



MAX-PLANCK-INSTITUT
FÜR PHYSIK

Hadronic B decays at Belle and Belle II

Markus Reif on behalf of the Belle and Belle II collaborations

Max Planck Institute for Physics, Munich

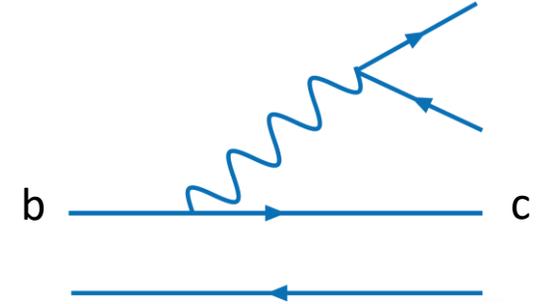
Lepton Photon 2021, Manchester
12 January 2022

Hadronic Charmed and Charmless B Decays



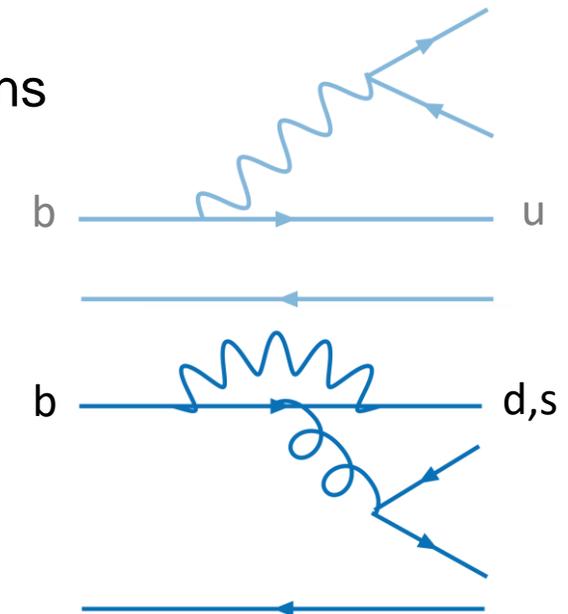
Charmed decays: $B \rightarrow D^{(*)}h$

- mediated through Cabibbo-favored $b \rightarrow c$ tree transitions
 - high branching fractions of $\sim 0.5\%$
 - clean channels to test QCD predictions
 - serve as important control modes
- $B \rightarrow D^{(*)}K$ modes are theoretically clean modes to precisely determine γ/Φ_3



Charmless decays: $B \rightarrow hh(h)$

- mediated through Cabibbo-suppressed $b \rightarrow u$ tree or $b \rightarrow d, s$ loop transitions
 - sensitive to **non-SM loop contributions**
 - contribute to determination of **all three CKM angles**
- Challenges:
 - small branching fractions $\sim O(10^{-5})$
 - high backgrounds: $e^+ e^- \rightarrow q\bar{q}$



Analysis Workflow

1. Reconstruction

- combine final state particles (e.g., pions and kaons) in kinematic fits to form the B decay of interest

2. Selection

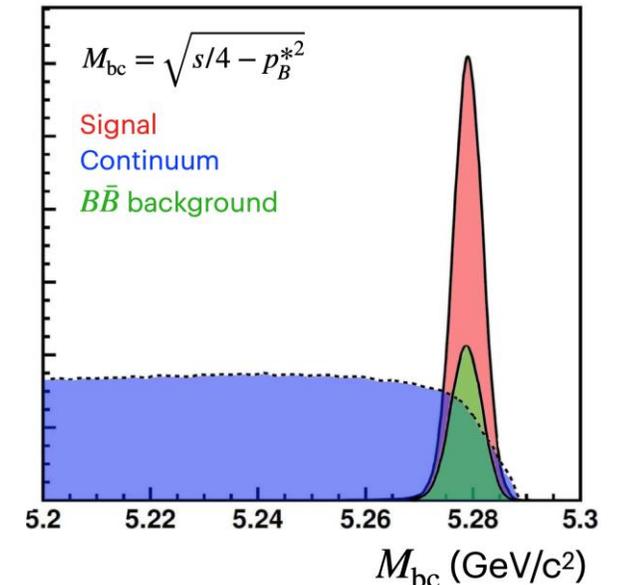
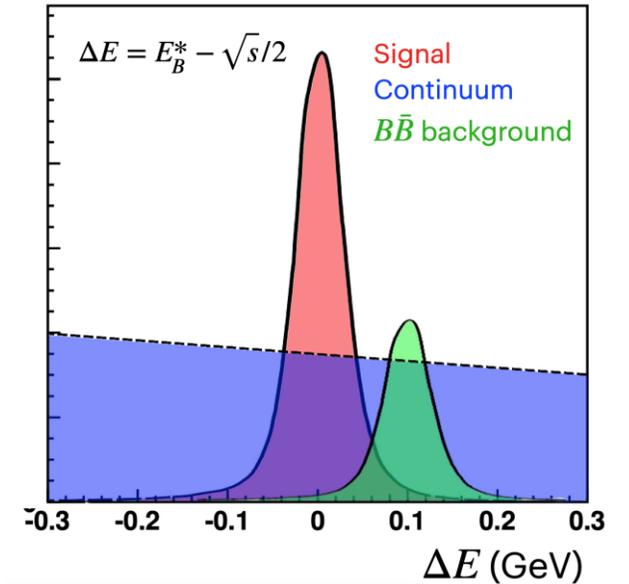
- optimized continuum suppression and particle ID criteria
- vetoes to remove peaking backgrounds (mainly in charmless)
- determine selection efficiencies for branching fraction calculations

3. Fit

- extract models in ΔE , M_{bc} (or more) from simulated data (+ calibrate on data)
- fit in to data and calculate physics quantities

4. Systematic Uncertainties

- evaluated with control modes and simplified simulations (toy studies)





Belle + Belle II

711fb⁻¹

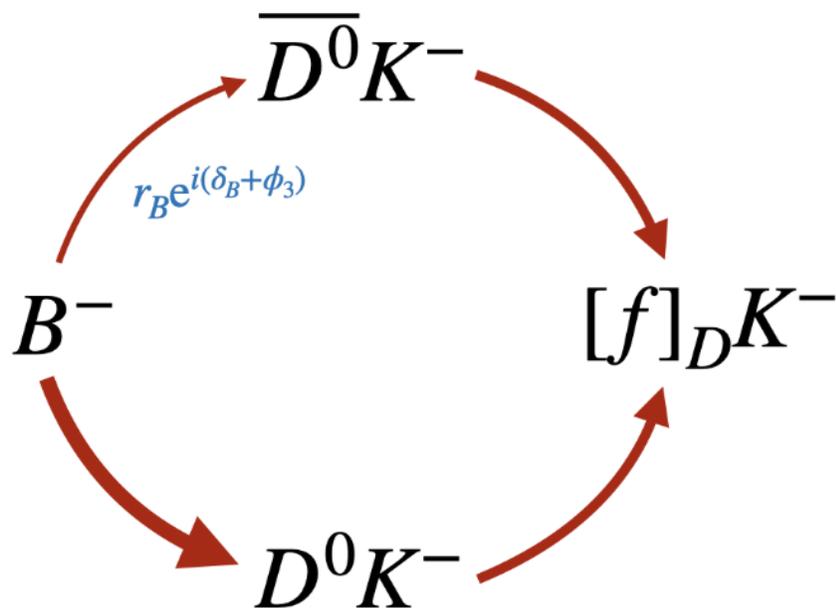
128fb⁻¹

Φ_3 from $B \rightarrow DK$ decays

Φ_3 from $B \rightarrow DK$ decays

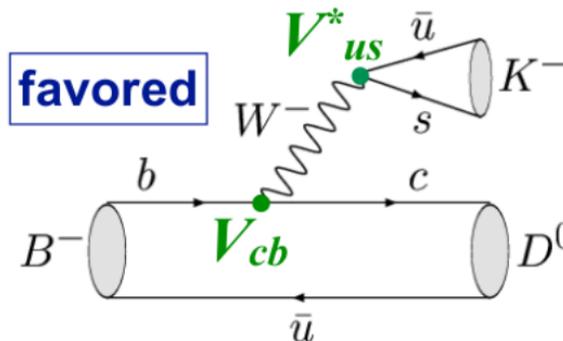
γ, Φ_3 is the phase between $b \rightarrow c$ and $b \rightarrow u$ transitions: $B \rightarrow DK$

- interference between two decays to same final state gives access to phase

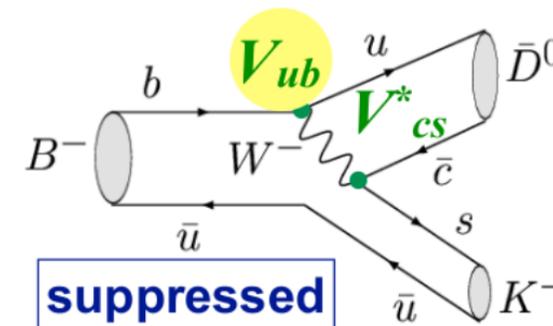


$$\frac{\mathcal{A}^{\text{suppr.}}(B^- \rightarrow \bar{D}^0 K^-)}{\mathcal{A}^{\text{favor.}}(B^- \rightarrow D^0 K^-)} = r_B e^{i(\delta_B + \phi_3)}$$

$B^- \rightarrow D^0 K^-$



$B^- \rightarrow \bar{D}^0 K^-$

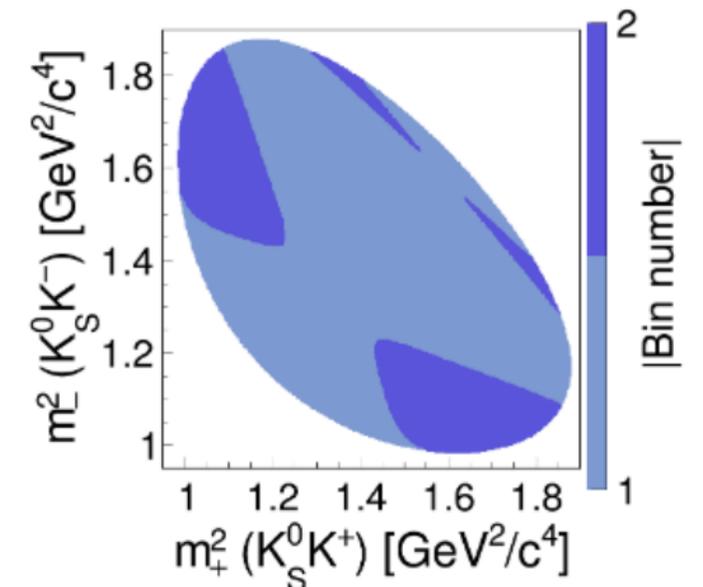
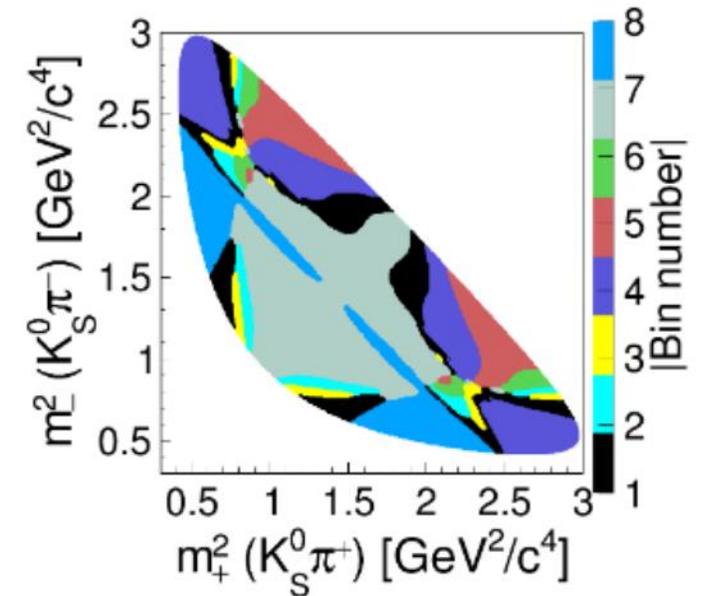


- D's reconstructed from: $K_S^0 \pi^+ \pi^-$ and $K_S^0 K^+ K^-$
- physics results limited by sample size, due to small branching fractions of involved decays

Φ_3 from $B \rightarrow DK$ decays

determination of Φ_3 is dependent on the physics of the D-decay

- could choose a model to describe the Dalitz plot
 - large systematic uncertainties
- **here:** use a binned model independent method
- independently measured D strong-phase parameters in each bin replace model (external input: CLEO & BESIII)
- observed yields per bin can be related to physics quantities of interest (Φ_3, δ_B, r_B)



Φ_3 from $B \rightarrow DK$ decays

<https://arxiv.org/pdf/2110.12125.pdf> (accepted by JHEP)

- 2D (ΔE , C') simultaneous fit of $B \rightarrow DK$ and $B \rightarrow D\pi$

- $K - \pi$ misidentification rate is directly extracted from data

$$\phi_3(^{\circ}) = 78.4 \pm 11.4 \text{ (stat.)} \pm 0.5 \text{ (syst.)} \pm 1.0 \text{ (ext. input)}$$

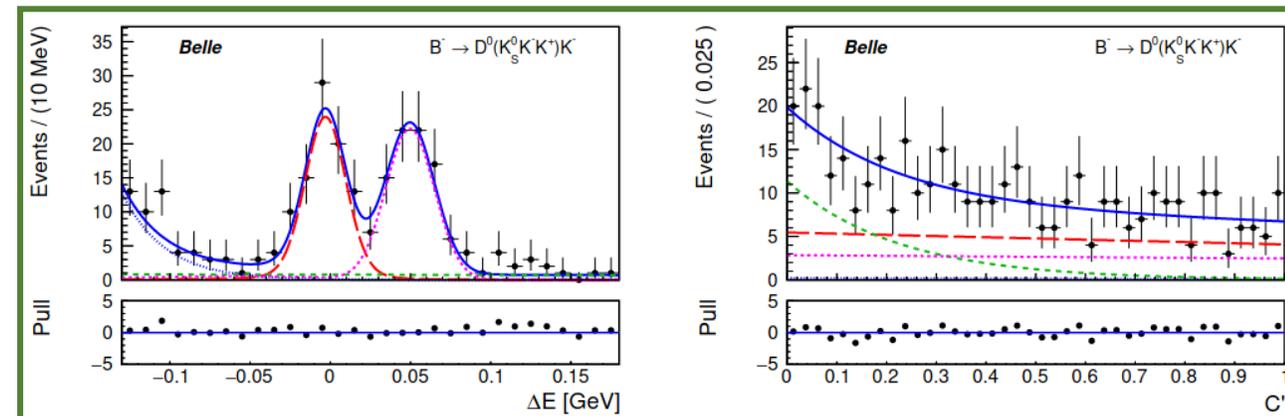
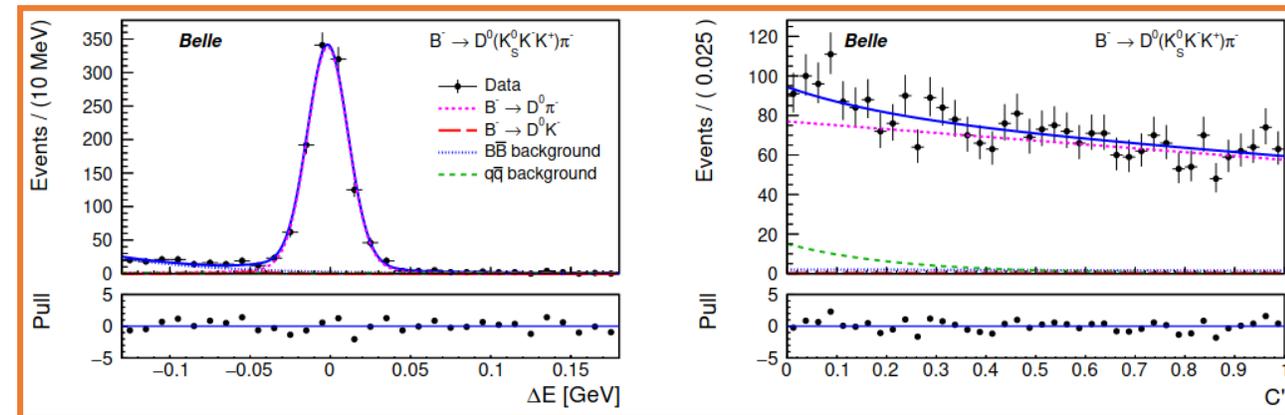
previous Belle result: PRD 85, 112014 (2012)

$$\phi_3(^{\circ}) = 77.3^{+15.1}_{-14.9} \pm 4.1 \pm 4.3$$

Improvements:

- multivariate K_S^0 selection
 - improved background rejection
 - new fitting strategy
 - new strong phase inputs (BESIII)
 - more data ($K_S^0 KK$ + Belle II)
- most precise B-factory result

pion-enhanced $\mathcal{L}(K/\pi) < 0.6$



kaon-enhanced $\mathcal{L}(K/\pi) > 0.6$

first combined Belle and Belle II analysis

Belle: $\bar{B}^0 \rightarrow D^+ h^-$
711fb⁻¹

$\bar{B}^0 \rightarrow D^+ h^-$

- theoretically clean modes to test factorization and SU(3) symmetry breaking in QCD

$$\mathcal{R}_{s/d}^{P(V)} \equiv \frac{\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^{(*)+} \pi^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{(*)+} K^-)}$$

➤ cancellation of most systematic effects

- tensions in branching ratio** between theory predictions and measurements, **R-ratios OK**
<https://arxiv.org/pdf/2007.10338.pdf> (Bordone et al.)

source	PDG [10 ⁻³]	QCDF prediction [10 ⁻³]	
χ^2/dof	—	—	
$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^+ \pi^-)$	3.00 ± 0.23	4.42 ± 0.21	→ 4σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$	0.186 ± 0.020	0.326 ± 0.015	→ 5σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)$	2.52 ± 0.13	—	
$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^{*+} \pi^-)$	2.0 ± 0.5	$4.3_{-0.8}^{+0.9}$	→ 2σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$	0.212 ± 0.015	$0.327_{-0.034}^{+0.039}$	→ 3σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$	2.74 ± 0.13	—	
$\mathcal{R}_{s/d}^P$	16.1 ± 2.1	$13.5_{-0.5}^{+0.6}$	OK
$\mathcal{R}_{s/d}^V$	9.4 ± 2.5	$13.1_{-2.0}^{+2.3}$	
$\mathcal{R}_s^{V/P}$	0.66 ± 0.16	$0.97_{-0.17}^{+0.20}$	
$\mathcal{R}_d^{V/P}$	1.14 ± 0.15	1.01 ± 0.11	

possible explanations:

- presence of large non-factorizable contributions of $\mathcal{O}(15 - 20\%)$ to amplitudes
- experimental issue
- systematic shift in input parameters
- new physics

$\bar{B}^0 \rightarrow D^+ h^-$

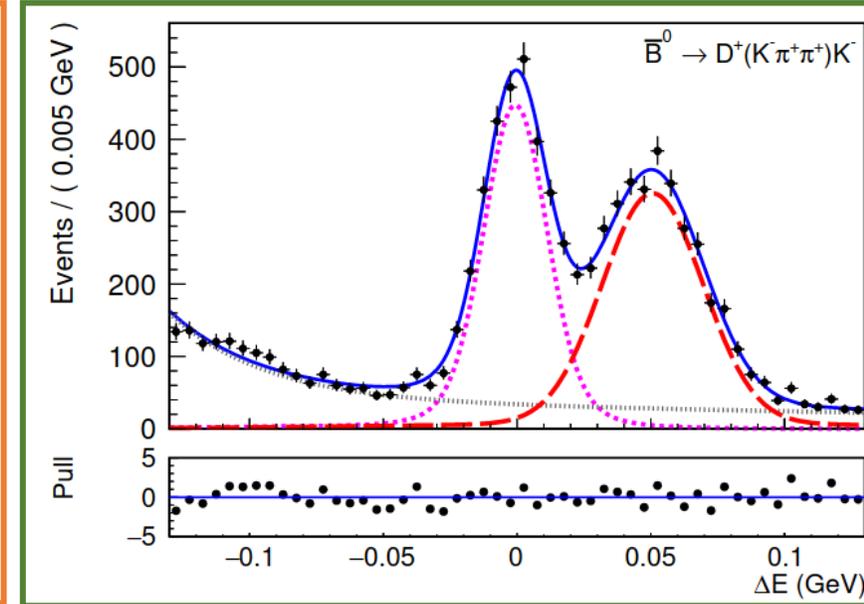
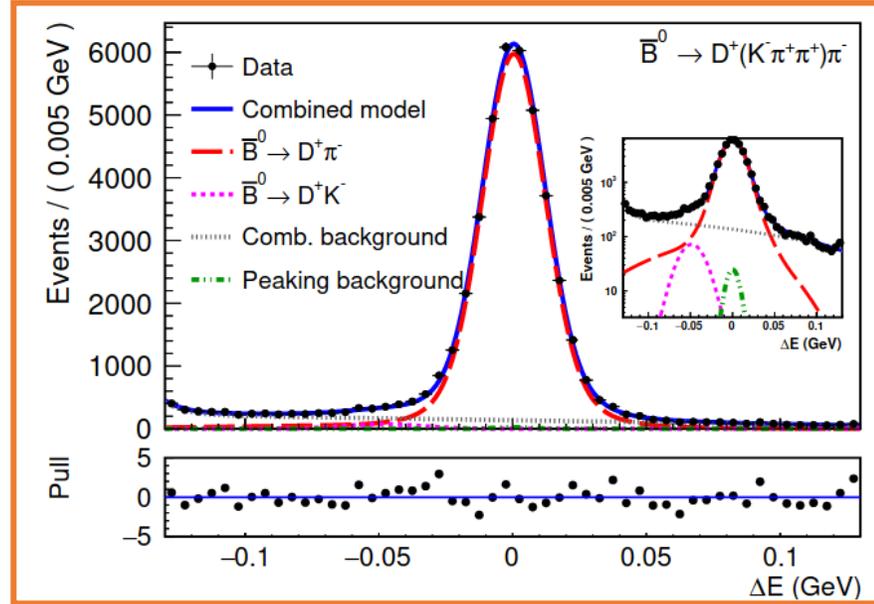
<https://arxiv.org/pdf/2111.04978.pdf> (accepted by PRD)

$$R^D \equiv \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)}$$

pion-enhanced $\mathcal{L}(K/\pi) < 0.6$

kaon-enhanced $\mathcal{L}(K/\pi) > 0.6$

- reconstruct $D^+ \rightarrow K^- \pi^+ \pi^+$
- ΔE simultaneous fit of $\bar{B}^0 \rightarrow D^+ K^-$ and $\bar{B}^0 \rightarrow D^+ \pi^-$



$$R^D = 0.0819 \pm 0.0020(\text{stat}) \pm 0.0023(\text{syst})$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-) = (2.03 \pm 0.05 \pm 0.07 \pm 0.03) \times 10^{-4}$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-) = (2.48 \pm 0.01 \pm 0.09 \pm 0.04) \times 10^{-3}$$

➤ compatible with world averages

6.6 σ from <https://arxiv.org/pdf/2007.10338.pdf> (Bordone et al.)

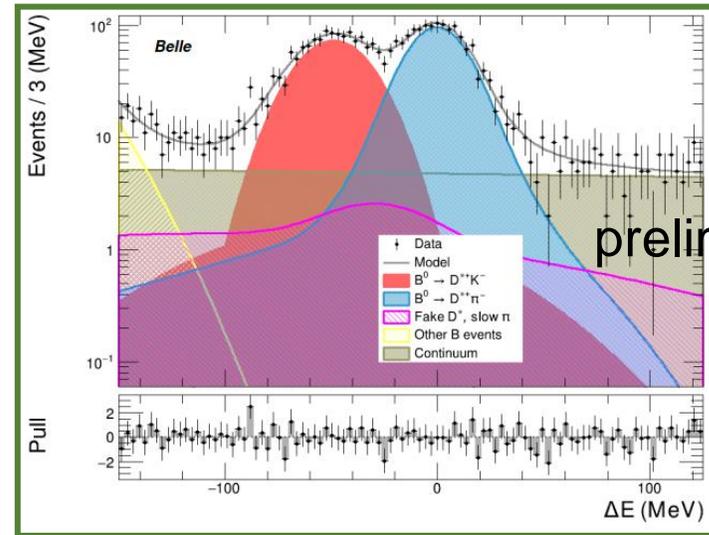
Belle: $\bar{B}^0 \rightarrow D^{*+} h^-$
711fb⁻¹

(preliminary)

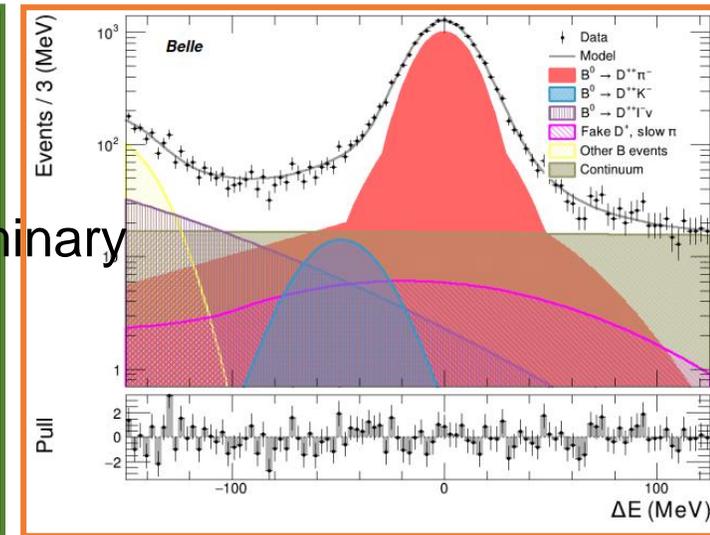
$\bar{B}^0 \rightarrow D^{*+} h^-$

- used signal channels:
 - $D^{*+} \rightarrow D^0 [K^- \pi^+] \pi^+$
 - $D^{*+} \rightarrow D^0 [K^- \pi^+ \pi^+ \pi^-] \pi^+$
- background from misreconstructed D^*
- ΔE simultaneous fit of $\bar{B}^0 \rightarrow D^{*+} K^-$ and $\bar{B}^0 \rightarrow D^{*+} \pi^-$

kaon-enhanced $\mathcal{L}(K/\pi) > 0.6$



pion-enhanced $\mathcal{L}(K/\pi) < 0.6$



preliminary

$D^0 \rightarrow K^- \pi^+$	Result	Discrepancy
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$	$(2.638 \pm 0.023 \pm 0.077) \times 10^{-3}$	1.7σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$	$(2.178 \pm 0.090 \pm 0.078) \times 10^{-4}$	$1.0\sigma(2.7\sigma)$
$D^0 \rightarrow K^- 2\pi^+ \pi^-$		
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$	$(2.499 \pm 0.021 \pm 0.095) \times 10^{-3}$	2.0σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$	$(2.134 \pm 0.082 \pm 0.086) \times 10^{-4}$	$1.1\sigma(2.8\sigma)$
Combined		
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$	$(2.569 \pm 0.015 \pm 0.083) \times 10^{-3}$	1.9σ
$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$	$(2.156 \pm 0.061 \pm 0.074) \times 10^{-4}$	$1.1\sigma(2.8\sigma)$

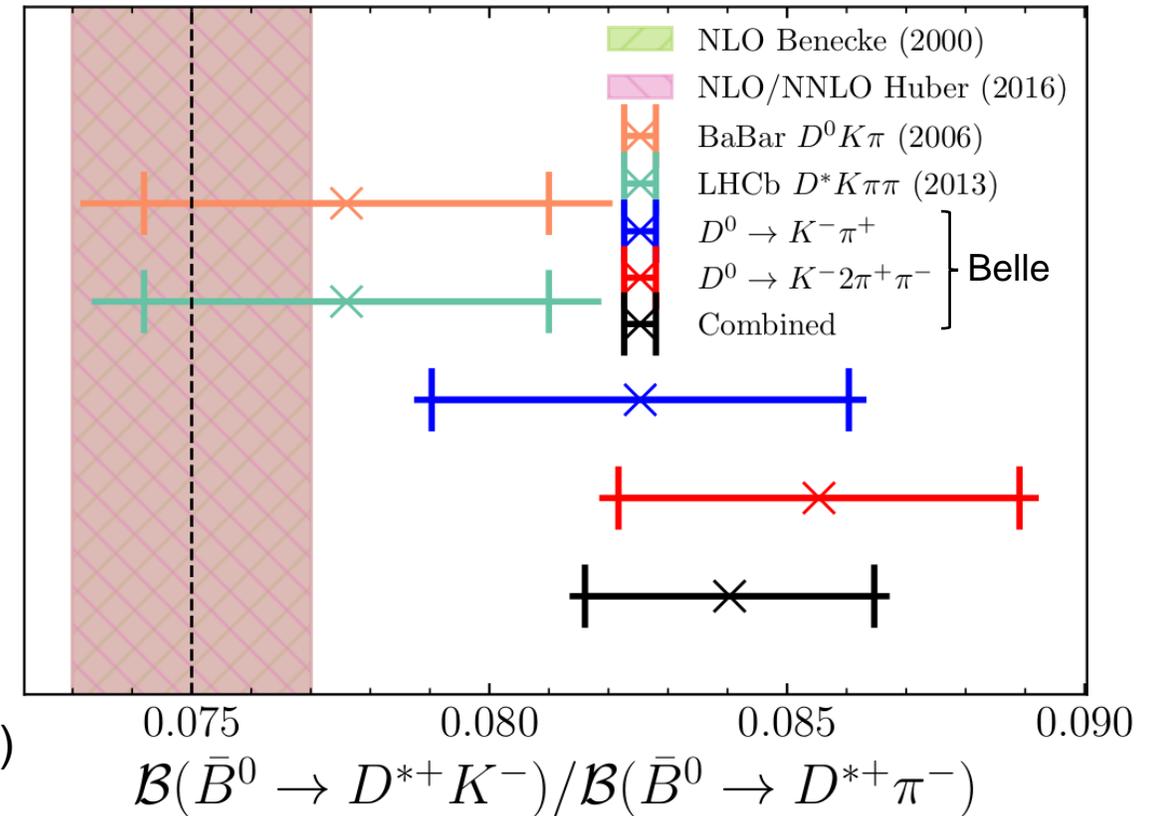
- slight deviations from theory predictions
 - w/o brackets: <https://arxiv.org/pdf/1606.02888.pdf> (Huber et al.)
 - w/ bracket: <https://arxiv.org/pdf/2007.10338.pdf> (Bordone et al.)
- results compatible with earlier Belle measurement
 - uncertainty improved by a factor of 3.5
 - <https://arxiv.org/pdf/hep-ex/0104051.pdf>

$$\mathcal{R}_{K/\pi} = \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)}$$

Channel	Result	Discrepancy
$D^0 \rightarrow K^- \pi^+$	$\mathcal{R}_{K/\pi} = (8.254 \pm 0.350 \pm 0.147) \times 10^{-2}$	1.7σ
$D^0 \rightarrow K^- 2\pi^+ \pi^-$	$\mathcal{R}_{K/\pi} = (8.527 \pm 0.336 \pm 0.150) \times 10^{-2}$	2.5σ
Combined	$\mathcal{R}_{K/\pi} = (8.390 \pm 0.243 \pm 0.115) \times 10^{-2}$	2.7σ

total experimental uncertainty reduced to **3.2%**

- LHCb: 5.5% ($\mathcal{R}_{\text{LHCb}} = \mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^- \pi^- \pi^+) / \mathcal{B}(\bar{B}^0 \rightarrow D^{*+} 2\pi^- \pi^+)$)
<https://journals.aps.org/prd/pdf/10.1103/PhysRevD.87.092001>
- BaBar: 5.7% (no simultaneous fit of kaon and pion sample)
<https://arxiv.org/pdf/hep-ex/0509036.pdf>



Belle II: $B^0 \rightarrow K^0 \pi^0$
62.8fb⁻¹

$$I_{K\pi} = \mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} - 2\mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

- **limiting channel in isospin sum rule**

- stringent null test of SM

- **first branching fraction and A_{CP} measurement shown at Moriond 2021**

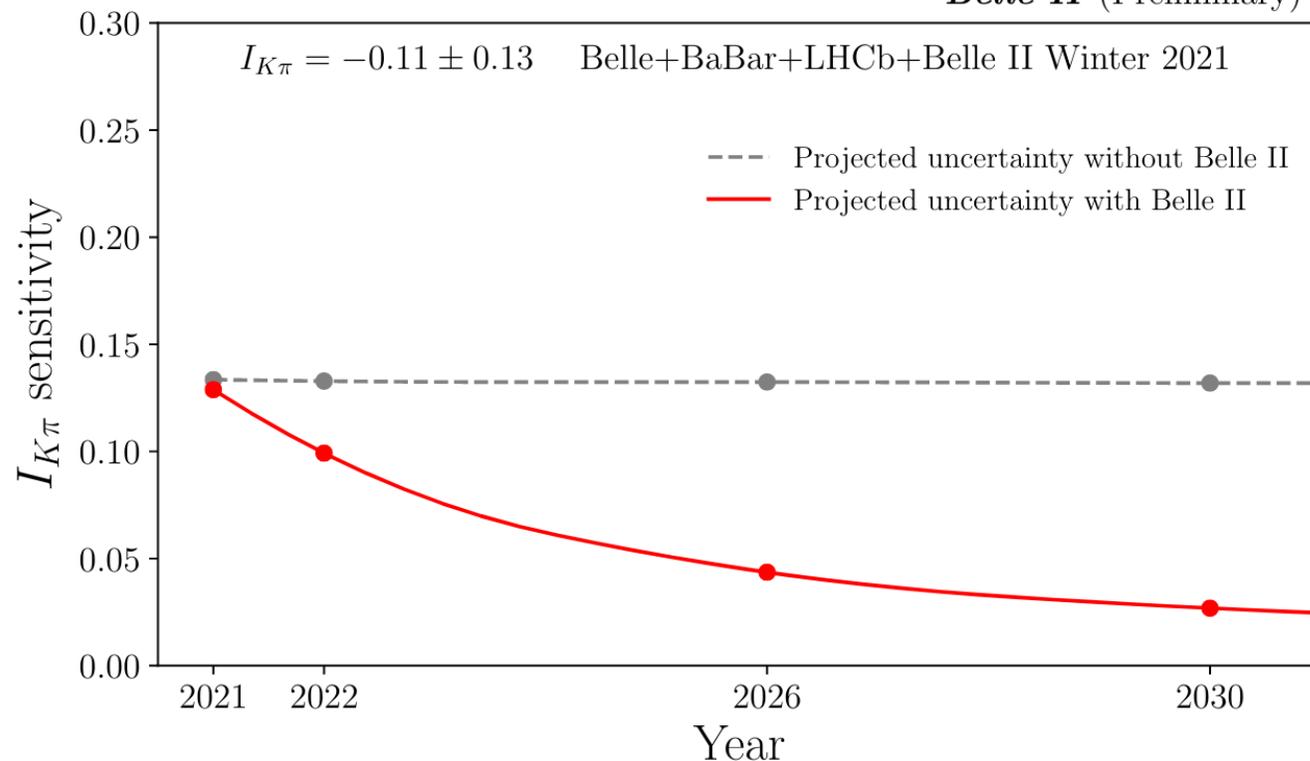
<https://arxiv.org/pdf/2104.14871.pdf>

$$\mathcal{A}_{K^0\pi^0} = -0.40_{-0.44}^{+0.46}(\text{stat}) \pm 0.04(\text{syst})$$

$$\mathcal{B}(B^0 \rightarrow K^0 \pi^0) = [8.5_{-1.6}^{+1.7}(\text{stat}) \pm 1.2(\text{syst})] \times 10^{-6}$$

- update on branching fraction and A_{CP}
plus time dependent CP violation

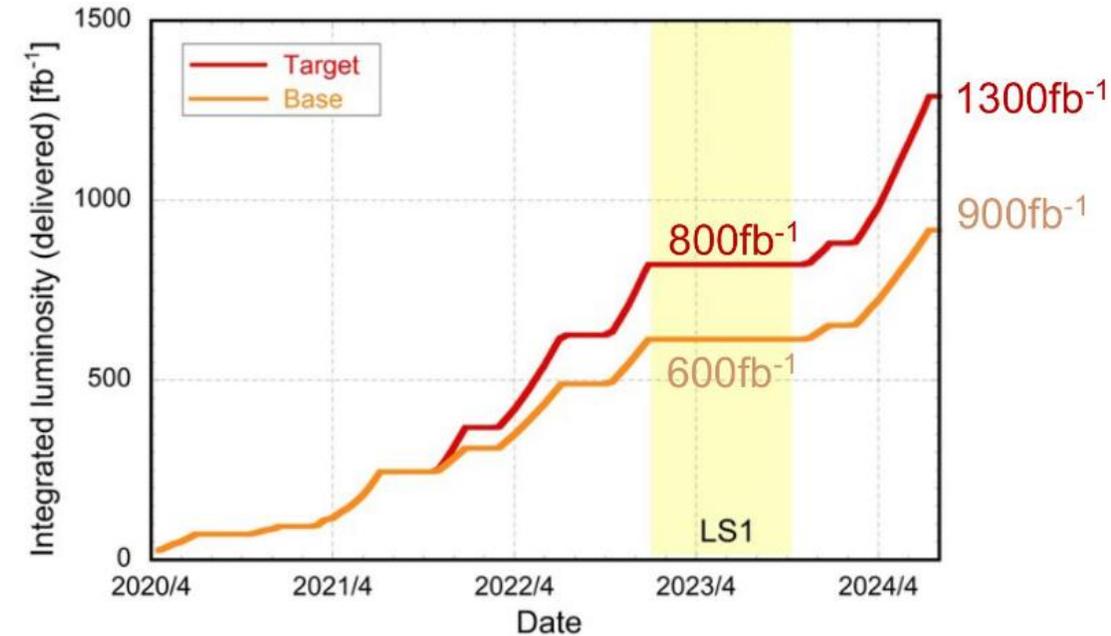
Belle II (Preliminary)



Summary

- Belle still in the game, producing world leading physics results
- Belle II has picked up pace
 - world leading results in charmless sector (i.e., $B^0 \rightarrow \pi^0 \pi^0$ and $B^0 \rightarrow K^0 \pi^0$) in ~ 1 year
 - improvements on Φ_3 longer scale
- possibility to combine Belle and Belle II datasets

Belle II luminosity projection



**new/updated results to come in the near future
→ stay tuned**

Backup

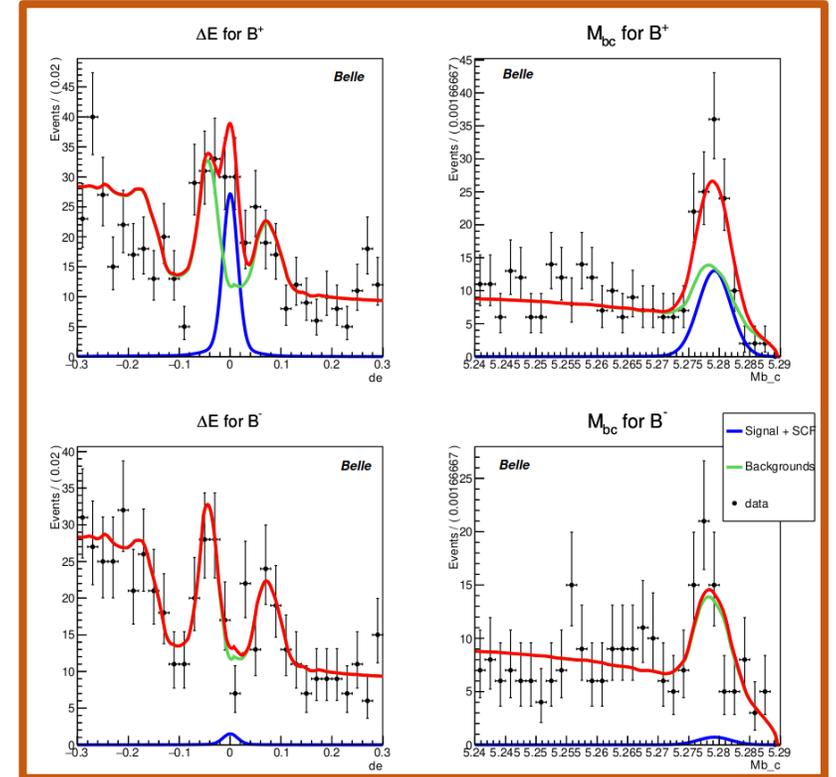
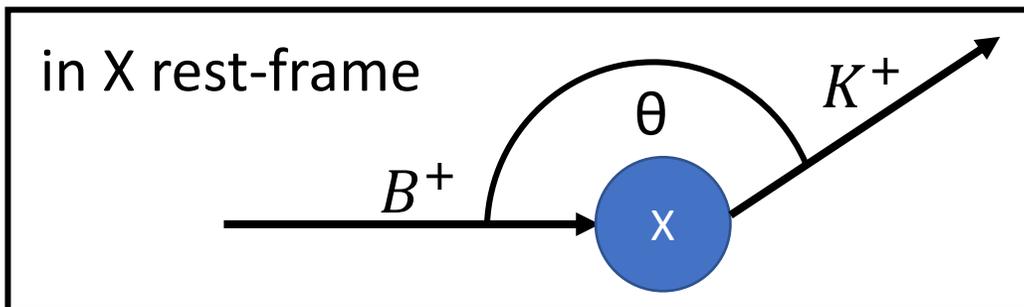
Belle: $B^+ \rightarrow K^+ K^- \pi^+$
711fb⁻¹

$B^+ \rightarrow K^+ K^- \pi^+$

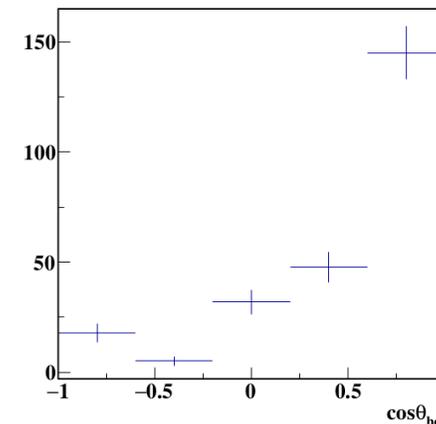
- BaBar and LHCb reported on an excess at low M_{KK}
- split the sample into five M_{KK} bins

M_{KK}	N_{sig}	$\mathcal{S}(\sigma)$	\mathcal{A}_{CP}	$\mathcal{S}(\sigma)$	$d\mathcal{B}/dM (\times 10^{-7})$
0.8-1.1	$59.81 \pm 11.38 \pm 2.58$	6.71	$-0.896 \pm 0.166 \pm 0.039$	4.80	$14.0 \pm 2.7 \pm 0.8$
1.1-1.5	$212.35 \pm 21.31 \pm 6.71$	12.49	$-0.157 \pm 0.098 \pm 0.007$	1.58	$37.8 \pm 3.8 \pm 1.9$
1.5-2.5	$113.45 \pm 26.74 \pm 18.59$	3.67	$-0.135 \pm 0.231 \pm 0.030$	0.57	$10.0 \pm 2.3 \pm 1.7$
2.5-3.5	$110.11 \pm 17.56 \pm 4.94$	7.37	$-0.092 \pm 0.158 \pm 0.009$	0.58	$10.0 \pm 1.6 \pm 0.6$
3.5-5.3	$172.64 \pm 25.68 \pm 7.39$	7.43	$-0.053 \pm 0.147 \pm 0.006$	0.36	$8.1 \pm 1.2 \pm 0.5$

- large \mathcal{A}_{CP} of -0.896 with stat. significance of 4.8σ in first bin
- helicity angle gives insight in nature of 'state'



<https://minerva-access.unimelb.edu.au/handle/11343/197534>



looks like spin 1



tracks

$|dr| < 0.2 \text{ cm}$ and $|dz| < 5 \text{ cm}$

binary kaonID > 0.6

or binary pionID < 0.4

veto D^0

$1.85 < M_{KK}, M_{K\pi}, M_{K^+\pi^-}, M_{\pi^+K^-} < 1.85 \text{ (GeV/c}^2\text{)}$

veto J/ψ

$3.06 < M_{ee}, M_{\mu\mu} < 3.14 \text{ (GeV/c}^2\text{)}$

veto χ_{c0}

$3.375 < M_{KK} < 3.475 \text{ (GeV/c}^2\text{)}$

B^-

continuum suppression MVA > 0.88

$-0.3 < \Delta E < 0.3 \text{ GeV}$

$5.24 < M_{bc} < 5.29 \text{ GeV/c}^2$

best candidate selection

average multiplicity: 1.344

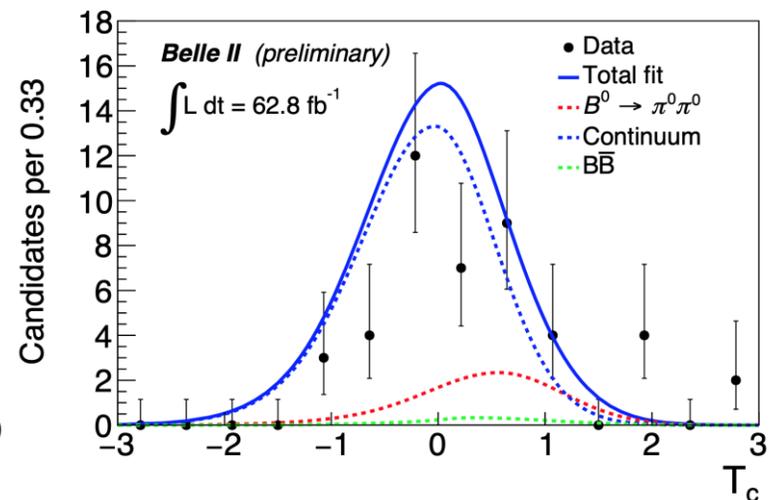
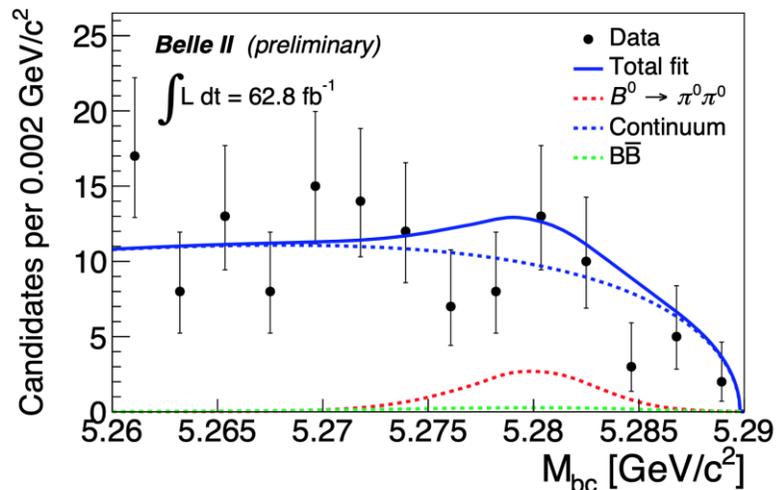
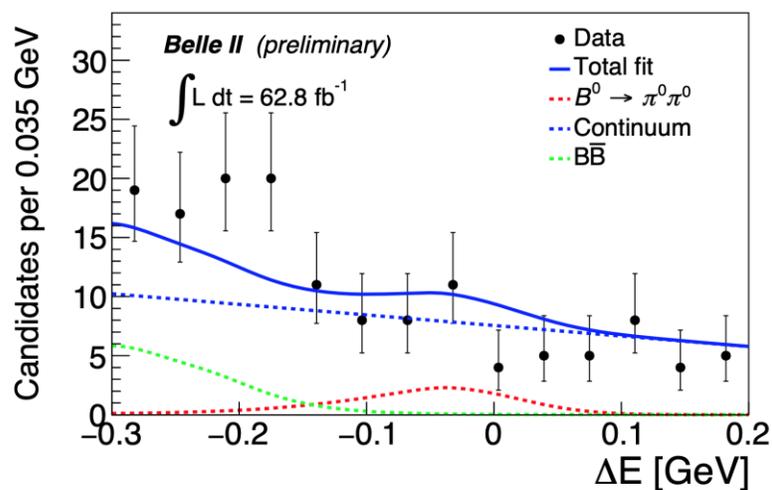
select candidate with smallest χ^2 of B-vertex fit

→ BCS selects the correct candidate in 92% of the cases

Belle II: $B^0 \rightarrow \pi^0 \pi^0$
62.8fb⁻¹

$B^0 \rightarrow \pi^0 \pi^0$

- unique Belle II capability to study **all** $B \rightarrow \pi\pi$ channels in consistent manner to extract α/Φ_2
- very **challenging**: two π^0
- first **branching fraction** measurement shown at Moriond 2021 <https://arxiv.org/pdf/2107.02373.pdf>
 - **3D-fit** in ΔE , M_{bc} and transformed continuum suppression variable T_c



$$\mathcal{B}(B^0 \rightarrow \pi^0 \pi^0) = [1.09_{-0.41}^{+0.50} \text{ (stat)} \pm 0.27 \text{ (sys)}] \times 10^{-6}$$

➤ update on branching fraction **plus direct CP violation**



Φ_3 from $B \rightarrow DK$ decays

tracks

$|dr| < 0.2$ cm and $|dz| < 1$ cm

fast kaon (pion) binary ID > 0.6 (< 0.6)

fast kaon or pion: $\cos\theta > -0.6$ (Belle II)

slow kaons or pions: binary ID

K_S^0

$0.487 < \text{InvM} < 0.508$ GeV/c²

BDT: 'good' K_S^0

fast kaon or pion: $\cos\theta > -0.6$ (Belle II)

slow kaons or pions: binary ID

D^0

$1.85 < \text{InvM} < 1.88$ GeV/c²

mass constrained fit

veto $e^+e^- \rightarrow cc$

$D^{*+} \rightarrow D^0\pi^+$: $0.143 < \text{InvM}(D^*) - \text{InvM}(D^0) < 0.149$ GeV/c²

B^+

$-0.13 < \Delta E < 0.18$ GeV

$M_{bc} > 5.27$ GeV/c²

continuum suppression

Belle: $C > 0.15$

Belle II: $C > 0.2$

best candidate selection

average multiplicity: 1.02

select candidate with smallest χ^2 of B-vertex fit

→ BCS selects the correct candidate in 65% of the cases



Φ_3 from $B \rightarrow DK$ decays

stolen from Niharika Rout's CKM Workshop talk

$$N_i^\pm = h_{B^\pm} \left[F_i + r_B^2 \bar{F}_i + 2\sqrt{F_i \bar{F}_i} (c_i x_\pm + s_i y_\pm) \right].$$

h_{B^\pm} : Normalization constant.

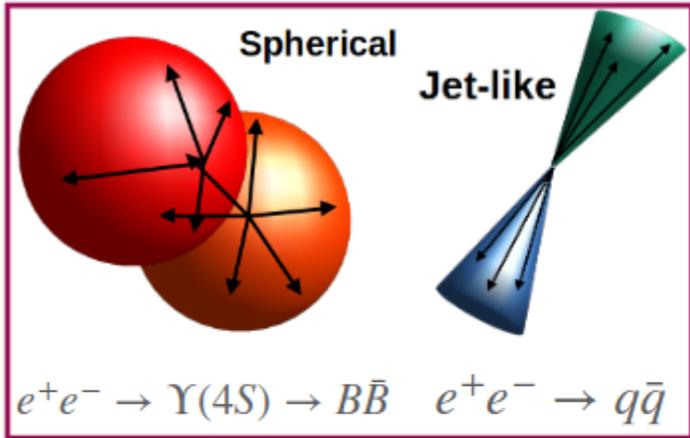
Physics parameters of interest: $(x_\pm, y_\pm) = r_B (\cos(\phi_3 + \delta_B), \sin(\phi_3 + \delta_B))$

Amplitude-averaged strong phase difference between \bar{D}^0 and D^0 over i^{th} bin and are obtained from external charm factories like *CLEO* and *BESIII*.

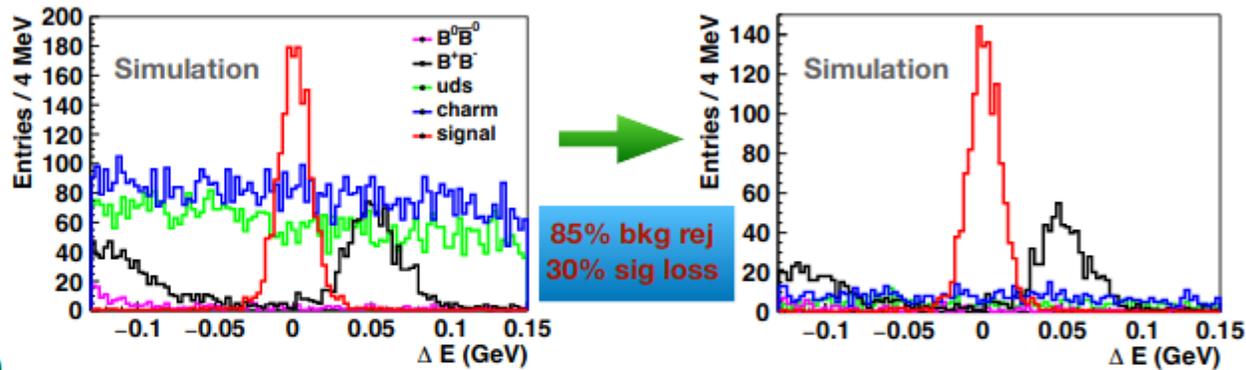
Fraction of pure D^0 decay to bin i taking into account the reconstruction and selection efficiency.

stolen from Niharika Rout's CKM Workshop talk

Background suppression



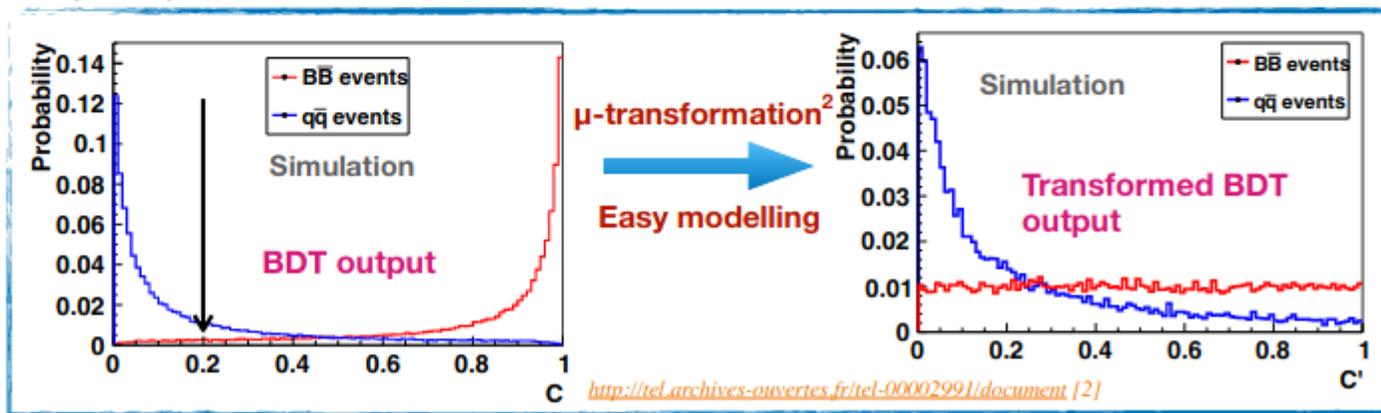
Dominant background from $e^+e^- \rightarrow q\bar{q}$ processes



Inputs to boosted-decision-tree (BDT)



- Event shape variables
- Angular variables
- Vertex variables
- Flavour tag variables



[http://tel.archives-ouvertes.fr/tel-00002991/document \[2\]](http://tel.archives-ouvertes.fr/tel-00002991/document)

Φ_3 from $B \rightarrow DK$ decays

Source	$\sigma_{x_+^{DK}}$	$\sigma_{y_+^{DK}}$	$\sigma_{x_-^{DK}}$	$\sigma_{y_-^{DK}}$	$\sigma_{x_\xi^{D\pi}}$	$\sigma_{y_\xi^{D\pi}}$
Input c_i, s_i	0.22	0.55	0.23	0.67	0.73	0.82
PDF parametrisation	0.07	0.08	0.12	0.16	0.12	0.12
PID	< 0.01	< 0.01	< 0.01	0.01	< 0.01	< 0.01
Peaking background	0.03	0.05	0.03	0.04	0.02	0.10
Fit bias	0.16	0.06	0.12	0.16	0.49	0.10
Bin migration	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.03
Total	0.18	0.11	0.17	0.23	0.51	0.19
Statistical	3.15	4.20	3.27	4.20	4.75	5.44

Table 3. Systematic uncertainty summary. All values are quoted in units of 10^{-2} .

$$\bar{B}^0 \rightarrow D^+ h^-$$

tracks

$|dr| < 0.2 \text{ cm}$ and $|dz| < 1.5 \text{ cm}$

binary kaonID > 0.6

or binary pionID < 0.6

D^+

mass within $\pm 2.5\sigma$ of nominal D^+ mass

mass constrained fit

\bar{B}^0

continuum suppression MVA > 0.88

$-0.13 < \Delta E < 0.13 \text{ GeV}$

$5.27 < M_{bc} < 5.29 \text{ GeV}/c^2$

veto $B^0 \rightarrow K^{*0}[K^+\pi^-]J/\psi[l^+l^-]$

$M_{\pi\pi}$ within $\pm 3\sigma$ of nominal J/ψ mass

best candidate selection

average multiplicity: 1.007

select candidate with smallest $|M_{bc} - m_{\bar{B}^0}|$

→ BCS selects the correct candidate in 92% of the cases

$$\bar{B}^0 \rightarrow D^+ h^-$$

Source	R^D	$\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)$	$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$
$\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)$	–	1.71%	1.71%
Tracking	–	1.40%	1.40%
$N_{B\bar{B}}$	–	1.37%	1.37%
f^{00}/f^{+-}	–	1.92%	1.92%
$D^+ \rightarrow K^- \pi^+ \pi^+$ model	–	0.69%	0.69%
PDF parameterization	2.71%	1.63%	1.79%
PID efficiency of K/π	0.88%	0.68%	0.73%
D^+ mass selection window	0.05%	0.56%	0.64%
J/ψ veto selection	0.12%	0.004%	0.15%
Peaking background yield	0.07%	0.04%	0.00%
MC statistics	< 0.01	0.04%	0.04%
Fit bias	–	0.58%	0.61%
Total	2.85%	3.43%	3.54%

$\bar{B}^0 \rightarrow D^{*+} h^-$ decays

Particle candidate	Requirement
all tracks	$ dz < 2 \text{ cm}, dr < 4 \text{ cm}$
fast π^-	$\mathcal{L}_{K/\pi} < 0.6$
slow π^-	no requirements
K^-	$\mathcal{L}_{K/\pi} > 0.6$
D^0	$M - 3\sigma_M < M < M + 3\sigma_M$
D^{*+}	$\Delta M - 3\sigma_{\Delta M} < \Delta M < \Delta M + 3\sigma_{\Delta M}$
B^0	$M_{bc} > 5.27 \text{ GeV}$
B^0	$-150 \text{ MeV} < \Delta E < 125 \text{ MeV}$

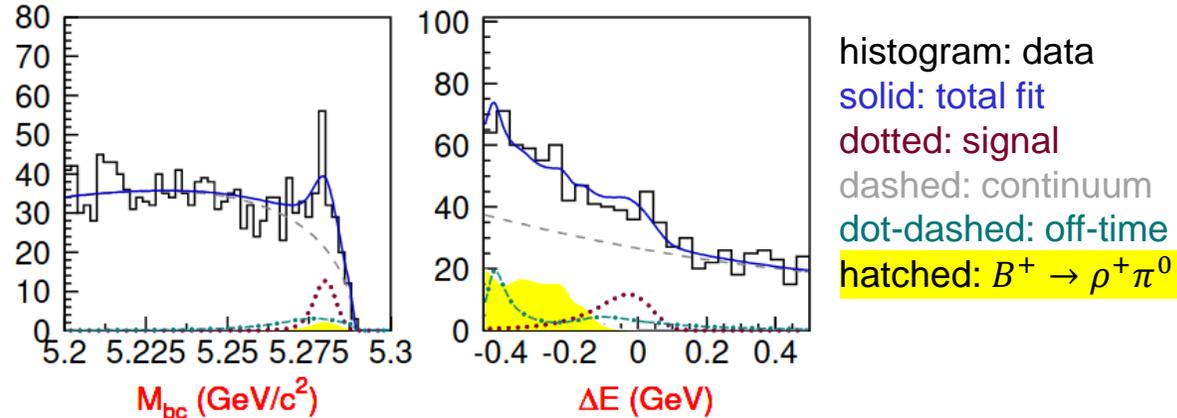
$\bar{B}^0 \rightarrow D^{*+} h^-$ decays

$D^0 \rightarrow K^- \pi^+$			$D^0 \rightarrow K^- 2\pi^+ \pi^-$			Combined			
type	$\bar{B} \rightarrow D^{*+} \pi^-$	$\bar{B} \rightarrow D^{*+} K^-$	type	$\bar{B} \rightarrow D^{*+} \pi^-$	$\bar{B} \rightarrow D^{*+} K^-$	Type	$\bar{B} \rightarrow D^{*+} \pi^-$	$\bar{B} \rightarrow D^{*+} K^-$	Corr. coeff.
π -ID stat.	0.78%(0.72% [†])	0.54%	π -ID stat.	0.95%(0.65% [†])	0.20%	π -ID stat.	0.77%(0.58% [†])	0.34%	3/5
π -ID sys.	0.60%(0.44% [†])	0.27%	π -ID sys.	0.52%(0.46% [†])	0.20%	π -ID sys.	0.50%(0.41% [†])	0.21%	3/5
K -ID stat.	0.76%	1.05%(0.72% [†])	K -ID stat.	0.72%	1.03%(0.72% [†])	K -ID stat.	0.66%	0.93%(0.64% [†])	3/5
K -ID sys.	0.53%	1.15%(0.61% [†])	K -ID sys.	0.57%	0.62%(0.62% [†])	K -ID sys.	0.49%	0.80%(0.55% [†])	3/5
K -ID run dep. sys.	0.30%	0.30%	K -ID run dep. sys.	0.30%	0.30%	K -ID run dep. sys.	0.27%	0.27%	3/5
π_{slow} stat.	0.79%	0.79%	π_{slow} stat.	0.79%	0.79%	π_{slow} stat.	0.79%	0.79%	1
π_{slow} sys.	0.01%	0.01%	π_{slow} sys.	0.01%	0.01%	π_{slow} sys.	0.01%	0.01%	1
π_{slow} corr.	1.33%	1.33%	π_{slow} corr.	1.33%	1.33%	π_{slow} corr.	1.33%	1.33%	1
3 tracks tracking sys.	1.05%	1.05%	5 tracks tracking sys.	1.75%	1.75%	tracking sys.	1.26%	1.26%	3/5
MC stat.	0.39% [†]	1.4% [†]	MC stat.	0.35% [†]	1.39% [†]	MC stat.	0.26% [†]	0.99% [†]	0
fixed yields bkg. PDF	0.10% [†]	0.10% [†]	fixed yields bkg. PDF	0.10% [†]	0.10% [†]	fixed yields bkg. PDF	0.07% [†]	0.07% [†]	0
fixed shapes bkg. PDF	0.10% [†]	0.10% [†]	fixed shapes bkg. PDF	0.10% [†]	0.10% [†]	fixed shapes bkg. PDF	0.07% [†]	0.07% [†]	0
fit bias	0.15% [†]	0.15% [†]	fit bias	0.08% [†]	0.74% [†]	fit bias	0.09% [†]	0.37% [†]	0
N- B^0 -mesons	1.84%	1.84%	N- B^0 -mesons	1.84%	1.84%	N- B^0 -mesons	1.60%	1.60%	1
$\mathcal{B}(D^{*+} \rightarrow D^0 \pi^+)$	0.74%	0.74%	$\mathcal{B}(D^{*+} \rightarrow D^0 \pi^+)$	0.74%	0.74%	$\mathcal{B}(D^{*+} \rightarrow D^0 \pi^+)$	0.74%	0.74%	1
$\mathcal{B}(D^0 \rightarrow K^- \pi^+)$	0.78%	0.78%	$\mathcal{B}(D^0 \rightarrow K^- 2\pi^+ \pi^-)$	1.70%	1.70%	$\mathcal{B}(D^0)$	0.94%	0.94%	0
total (Br.)	3.20%	3.60%	total (Br.)	3.81%	4.05%	total (Br.)	3.25%	3.42%	
total (ratio)	1.93%	1.93%	total (ratio)	1.89%	1.89%	total (ratio)	1.50%	1.50%	
fit stat. err.	0.84%	4.00%	fit stat. err. (Br.)	0.78%	3.70%	fit stat. err. (Br.)	0.57%	2.74%	

Belle: $B^0 \rightarrow \pi^0\pi^0$ and $B^0 \rightarrow K^0\pi^0$

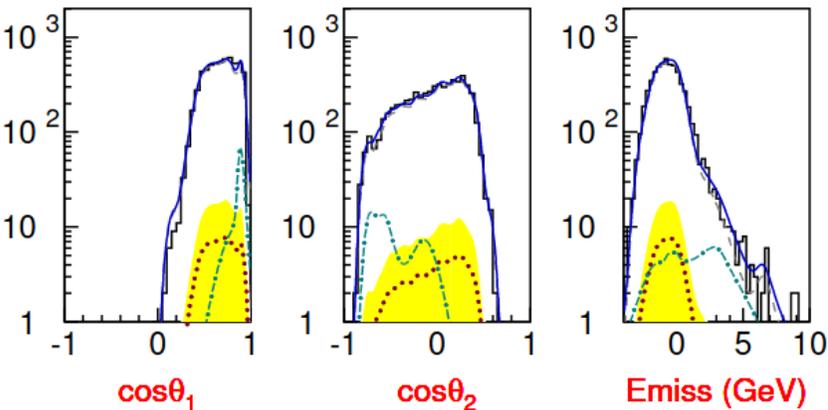
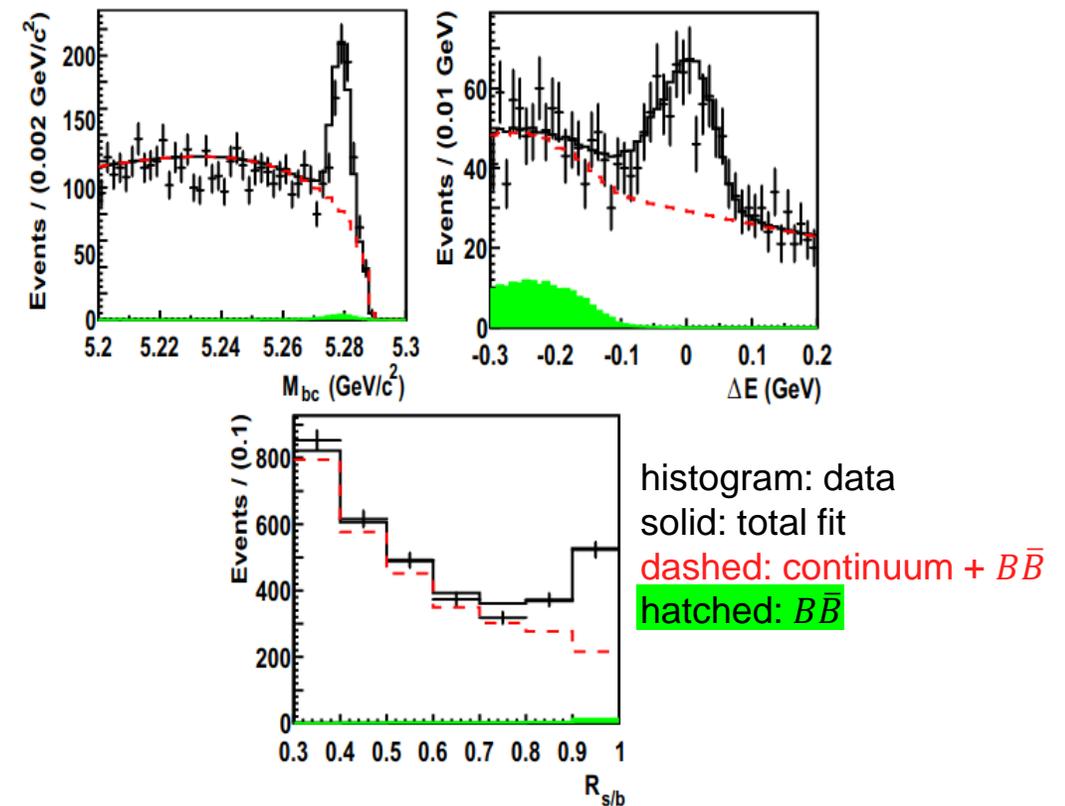
$B^0 \rightarrow \pi^0\pi^0$ ($535 \times 10^6 B\bar{B}$ pairs)

<https://arxiv.org/pdf/hep-ex/0610065.pdf>



$B^0 \rightarrow K^0\pi^0$ ($657 \times 10^6 B\bar{B}$ pairs)

<https://arxiv.org/pdf/0809.4366.pdf>



$$\mathcal{B}(B^0 \rightarrow \pi^0\pi^0) = (1.1 \pm 0.3(\text{stat.}) \pm 0.1(\text{syst.})) \times 10^{-6}$$

$$\mathcal{A}_{CP}(B^0 \rightarrow \pi^0\pi^0) = 0.44_{-0.62}^{+0.73}(\text{stat.})_{-0.06}^{+0.04}(\text{syst.})$$

$$\mathcal{B}(B^0 \rightarrow K^0\pi^0) = (8.7 \pm 0.5 \pm 0.6) \times 10^{-6}$$

$$\mathcal{A}_{K^0\pi^0} = +0.14 \pm 0.13 \pm 0.06$$