncertainties and yield $\sim 5^\circ$ uncertainty
- Belle II accesses all inputs and expects to reach $O(1^\circ)$ precision with $O(10/\text{ab})$
- Need to be accompanied by an improved understanding of the size of isospin breaking (e.g., using $B \rightarrow \pi\eta^{(\prime)}$)

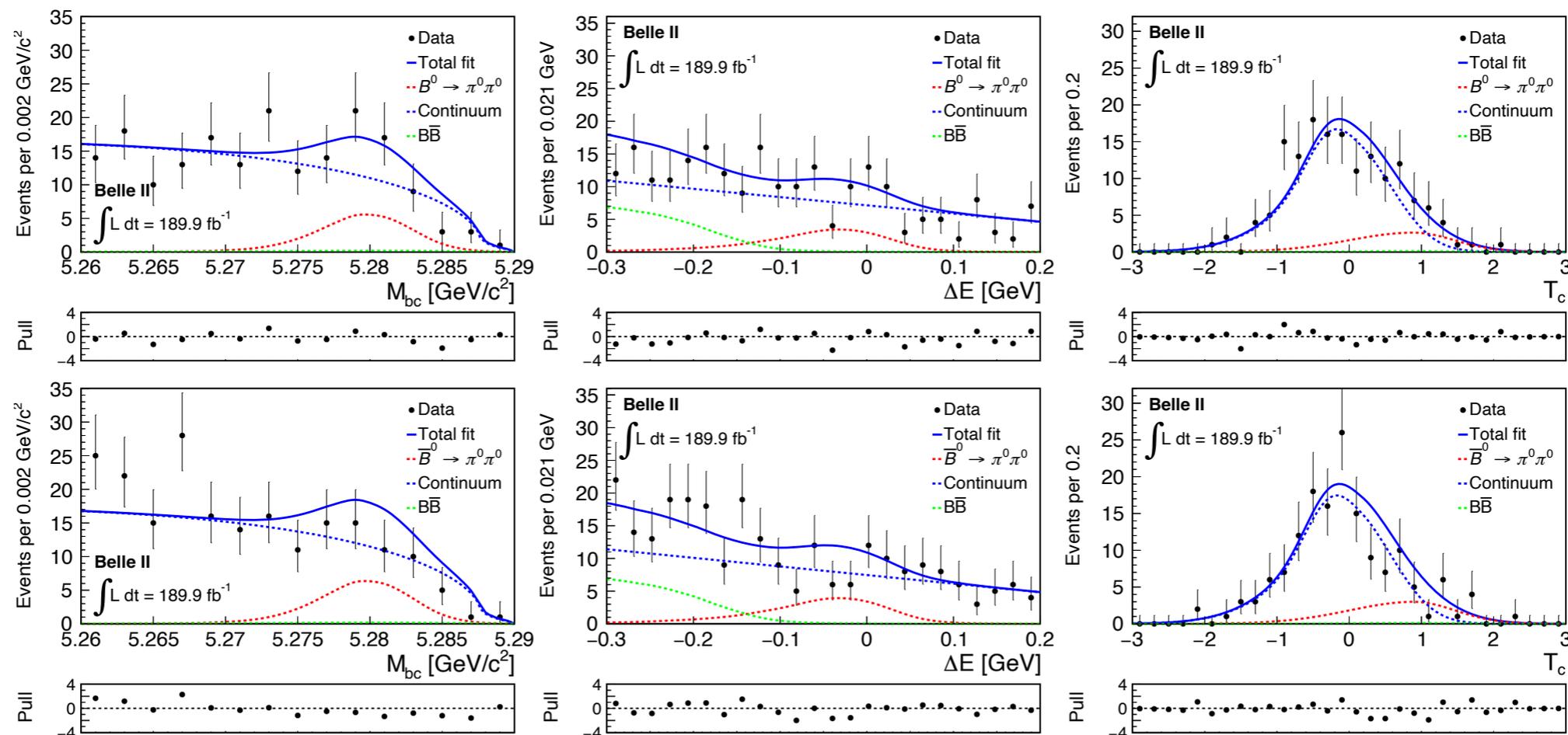


Towards CKM angle α with $B \rightarrow \pi\pi$

- $B^0 \rightarrow \pi^0 \pi^0$ only accessible in e^+e^- collisions
 - Rare: CKM- and color-suppressed
 - Only photons in the final state
 - Requires efficient flavor tagging
- Belle II measurement achieves Belle's precision using only 1/3 of data

$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = (1.38 \pm 0.27 \pm 0.22) \times 10^{-6}$$

$$\mathcal{A}_{CP}(B^0 \rightarrow \pi^0 \pi^0) = 0.14 \pm 0.46 \pm 0.07$$



For $B \rightarrow \pi^+\pi^-$, $\pi^+\pi^0$ (and $\rho\rho$) results see S. Raiz's talk

$B \rightarrow K\pi$ isospin sum-rule

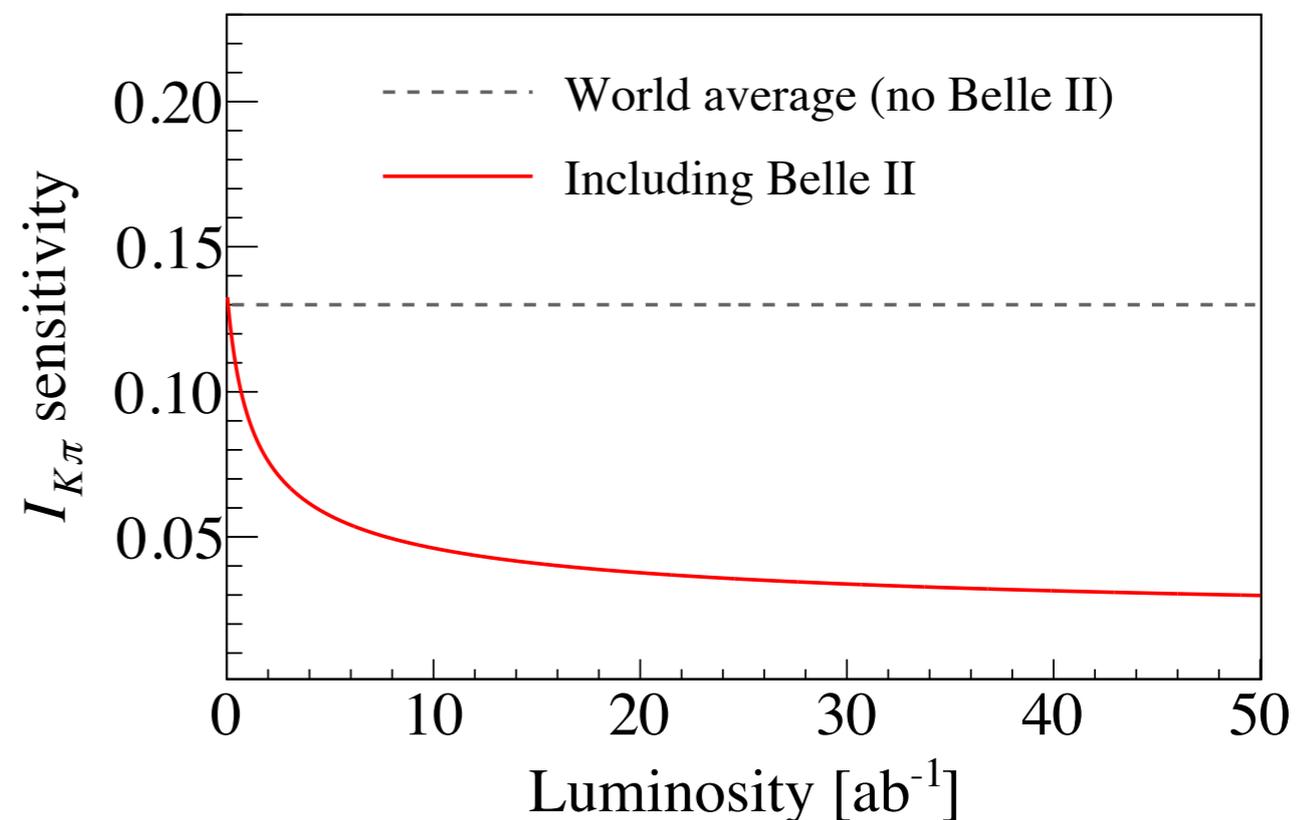
- Appropriate combination of channels suppresses unknowns offering a 1%-level null-test of the SM

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0) \tau_{B^0}}{\mathcal{B}(K^+\pi^-) \tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

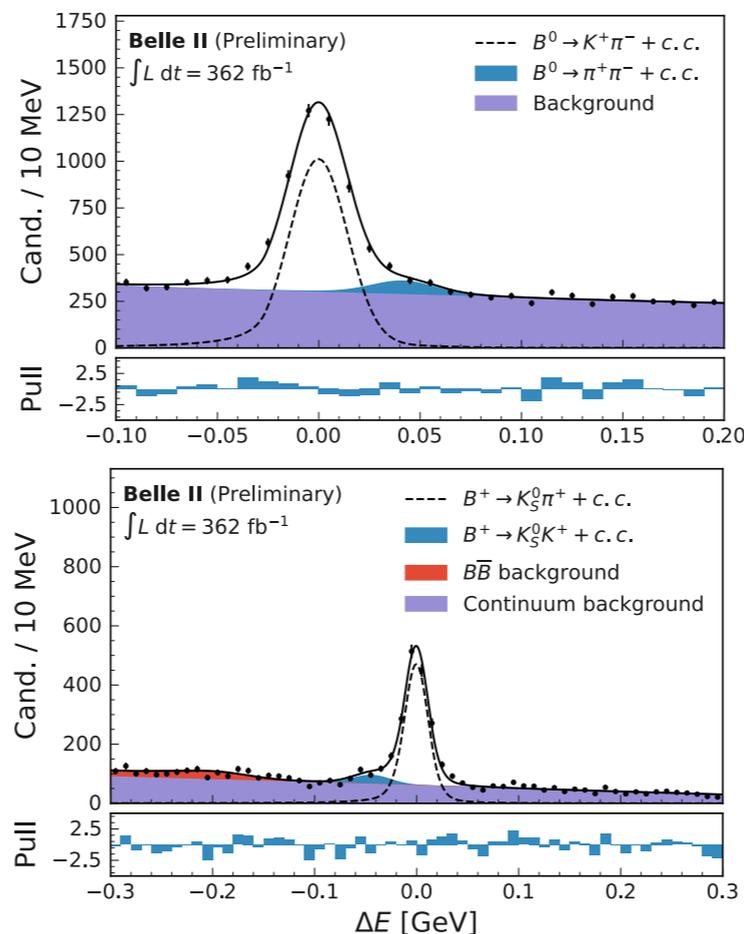
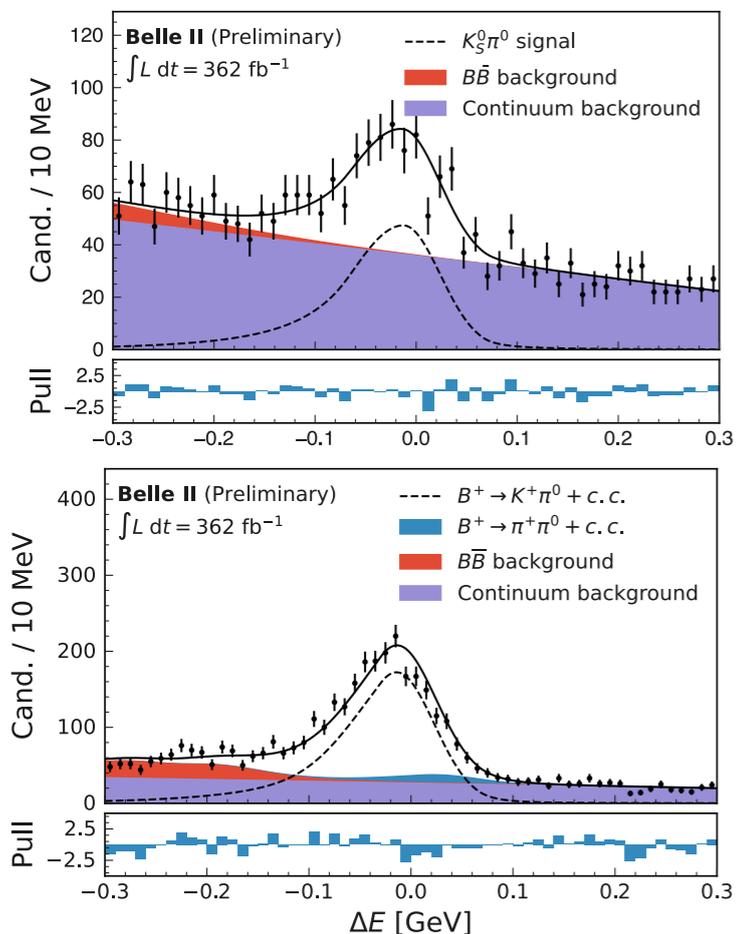
- Current world average

$$I_{K\pi} = 0.13 \pm 0.11$$

limited by $B \rightarrow K^0\pi^0$, which in the foreseeable future can only be measured at Belle II



$B \rightarrow K\pi$ isospin sum-rule



$$B^0 \rightarrow K^+ \pi^-$$

$$\mathcal{B}(K^+ \pi^-) = (20.67 \pm 0.37 \pm 0.62) \times 10^{-6}$$

$$\mathcal{A}_{CP}(K^+ \pi^-) = -0.072 \pm 0.019 \pm 0.007$$

$$B^+ \rightarrow K_S^0 \pi^+$$

$$\mathcal{B}(K_S^0 \pi^+) = (24.40 \pm 0.71 \pm 0.86) \times 10^{-6}$$

$$\mathcal{A}_{CP}(K_S^0 \pi^+) = +0.046 \pm 0.029 \pm 0.007$$

$$B^+ \rightarrow K^+ \pi^0$$

$$\mathcal{B}(K^+ \pi^0) = (13.93 \pm 0.38 \pm 0.84) \times 10^{-6}$$

$$\mathcal{A}_{CP}(K^+ \pi^0) = +0.013 \pm 0.027 \pm 0.005$$

$$B^0 \rightarrow K_S^0 \pi^0$$

$$\mathcal{B}(K_S^0 \pi^0) = (10.16 \pm 0.65 \pm 0.67) \times 10^{-6}$$

$$\mathcal{A}_{CP}(K_S^0 \pi^0) = -0.006 \pm 0.15 \pm 0.05$$

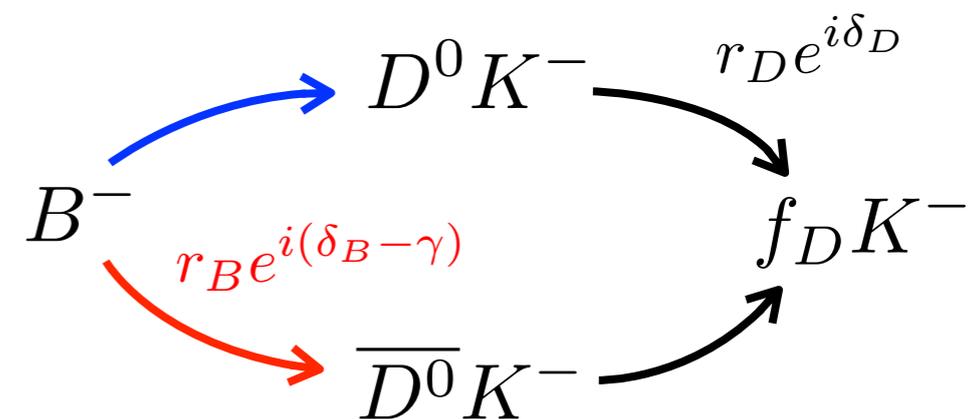
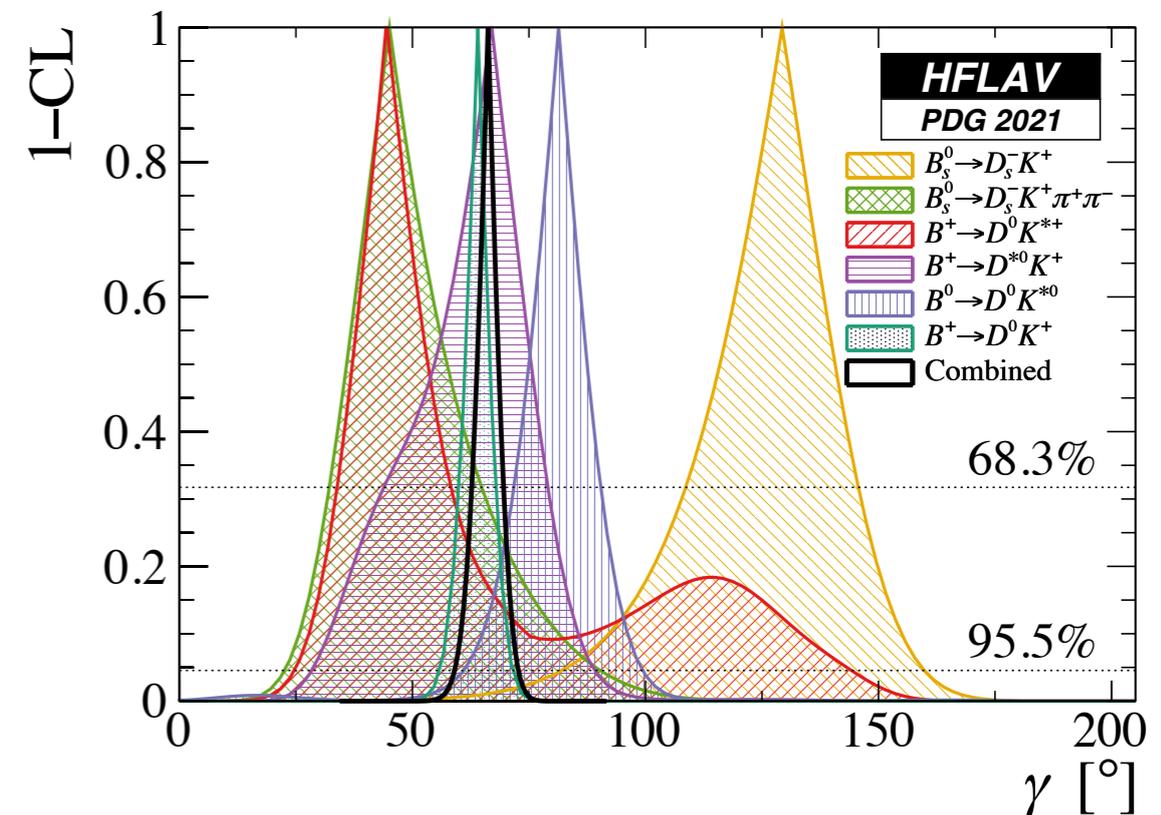
- Combining with $\mathcal{A}_{CP}(K^0 \pi^0)$ from time-dependent analysis [2305.07555] and with world-average lifetimes, Belle II obtains result competitive with world average

$$I_{K\pi} = -0.03 \pm 0.13 \pm 0.05$$

See J. Skorupa's,
J. Bennett's and
S. Raiz's talks

CKM angle γ

- The only CP -violation parameter that can be measured from tree-level decays (negligible theory uncertainty)
- Unconstrained CP violating effects in non-leptonic tree-level decays can modify the SM relation between γ and other CKM elements by several degrees
- Current $\sim 4^\circ$ precision dominated by LHCb, in particular by the measurement of $B^- \rightarrow DK^-$ with $D \rightarrow K_s^0 \pi^+ \pi^-$
- CLEO+BESIII coherent $D^0 \bar{D}^0$ data instrumental to constrain the strong-phase difference δ_D , which for $D \rightarrow K_s^0 \pi^+ \pi^-$ is measured in bins of the Dalitz plot: (c_i, s_i)

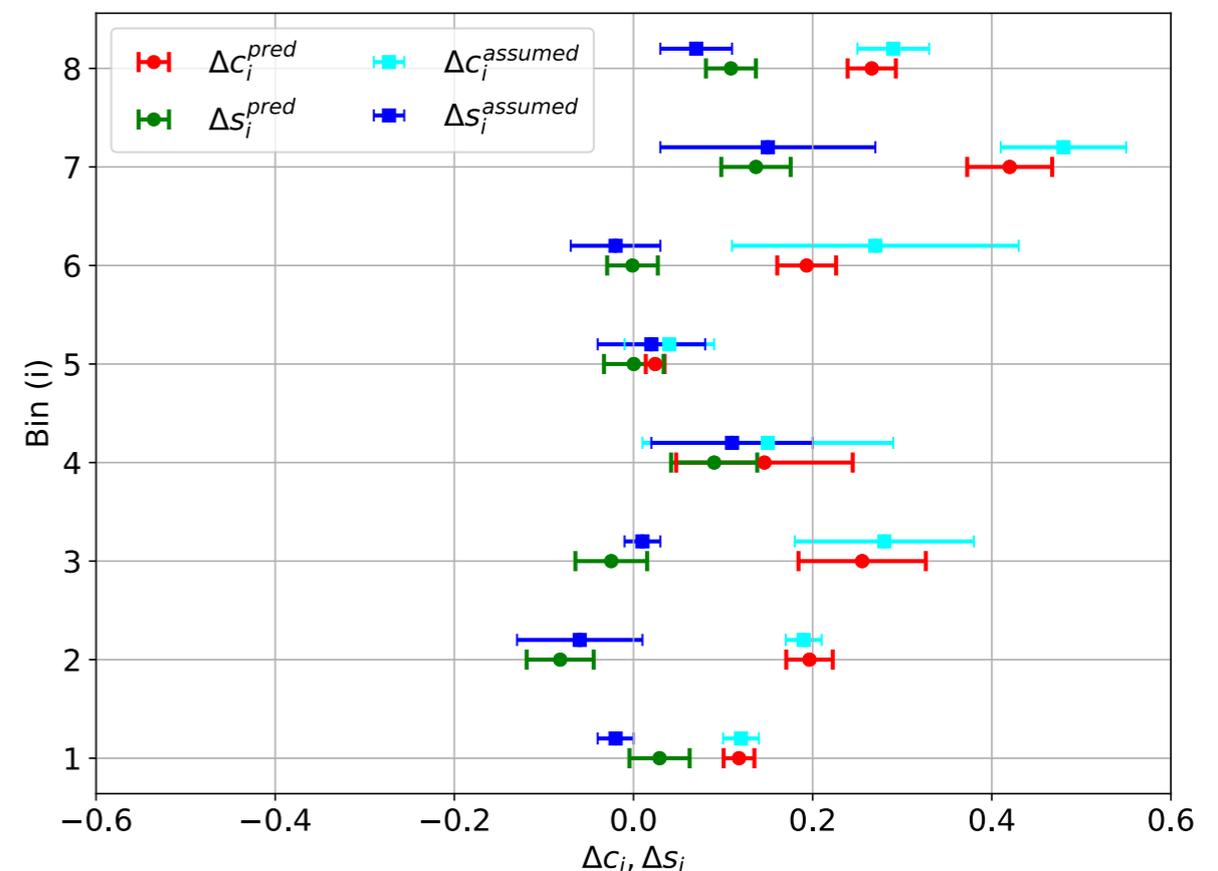
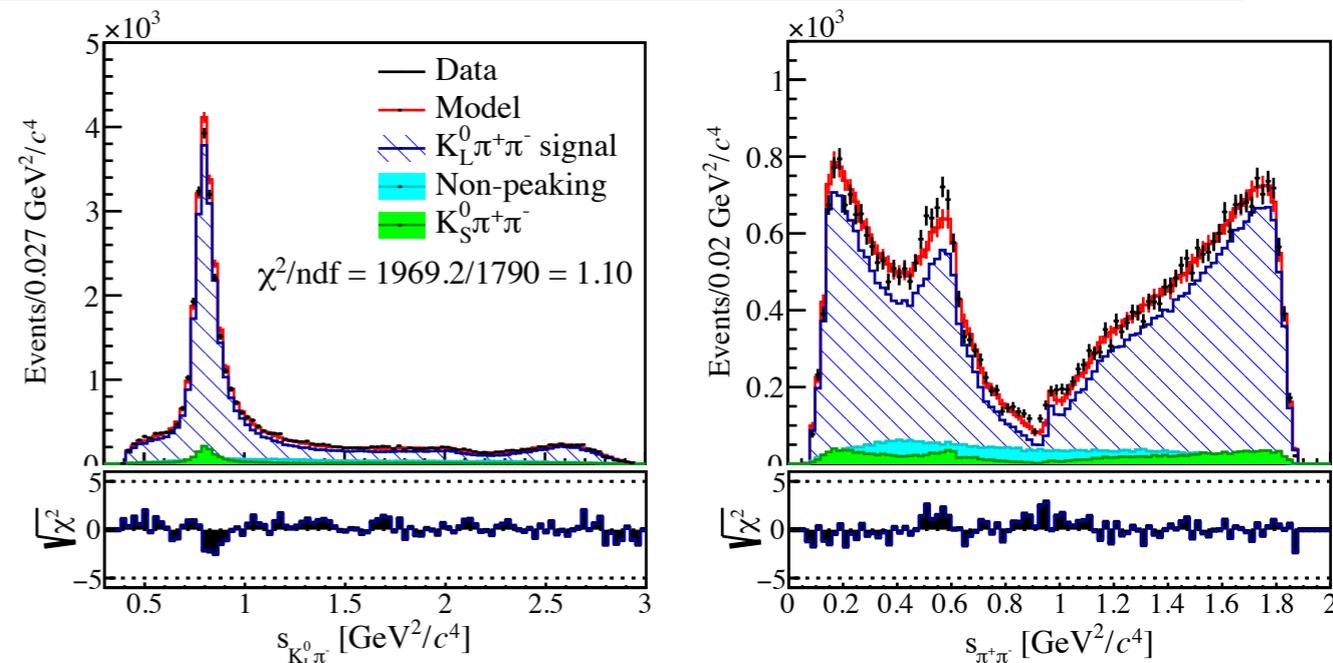


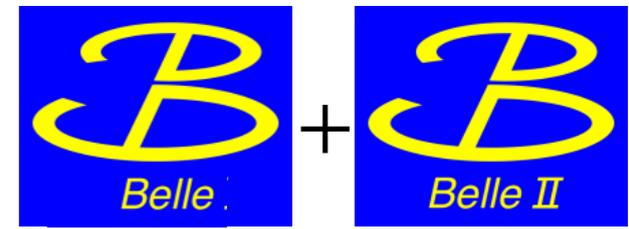
BESIII inputs to γ

- The inclusion of the $D^0 \rightarrow K_L^0 \pi^+ \pi^-$ mode in the determination of (c_i, s_i) provides a 3× more data at BESIII, but introduces uncertainty due to unknown U -spin-breaking parameters

$$\frac{A(D^0 \rightarrow K_L^0 (\pi^+ \pi^-)_{k_{CP}})}{A(D^0 \rightarrow K_S^0 (\pi^+ \pi^-)_{k_{CP}})} = 1 - 2\hat{\rho}_{k_{CP}} \tan^2 \theta_C$$

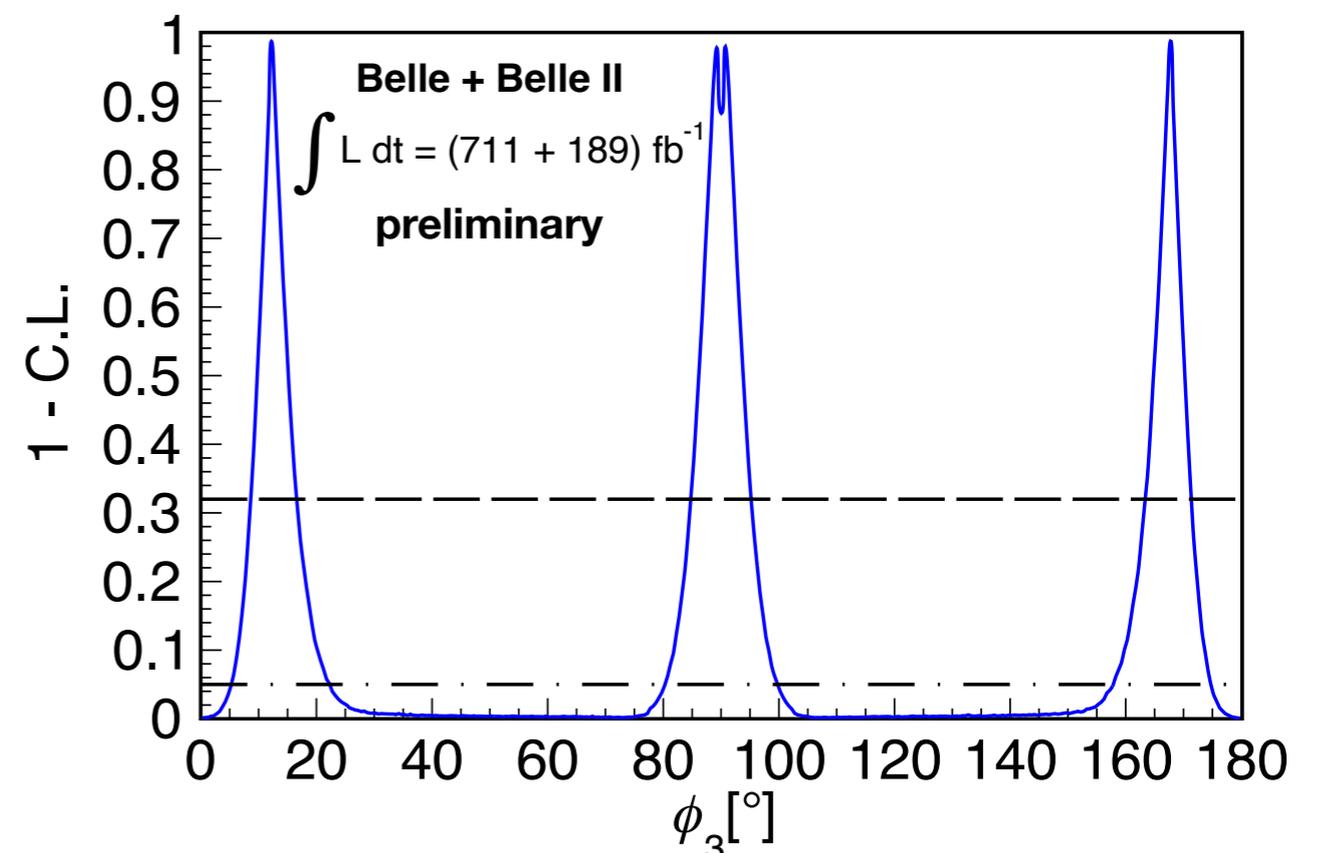
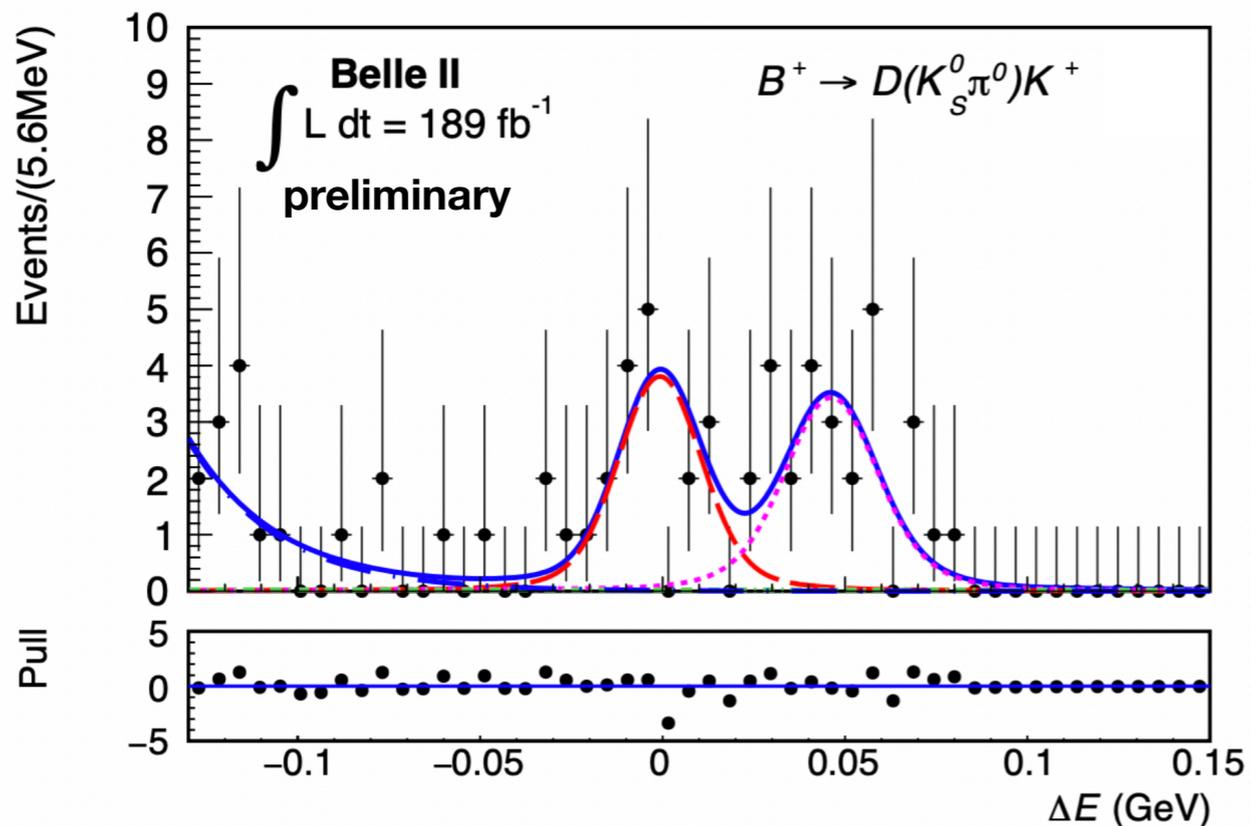
- Now measured with an amplitude analysis of $D^0 \rightarrow K_L^0 \pi^+ \pi^-$ (first ever with a K_L^0)
 - Large deviations from assumed values of unity (*i.e.*, large U -spin breaking) observed
- Model-predicted strong-phase parameter differences between $K_S^0 \pi^+ \pi^-$ and $K_L^0 \pi^+ \pi^-$ consistent with assumed values but more precise



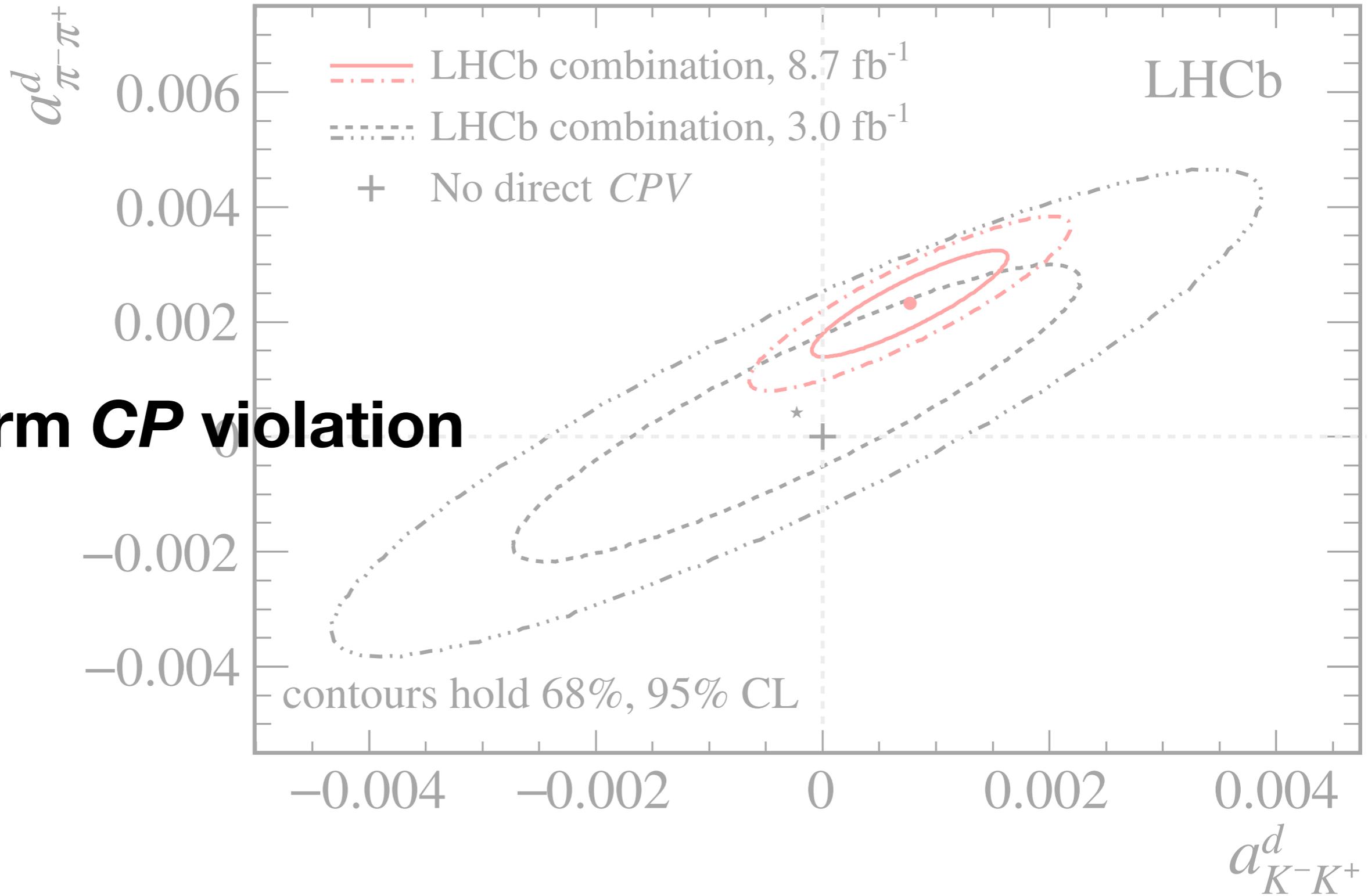


γ with CP -odd D final states

- B factories have unique access to CP -odd D final states, such as in $B^- \rightarrow D(\rightarrow K_S^0 \pi^0) K^-$ decays
- Combined with CP -even modes, such as $B^- \rightarrow D(\rightarrow K^+ K^-) K^-$, can measure γ without additional inputs

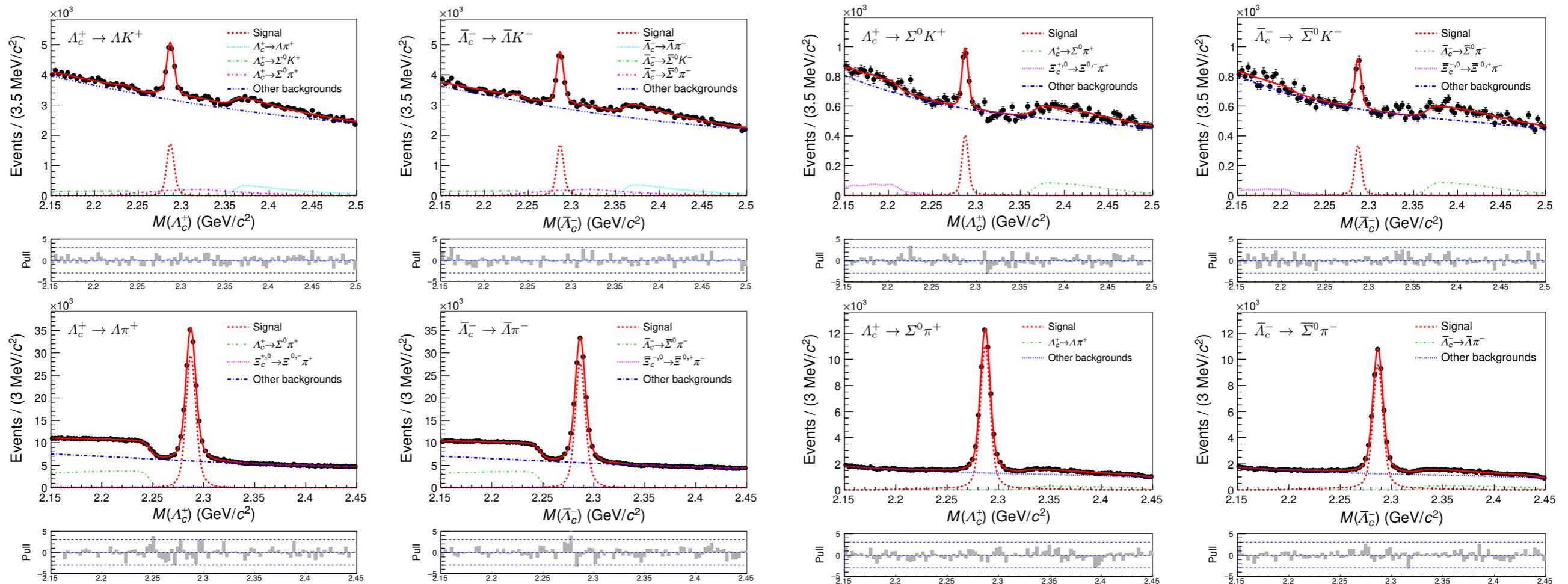


Charm CP violation



CP violation in charmed baryons

- Mostly unexplored, complements searches in charmed mesons and in beauty baryons
- At e^+e^- machines can get good signals for many modes, and Belle is (still) among the most active contributors



$$A_{CP}^{\text{dir}}(\Lambda_c^+ \rightarrow \Lambda K^+) = (+2.1 \pm 2.6 \pm 0.1)\%$$

$$A_{CP}^{\text{dir}}(\Lambda_c^+ \rightarrow \Sigma^0 K^+) = (+2.5 \pm 5.4 \pm 0.4)\%$$



CP violation in charmed baryons

- Angular distribution gives access to interference between parity-violating S -wave and the parity-conserving P -wave amplitudes in the decay

$$\frac{dN}{d \cos \theta_{\Lambda}} \propto 1 + \alpha_{\Lambda_c^+} \alpha_{-} \cos \theta_{\Lambda} \quad \alpha_{-} \propto \frac{\Re(S P^*)}{|S|^2 + |P|^2}$$

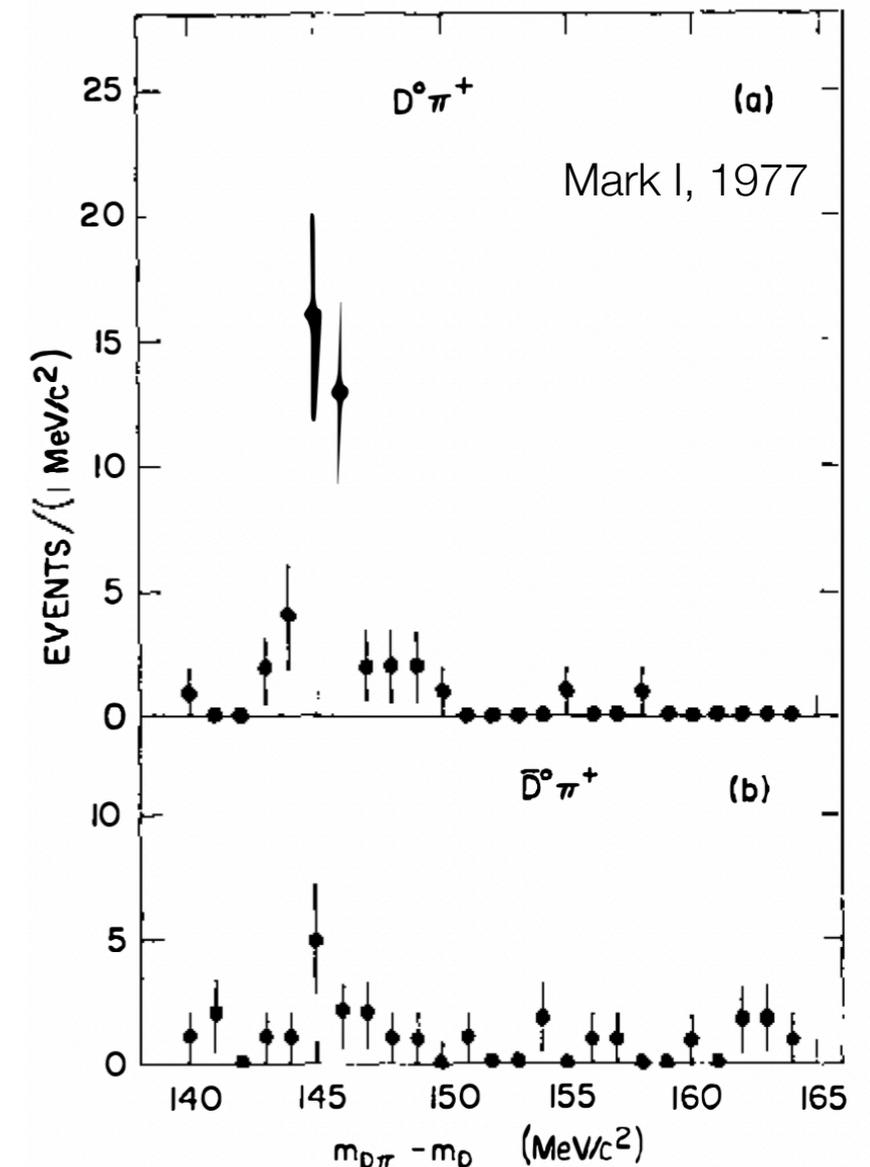
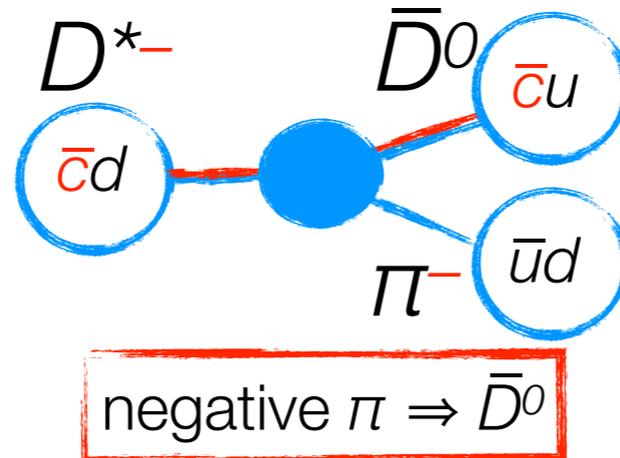
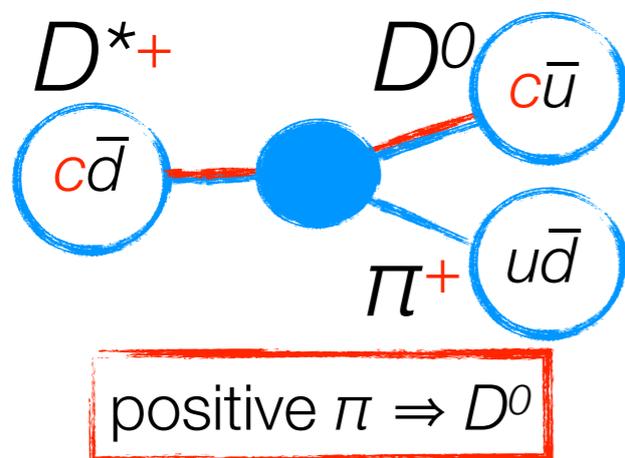
- This offers alternative paths to look for CP violation

$$A_{CP}^{\alpha} = \frac{\alpha_{-}(\Lambda_c^+) - \alpha_{-}(\bar{\Lambda}_c^-)}{\alpha_{-}(\Lambda_c^+) + \alpha_{-}(\bar{\Lambda}_c^-)}$$

Channel	A_{CP}^{α}	W.A. A_{CP}^{α}
$\Lambda_c^+ \rightarrow \Lambda K^+$	$-0.023 \pm 0.086 \pm 0.071$	—
$\Lambda_c^+ \rightarrow \Lambda \pi^+$	$+0.020 \pm 0.007 \pm 0.014$	-0.07 ± 0.22
$\Lambda_c^+ \rightarrow \Sigma^0 K^+$	$+0.08 \pm 0.35 \pm 0.14$	—
$\Lambda_c^+ \rightarrow \Sigma^0 \pi^+$	$-0.023 \pm 0.034 \pm 0.030$	—

Charm flavor tagging

- Tagging the production flavor is needed to measure CP violation (and mixing) in neutral D decays
- Since 1977 this is achieved by restricting to the strong-interaction decays



- Added bonus: sample is much cleaner
- Malus: sample is reduced by 5-20 \times

Conclusions

- Despite being often affected by hadronic uncertainties, non-leptonic hadron decays offer precise tests of the SM and discovery potential for new physics
- They also serve as valuable tools for measurements based on other channels
- Plenty of contributions from e^+e^- colliders in this area are (and will remain) crucial (thanks to the larger samples expected at Belle II and BESIII)

