

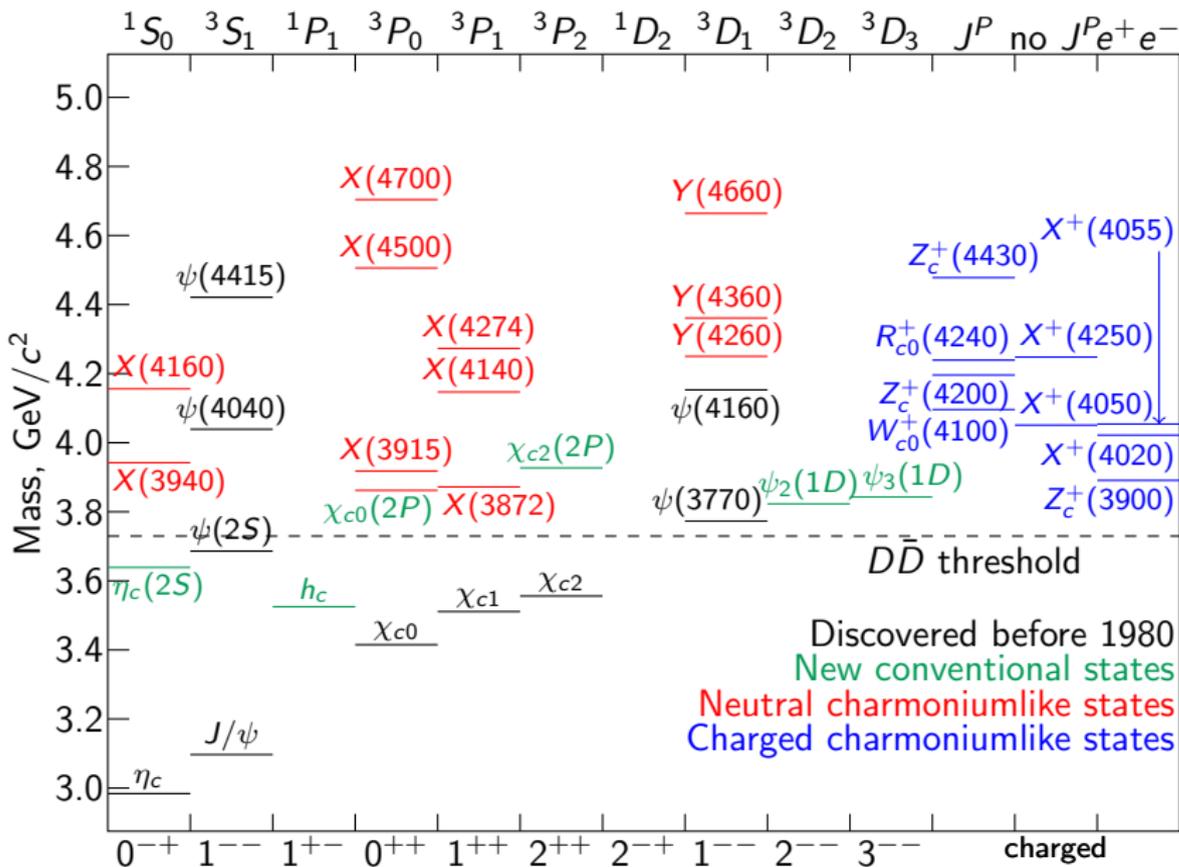
Quarkonium physics at Belle II

K. Chilikin (Belle II Collaboration)

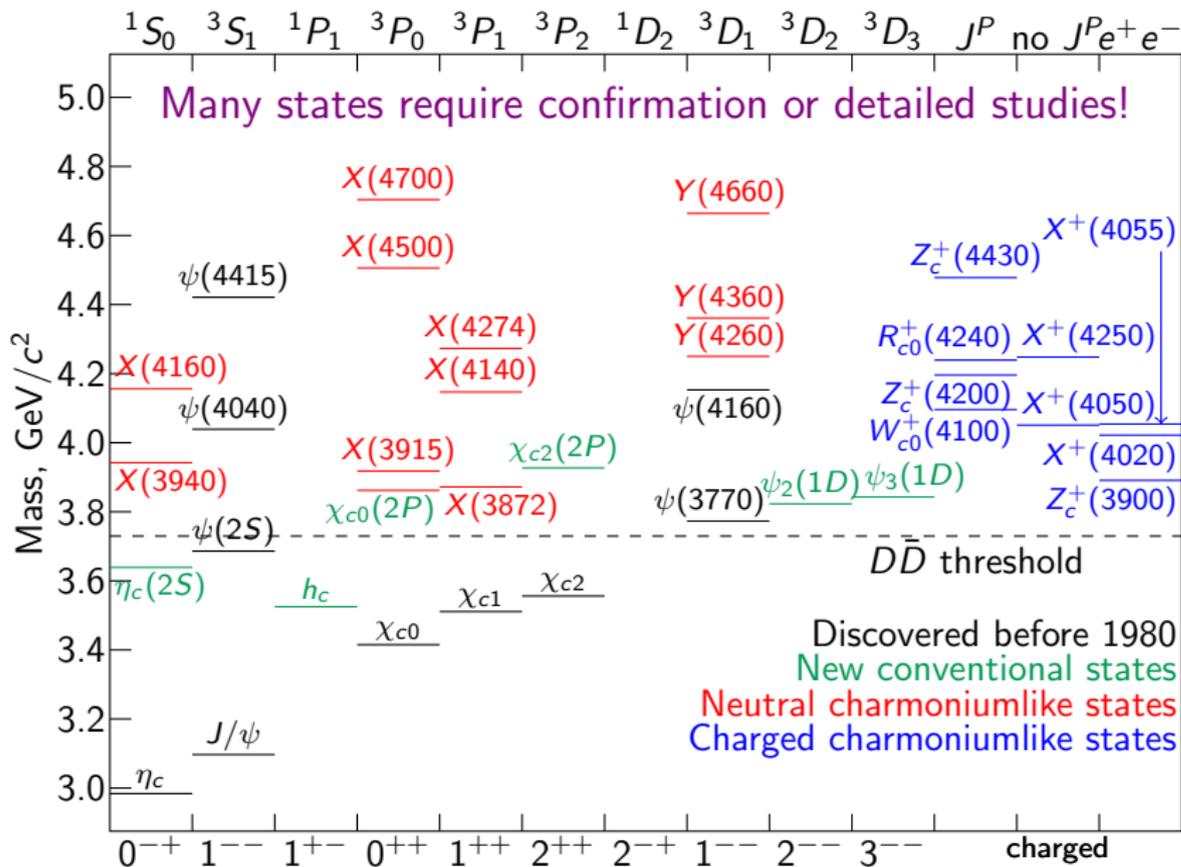
P.N. Lebedev Physical Institute of the Russian Academy of Sciences, Moscow, Russia

Excited QCD 2020, 4 February 2020

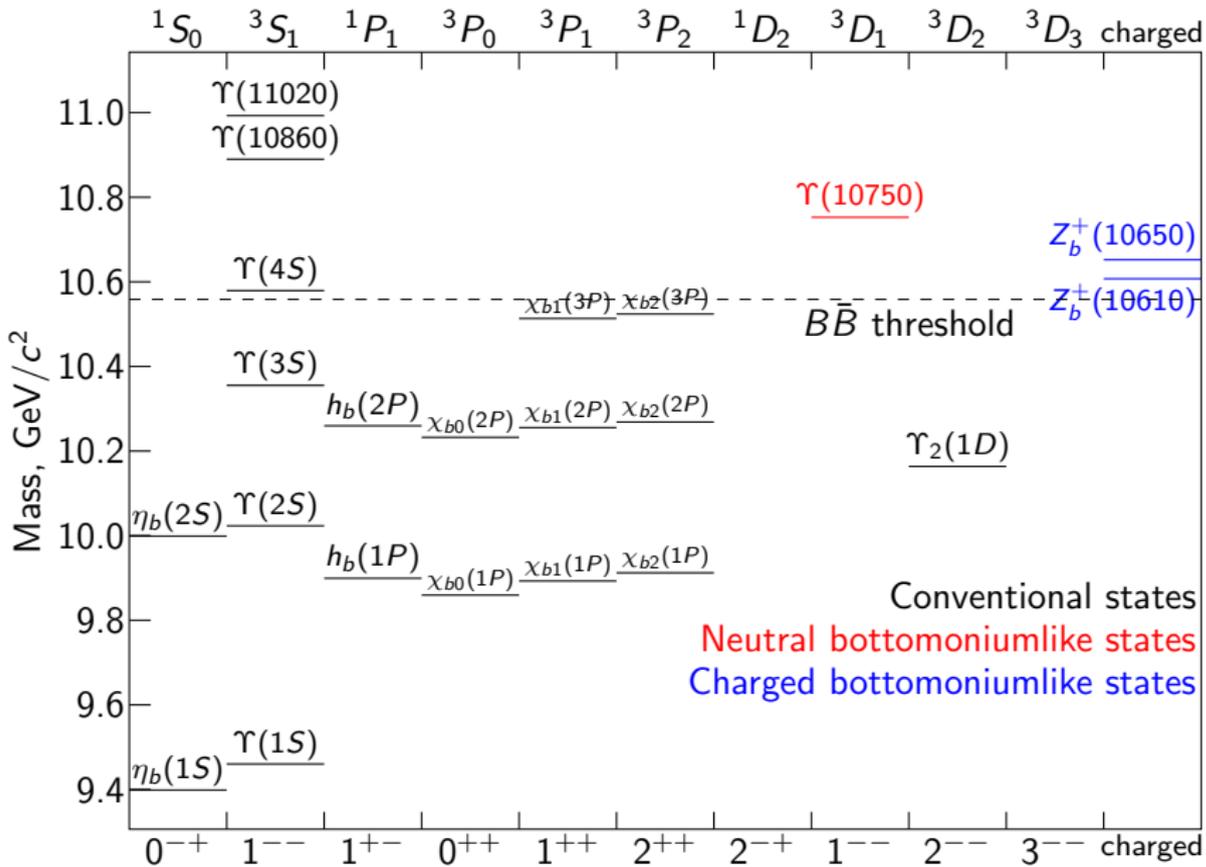
Charmonium states



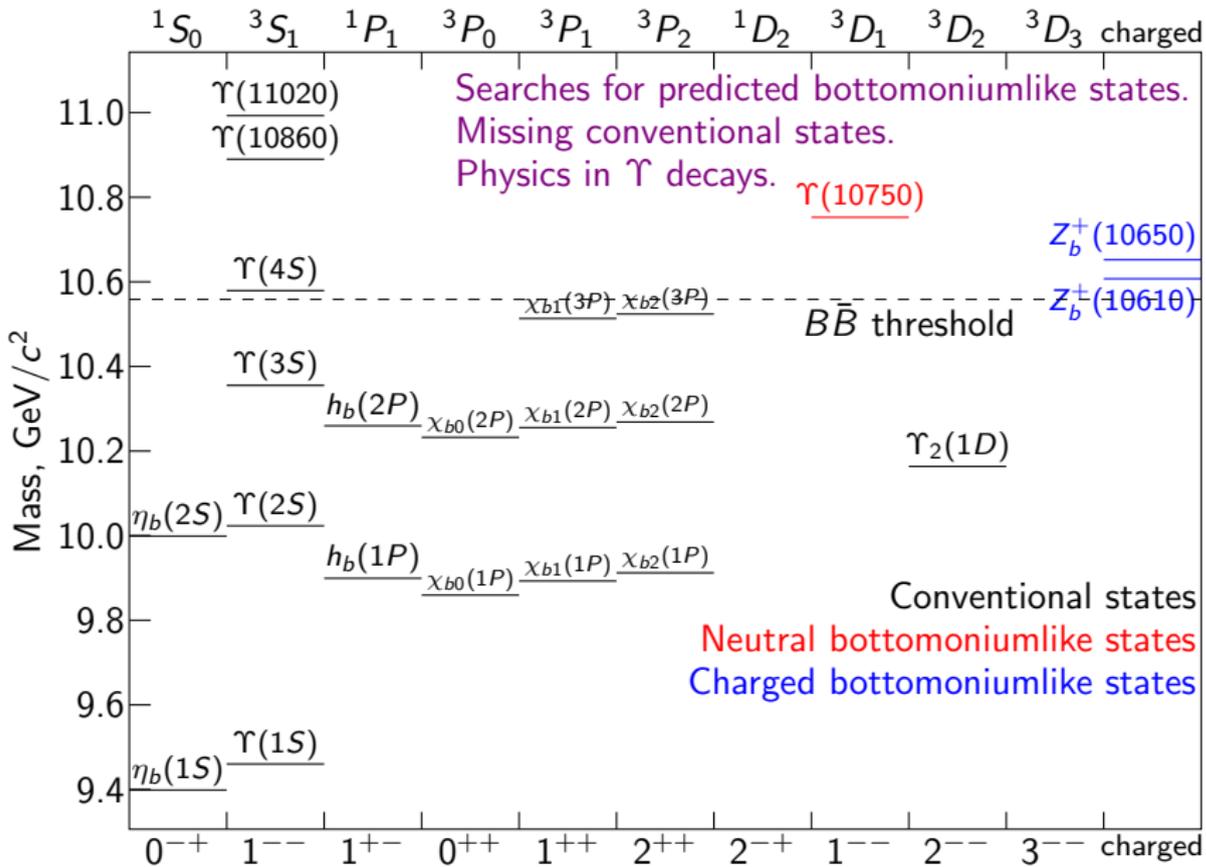
Charmonium states

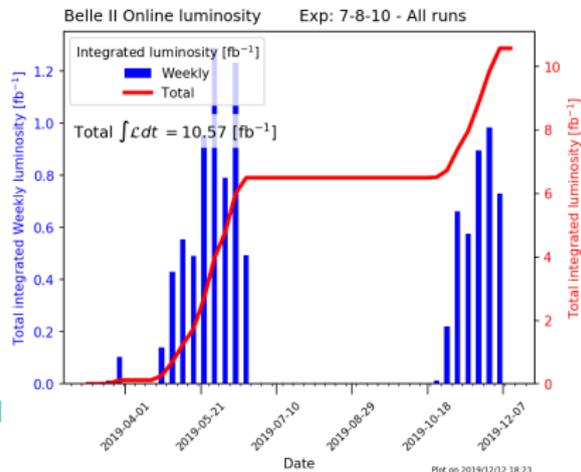
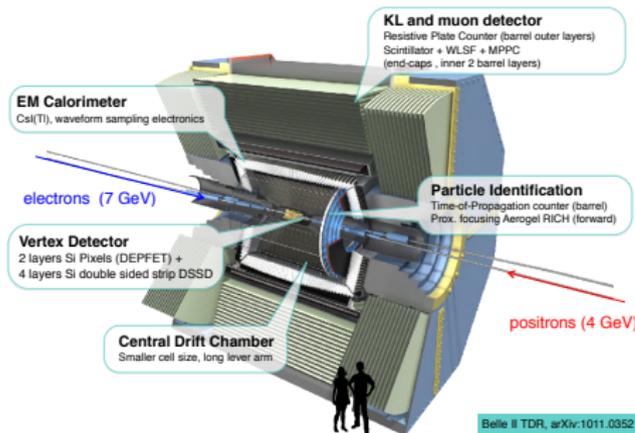


Bottomonium states



Bottomonium states



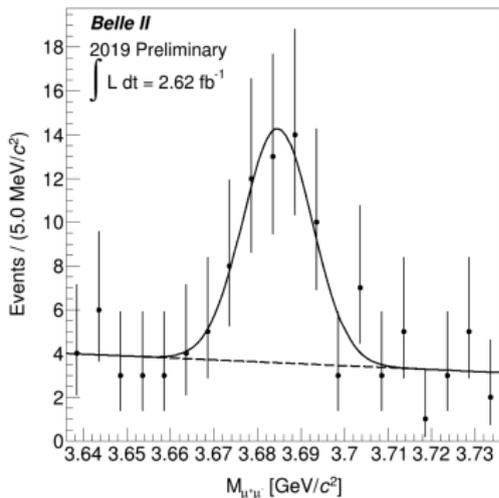
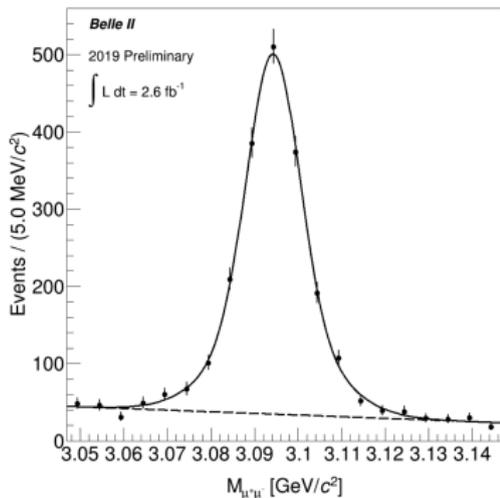


- The Belle II experiment operates at the e^+e^- collider SuperKEKB (the operation is mostly planned at the $\Upsilon(4S)$ resonance with $B\bar{B}$ pair production). The experiment and collider are designed to collect a much larger data sample compared to the old Belle experiment: $\approx 1 \text{ ab}^{-1} \rightarrow 50 \text{ ab}^{-1}$.
- A data sample of $\approx 10 \text{ fb}^{-1}$ was collected in 2019. The 2020 run will start soon.
- The data sample is currently too small for new quarkonium results. However, it is already possible to look at some known quarkonium states or exclusive B decays to the J/ψ or $\psi(2S)$ and other particles.

Current quarkonium studies

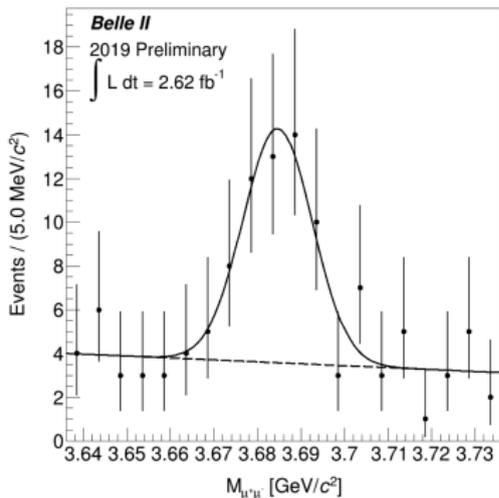
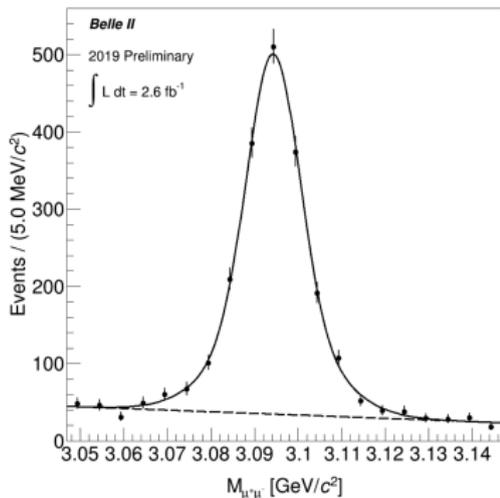
Inclusive J/ψ and $\psi(2S)$ from B decays

Inclusive production of the J/ψ and $\psi(2S)$ in B decays is observed in the $\mu^+\mu^-$ decay mode using a data sample of 2.62 fb^{-1} . The tracks are required to be identified as muons. Charmonia produced from B decays are selected by requiring $R_2 < 0.3$, $p_{\text{cms}} < 4.25 \text{ GeV}/c$, and $N_{\text{tracks}} > 4$, where R_2 is the second normalized Fox-Wolfram moment.



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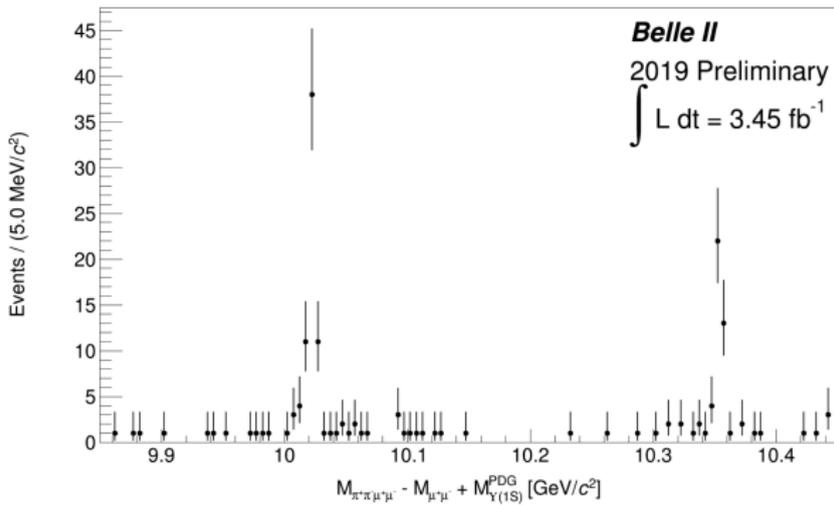
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Inclusive production of ψ states is observed.

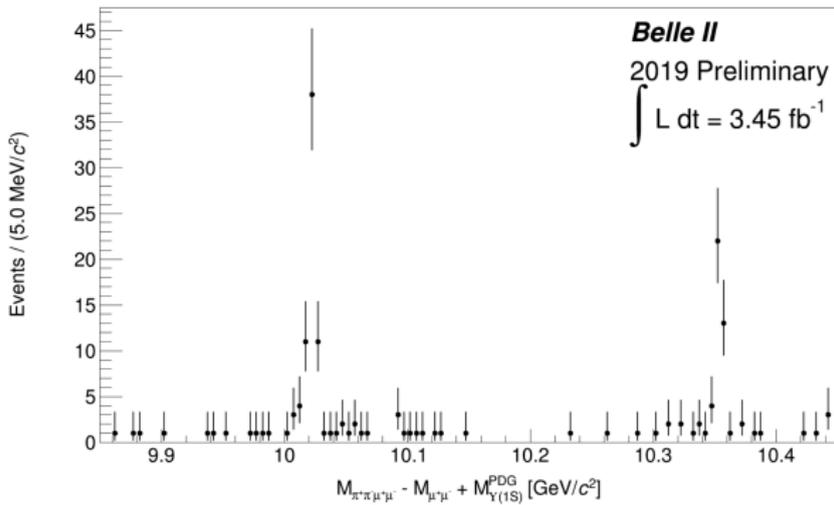
$$\Upsilon(nS) \rightarrow \Upsilon(1S)\pi^+\pi^-$$

The $\Upsilon(2S)$ and $\Upsilon(3S)$ resonances produced via initial-state radiation are observed in the channel $\Upsilon(nS) \rightarrow \Upsilon(1S)\pi^+\pi^-$ using a data sample of 3.45 fb^{-1} . The $\Upsilon(1S)$ is reconstructed in the $\Upsilon(1S) \rightarrow \mu^+\mu^-$ decay mode with the requirement $|M_{\Upsilon(1S)} - m_{\Upsilon(1S)}| < 50 \text{ MeV}/c^2$, where $M_{\Upsilon(1S)}$ and $m_{\Upsilon(1S)}$ are the reconstructed and nominal masses, respectively.



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Inclusive production of Υ states is observed.

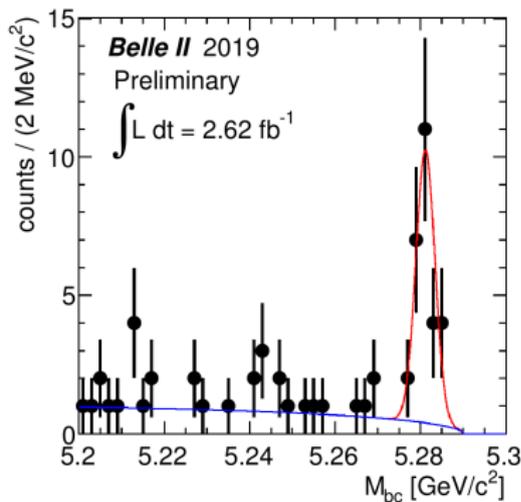
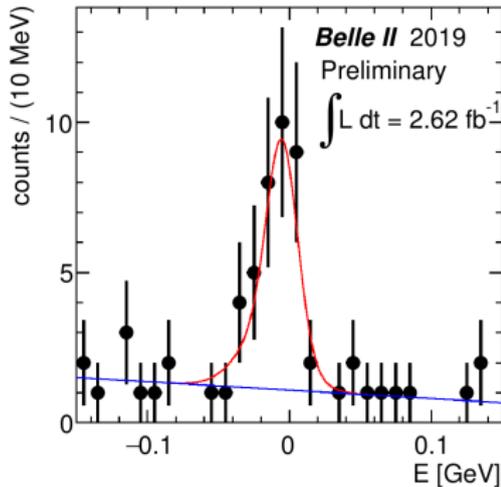
$$B^0 \rightarrow J/\psi K_S^0$$

The decay $B^0 \rightarrow J/\psi K_S^0$ is observed using a data sample of 2.62 fb^{-1} .

The decay modes used for reconstruction are $J/\psi \rightarrow \mu^+ \mu^-$,

$J/\psi \rightarrow e^+ e^-$, and $K_S^0 \rightarrow \pi^+ \pi^-$.

Fit: ΔE : 2 Gaussians + first-order polynomial, M_{bc} : Gaussian + ARGUS. Yield: 26.9 ± 5.2 (expected: 27.5).



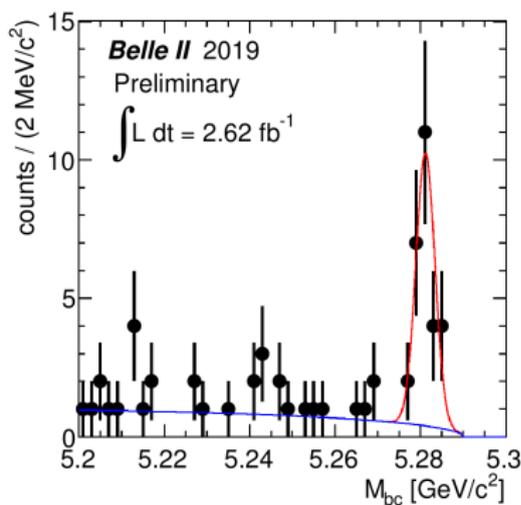
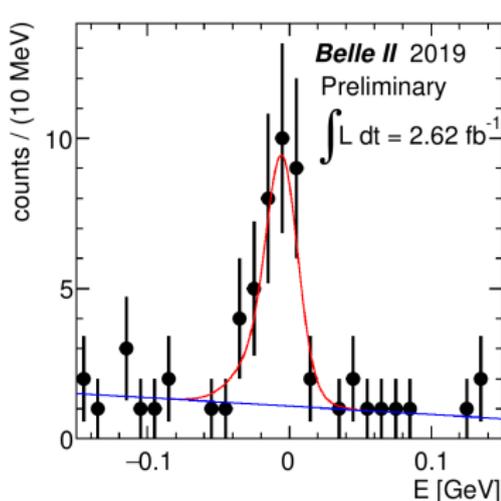
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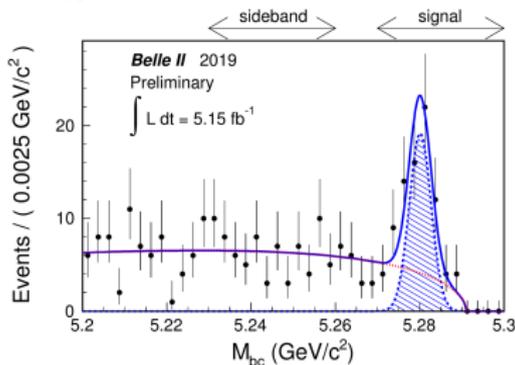


This decay mode is important for CP violation studies.

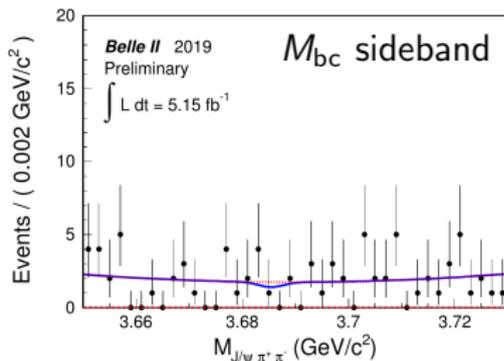
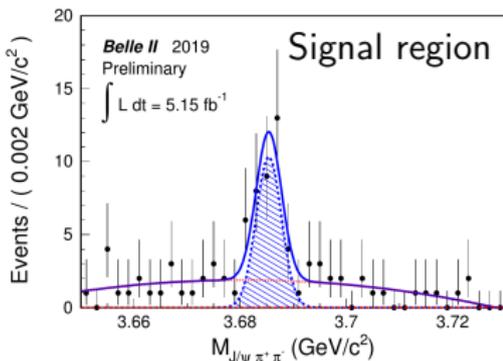
$B \rightarrow \psi(2S)K$

The decay $B \rightarrow \psi(2S)K$ ($K = K^+, K_S^0$) is observed using a data sample of 5.15 fb^{-1} . The decay modes used for reconstruction are $\psi(2S) \rightarrow J/\psi \pi^+ \pi^-$, $J/\psi \rightarrow \mu^+ \mu^-$, $J/\psi \rightarrow e^+ e^-$, and $K_S^0 \rightarrow \pi^+ \pi^-$.

M_{bc} fit: ARGUS + Gaussian:



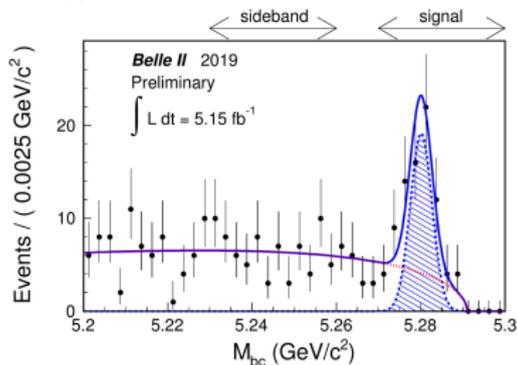
$M_{\psi(2S)}$ fit: Gaussian + second-order polynomial:



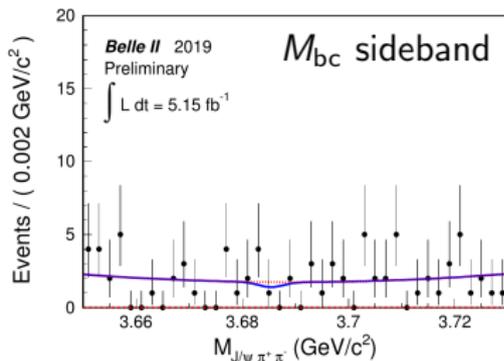
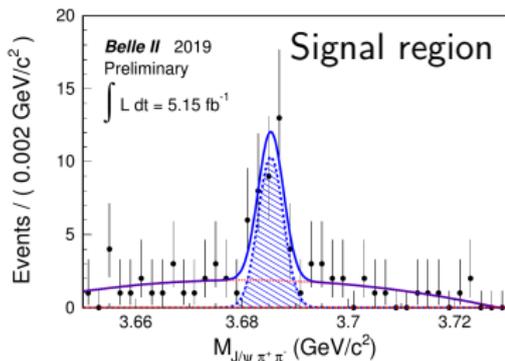
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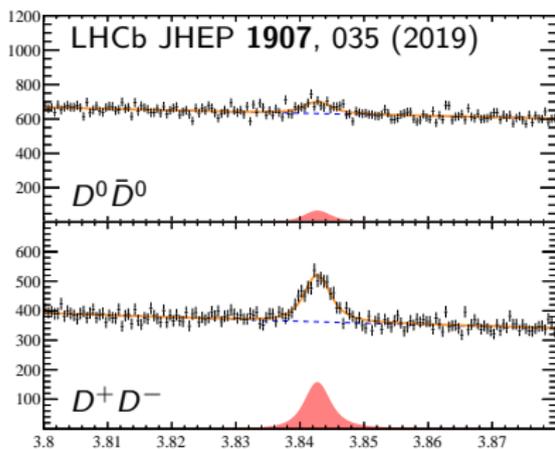


The decay mode $B \rightarrow J/\psi\pi^+\pi^-K$ is the $X(3872)$ observation mode.

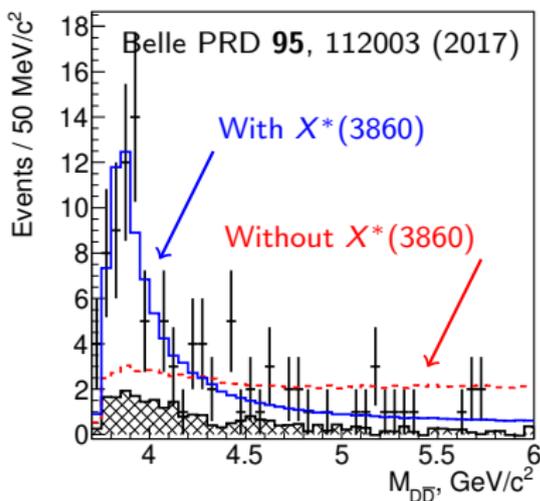
Quarkonium physics program

Conventional charmonium: current status

Observation of the $\psi_3(1D)$
(prompt production)



Observation of the $X^*(3860)$
($e^+e^- \rightarrow J/\psi X^*(3860) (\rightarrow D\bar{D})$)



The $\psi_3(1D)$ has not been observed in B decays (although its production should be suppressed because of its high spin: the decay $B \rightarrow \psi_3(1D)K$ proceeds in the F -wave). None of the states observed in double charmonium production were observed in B decays.

Conventional charmonium: can be done

1. Search for the $\psi_3(1D)$ in B decays ($B \rightarrow D\bar{D}K$).
2. Search for excited conventional states using $B \rightarrow D^{(*)}\bar{D}^{(*)}K$, for example, $X^*(3860) \rightarrow D\bar{D}$ (expected to be seen in B decays if the $X^*(3860)$ is the $\chi_{c0}(2P)$).
3. Search for the $\eta_{c2}(1D)$ using the channel $\eta_{c2}(1D) \rightarrow h_c\gamma$.

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Belle II has a good sensitivity for channels with photons.

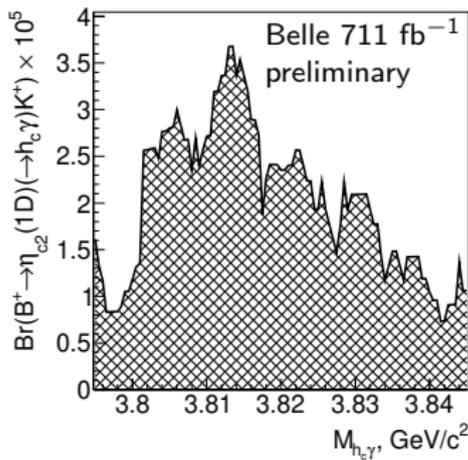
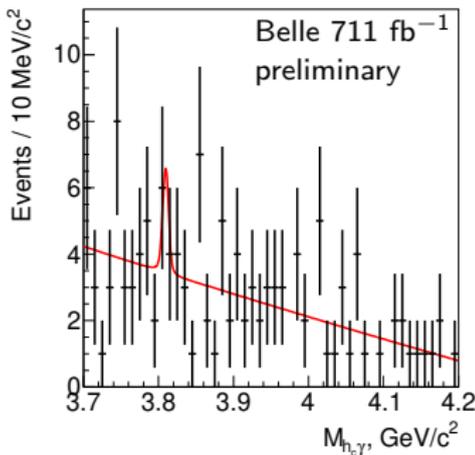
The $\eta_{c2}(1D)$ is the only charmonium state without open-charm decays that remains unobserved.

Detailed discussion of the $\eta_{c2}(1D)$ search follows.

A search for the $\eta_{c2}(1D)$ is performed in 4 B decays: $B^+ \rightarrow \eta_{c2}(1D)K^+$, $B^0 \rightarrow \eta_{c2}(1D)K_S^0$, $B^0 \rightarrow \eta_{c2}(1D)\pi^-K^+$, $B^+ \rightarrow \eta_{c2}(1D)\pi^+K_S^0$ with $\eta_{c2}(1D) \rightarrow h_c\gamma$, $h_c \rightarrow \eta_c\gamma$, and $\eta_c \rightarrow 10$ channels. The $\eta_{c2}(1D)$ search region is from 3795 to 3845 MeV/c^2 . No significant signal is found.

$B^+ \rightarrow \eta_{c2}(1D)K^+$ signal fit.

B confidence intervals (90%).



Upper limits (90% C. L.) for any mass within the search range:

$$\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)K^+) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma) < 3.7 \times 10^{-5},$$

$$\mathcal{B}(B^0 \rightarrow \eta_{c2}(1D)K_S^0) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma) < 3.5 \times 10^{-5},$$

$$\mathcal{B}(B^0 \rightarrow \eta_{c2}(1D)\pi^-K^+) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma) < 1.0 \times 10^{-4},$$

$$\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)\pi^+K_S^0) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma) < 1.1 \times 10^{-4}.$$

Theoretical prediction (PRD **94**, 034005 (2016)):

$$\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)K^+) = (1.72 \pm 0.42) \times 10^{-5}, \text{ thus,}$$

$$\mathcal{B}(B^+ \rightarrow \eta_{c2}(1D)K^+) \times \mathcal{B}(\eta_{c2}(1D) \rightarrow h_c\gamma) \sim 1.0 \times 10^{-5}.$$

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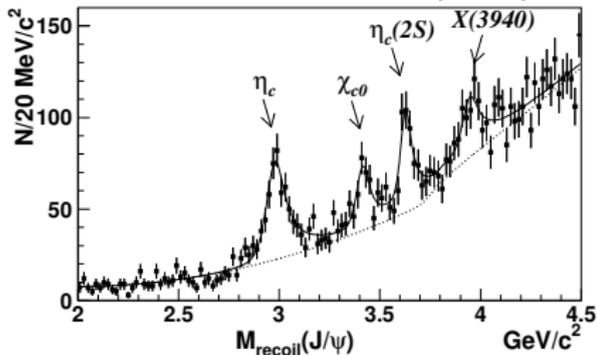
Simple estimate of the required luminosity for Belle II by rescaling:

$$\text{Sensitivity} \propto S/\sqrt{S+B} \propto \sqrt{\mathcal{L}}.$$

$$\text{Required luminosity: } \mathcal{L} \propto (\mathcal{B}_{\text{observed limit}}/\mathcal{B}_{\text{theory}})^2 \mathcal{L}_{\text{Belle}} \approx 10 \text{ ab}^{-1}.$$

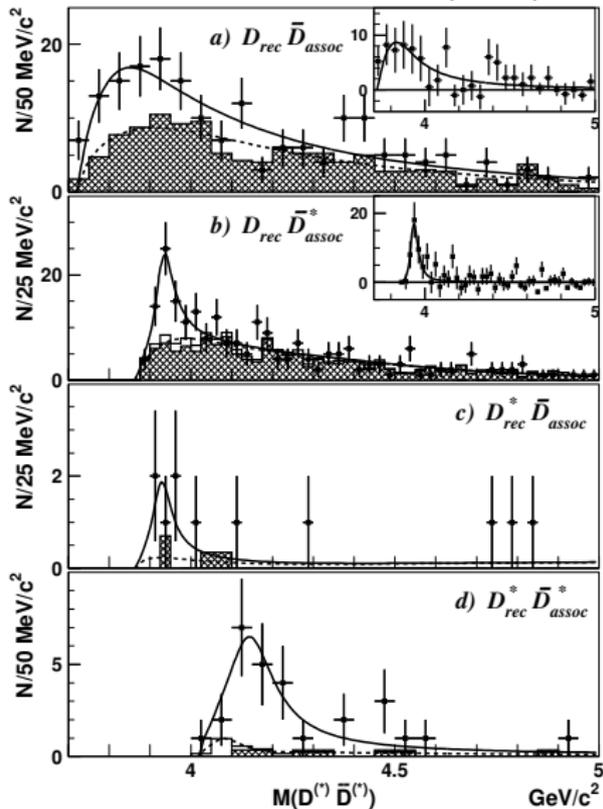
While this estimate does not account for difference of reconstruction efficiency or background conditions, that can modify it, with full luminosity of 50 ab^{-1} Belle II should certainly be able to observe the $\eta_{c2}(1D)$ or exclude the predicted branching fraction.

Belle PRL **98**, 092001 (2007)



The $X(3940)$ ($X(4160)$) was observed in $e^+e^- \rightarrow J/\psi D^* \bar{D}^{(*)}$. The $X(3940)$ was also observed in inclusive $e^+e^- \rightarrow J/\psi X$ events. Channels without the J/ψ require more statistics for their study. It was done in PRD **79**, 071101 for the $\psi(2S)$, χ_{c1} , and χ_{c2} , but only the $e^+e^- \rightarrow \psi(2S)X$ spectrum has significant signals.

Belle PRL **100**, 202001 (2008)



Double charmonium production: can be done

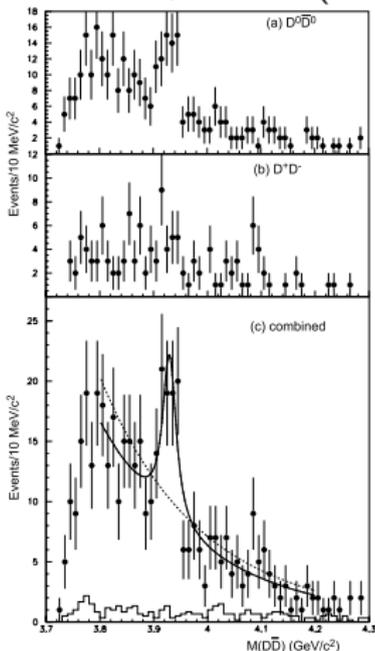
1. All observed exclusive processes are of the type $e^+e^- \rightarrow (c\bar{c})_{J=1}(c\bar{c})_{J=0}$. Is this rule valid for the reconstructed state that is not the J/ψ or $\psi(2S)$? One can try to study $e^+e^- \rightarrow \eta_c X$, $e^+e^- \rightarrow \chi_{c0} X$; these analyses are difficult due to hadronic decays of the reconstructed charmonium states and, if possible, require large statistics.
2. Amplitude analyses of $e^+e^- \rightarrow J/\psi D^* \bar{D}$ and $e^+e^- \rightarrow J/\psi D^* \bar{D}^*$ to measure the quantum numbers of the $X(3940)$ and $X(4160)$, respectively. Updated amplitude analysis of $e^+e^- \rightarrow J/\psi D \bar{D}$ to measure the $X^*(3860)$ quantum numbers with certainty.
3. Analysis of the $e^+e^- \rightarrow \psi(2S) D^{(*)} \bar{D}^{(*)}$, measurement of the $X^*(3860)$, $X(3940)$, $X(4160)$ production in the above processes.

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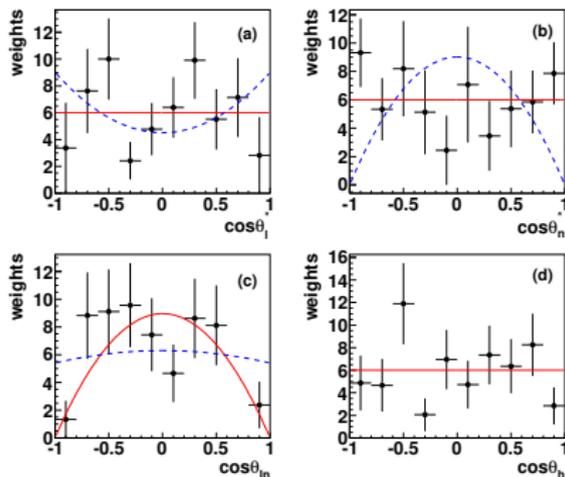
Unique for Belle II!

Conventional states, e.g.: $\chi_{c2}(2P)$
 Belle PRL **96**, 082003 (2006)



This is the only state with an open-charm decay observed in $\gamma\gamma$.

J^P of the $X(3915)$: 0^+ vs. 2^+
 BABAR PRD **86**, 072002 (2012)



BABAR assumed that for $J = 2$
 $\lambda = \pm 2$, without this assumption 2^+
 is not excluded [see PRL **115**,
 022001 (2015)].

Charmonium in two-photon processes: can be done

1. Measurement of the $X(3915)$ quantum numbers without any restrictions on its helicity.
2. Amplitude analysis of the $\chi_{c2}(2P)$, measurement of the production amplitudes with $\lambda = \pm 2$ and $\lambda = 0$.
3. Search for charmonium states produced in $\gamma\gamma$ decaying to $D^*\bar{D}$ or $D^*\bar{D}^*$.
4. Updated analysis of the $J/\psi\phi$, check of the $X(4350)$ existence.

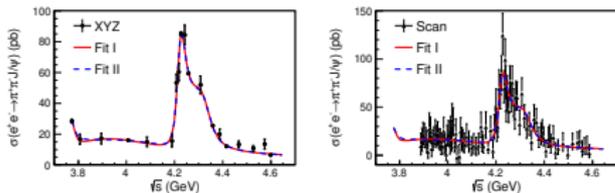
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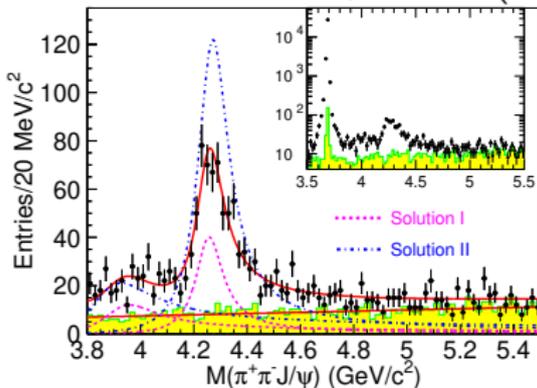
Unique for Belle II!

Charmonium in ISR: current status

Cross section of $e^+e^- \rightarrow J/\psi\pi^+\pi^-$
 BESIII PRL **118**, 092001 (2017)

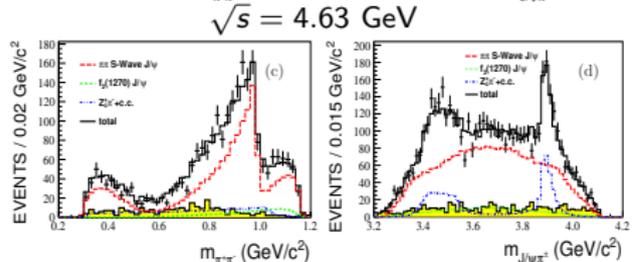
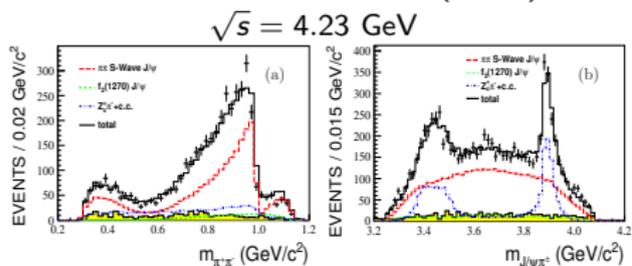


Belle PRL **110**, 252002 (2013)

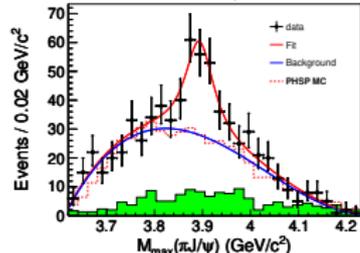


Comparison of Belle and BESIII
 (latest high-statistic analyses for
 BESIII).

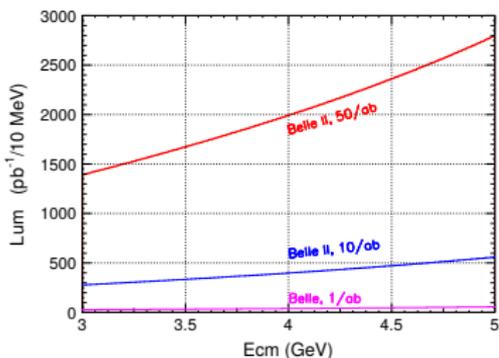
Observation of $Z_c(3900)^+ \rightarrow J/\psi\pi^+$
 BESIII PRL **119**, 072001 (2017)



Belle PRL **110**, 252002 (2013)



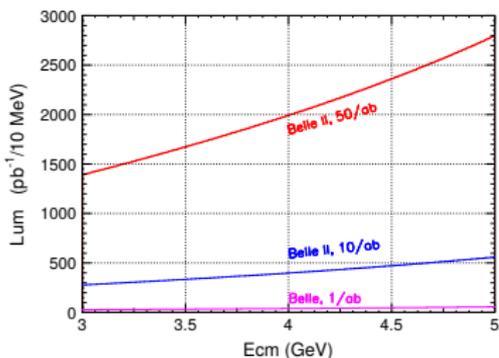
Charmonium in ISR: can be done



- Comparable samples for e.g. $e^+e^- \rightarrow J/\psi\pi^+\pi^-$.
- Access for high-energy region (current limit for BESIII is 4.6 GeV).
- Data are accumulated at the same time for all energies - simplifies lineshape analysis.

1. Improved measurements and fits of $e^+e^- \rightarrow \gamma_{\text{ISR}}(c\bar{c})(X)$ cross sections.
2. Improved measurements and fits of the open-charm cross-sections, for example $e^+e^- \rightarrow \gamma_{\text{ISR}}D^{(*)}\bar{D}^{(*)}(X)$
3. Measurements of higher mass open-charm channels, for example $e^+e^- \rightarrow \gamma_{\text{ISR}}\Sigma_c^+\bar{\Sigma}_c^-$.
4. Analyses of the channels that are currently studied at BESIII only, for example $e^+e^- \rightarrow h_c\pi^+\pi^-$ with confirmation of the $Z_c(4020)^+$.

Charmonium in ISR: can be done



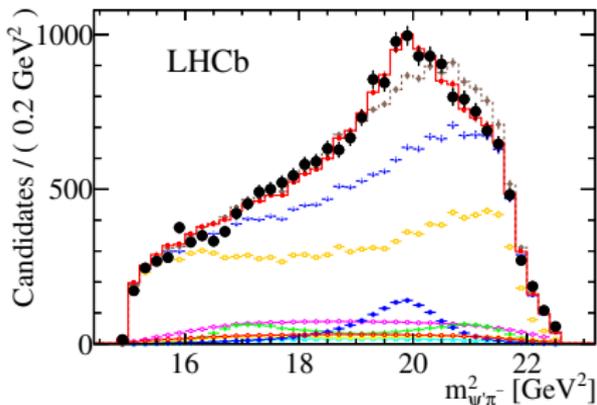
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1. Improved measurements and fits of $e^+e^- \rightarrow \gamma_{\text{ISR}}(c\bar{c})(X)$ cross sections.
2. Improved measurements and fits of the open-charm cross-sections, for example $e^+e^- \rightarrow \gamma_{\text{ISR}}D^{(*)}\bar{D}^{(*)}(X)$
3. Measurements of higher mass open-charm channels, for example $e^+e^- \rightarrow \gamma_{\text{ISR}}\Sigma_c^+\bar{\Sigma}_c^-$.
4. Analyses of the channels that are currently studied at BESIII only, for example $e^+e^- \rightarrow h_c\pi^+\pi^-$ with confirmation of the $Z_c(4020)^+$.

Can be done at Belle II and BESIII with direct production.

Charged charmoniumlike states: current status

$Z_c(4430)^+ (B^0 \rightarrow \psi(2S)\pi^- K^+)$
 LHCb PRL **112**, 222002 (2014)

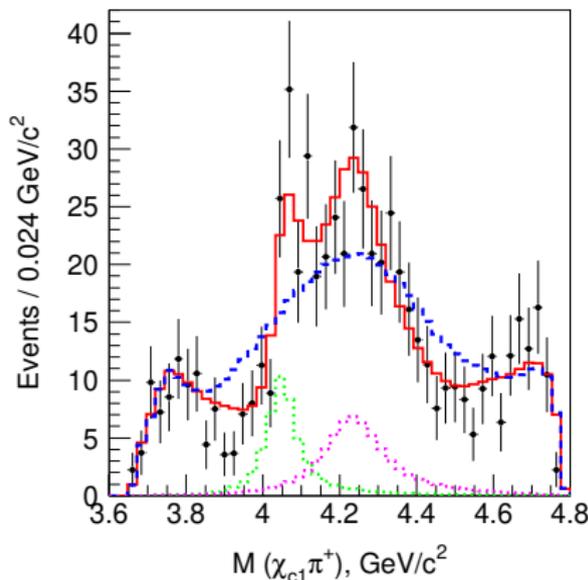


Belle (first J^P): PRD **88**, 074026
 (2013)
 (These analyses are the latest ones;
 observed by Belle in PRL **100**, 142001
 (2008).)

Only the $Z_c(4430)^+$ is confirmed (seen by Belle and LHCb), it is studied relatively well now. Other charged charmoniumlike states observed in B decays are not confirmed; the analyses were performed either only at Belle or only at LHCb.

$Z_c(4050)^+, Z_c(4250)^+$
 $(B^0 \rightarrow \chi_{c1}\pi^- K^+)$

Belle PRD **78**, 072004 (2008)



Charged charmoniumlike states: can be done

1. Updated amplitude analysis of $\bar{B}^0 \rightarrow \psi(2S)\pi^+K^-$: confirmation of the LHCb observation of the resonant character of the $Z_c(4430)^+$, confirmation of the $Z_c(4240)^+ / R_{c0}(4240)^+$.
2. Confirmation of the $W_{c0}(4100)^+$ in $\bar{B}^0 \rightarrow \eta_c\pi^+K^-$
3. Amplitude analysis of $\bar{B}^0 \rightarrow \chi_{c1}\pi^+K^-$, measurement of the $Z_c(4050)^+$ and $Z_c(4250)^+$ quantum numbers.
4. Search for the neutral partners of all charged charmoniumlike states observed in B decays.
5. Amplitude analyses of unexplored channels, for example $\bar{B}^0 \rightarrow X(3872)\pi^+K^-$.
6. Search for the $Z_c(3900)^+$ in $\bar{B}^0 \rightarrow J/\psi\pi^+\pi^-K^+$.
7. Search for decays of charged charmoniumlike states to $D^{(*)}\bar{D}^{(*)}$ in $B \rightarrow D^{(*)}\bar{D}^{(*)}K$.

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Can be done at Belle II and LHCb.

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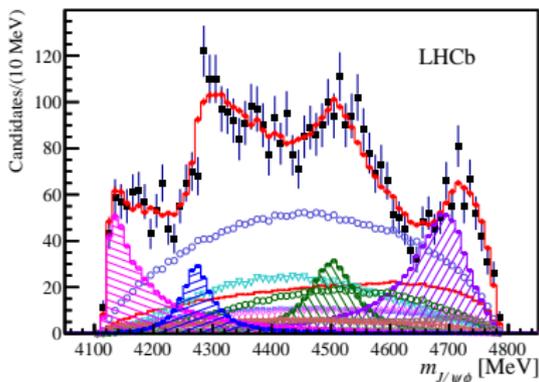
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Belle II has a good sensitivity for neutral partners.

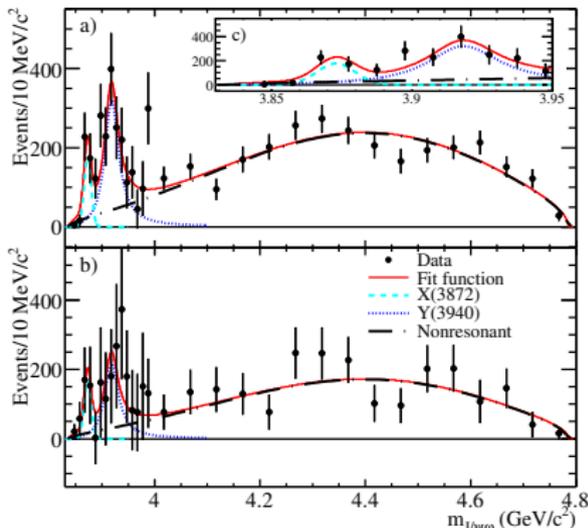
$$B^+ \rightarrow J/\psi \phi K^+$$

LHCb PRL **118**, 022003 (2017)
(amplitude analysis)



$$B \rightarrow J/\psi \omega K$$

BABAR PRD **82**, 011101 (2010)



While the $X(4140)$ and $X(4274)$ are seen by many experiments, the only amplitude analysis (and observation of two other states), has been performed by LHCb. The $X(3915)$ is also seen by Belle and BABAR, but the amplitude analysis of the decay $B \rightarrow J/\psi \omega K$ has never been performed.

Neutral charmoniumlike states: can be done

1. Amplitude analysis of $B \rightarrow J/\psi\phi K$, confirmation of 4 states observed by LHCb.
2. Amplitude analysis of $B \rightarrow J/\psi\omega K$, measurement of the $X(3915)$ quantum numbers in B decays.
3. Updated search for $B \rightarrow Y(4260)(\rightarrow J/\psi\pi^+\pi^-)K$ and other $J^{PC} = 1^{--}$ charmoniumlike states.
4. Amplitude analyses of unexplored channels with a J/ψ such as $B \rightarrow J/\psi\eta K$ or $B \rightarrow J/\psi\eta' K$.
5. Analyses of the above channels with K_S^0 .
6. Search for decays of known charmoniumlike states to other final states, for example, $X(3915) \rightarrow \eta_c\eta$ ($X(3915)$ should decay to this channel if it is a $c\bar{c}s\bar{s}$ state).
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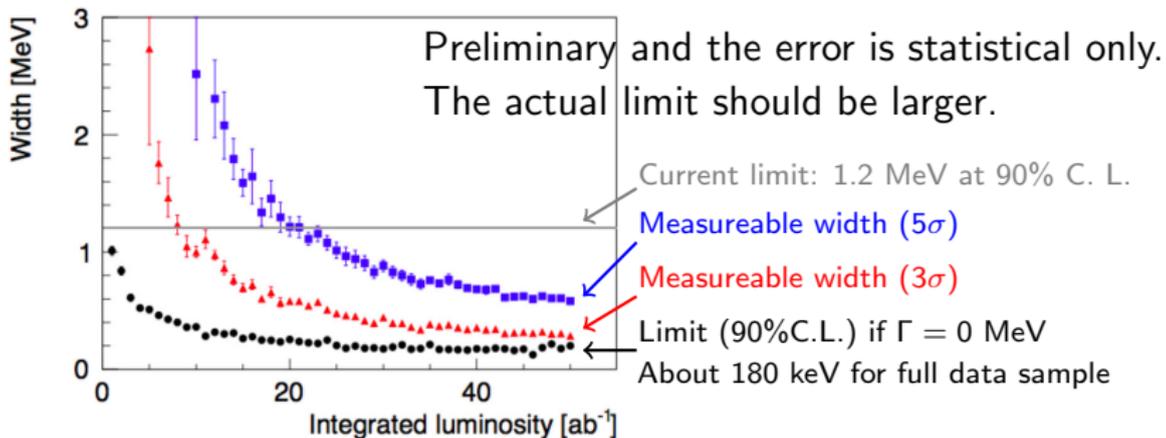
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Can be done at Belle II and LHCb.

Absolute branching fractions are unique for Belle II!

The $X(3872)$ width: sensitivity

- The current upper limit on the $X(3872)$ width is 1.2 MeV at 90% C. L (Belle PRD **84**, 052004 (2011), from $B \rightarrow J/\psi\pi^+\pi^-K$ data).
- Using the $B \rightarrow (D^0\bar{D}^0\pi^0)K$ data can significantly improve the mass resolution (near-threshold decay), and, consequently, the total-width sensitivity.
- The sensitivity has been estimated on MC (H. Hirata, master thesis, 2019), the expectation is shown below.



Bottomonium: $\Upsilon(3S)$ data

Current samples in fb^{-1} (millions of events)

Experiment	$\Upsilon(1S)$	$\Upsilon(2S)$	$\Upsilon(3S)$	$\Upsilon(4S)$	$\Upsilon(5S)$	$\Upsilon(6S)$	$\frac{\Upsilon(nS)}{\Upsilon(4S)}$
CLEO	1.2 (21)	1.2 (10)	1.2 (5)	16 (17.1)	0.1 (0.4)	-	23%
BaBar	-	14 (99)	30 (122)	433 (471)	R_b scan	R_b scan	11%
Belle	6 (102)	25 (158)	3 (12)	711 (772)	121 (36)	5.5	23%
BelleII	-	-	300 (1200)	5×10^4 (5.4×10^4)	1000 (300)	100+400(scan)	3.6%

1. Inclusive production of charmonium(-like) states in $\Upsilon(nS)$ decays.
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4. Search for missing $\pi\pi$ and η transitions to lower-mass bottomonium states, suppressed radiative transitions.
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6. Correlation in $D\bar{D}^*$ production.
7. Study of deuteron production.

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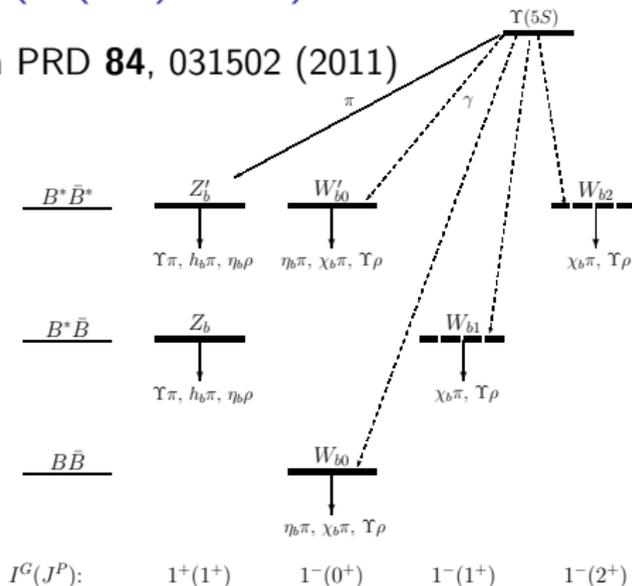
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Can be done at Belle and (some topics) LHC experiments.

Bottomonium ($\Upsilon(5S)$ data): can be done

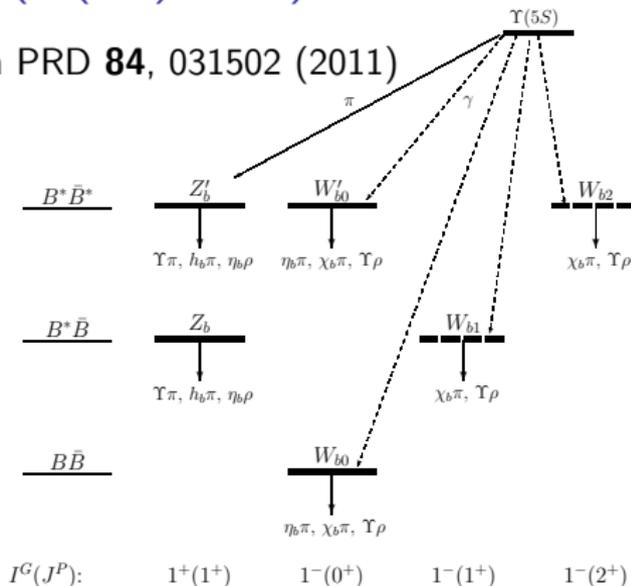
M. Voloshin PRD **84**, 031502 (2011)



Molecular states with quantum numbers other than $I^G = 1^+, J^P = 1^+$ are expected to exist. The transitions to such states are radiative and they are consequently suppressed by $\sim \alpha$. However, using the high statistics their observation might be possible.

Bottomonium ($\Upsilon(5S)$ data): can be done

M. Voloshin PRD **84**, 031502 (2011)

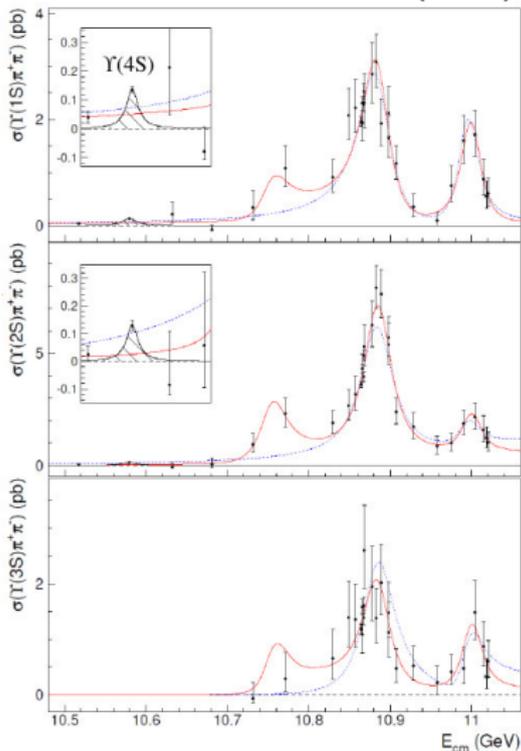


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Unique for Belle II!

Bottomonium: $\Upsilon(6S)$ data and $\Upsilon(5S) - \Upsilon(6S)$ scan

Belle JHEP **1910**, 220 (2019)

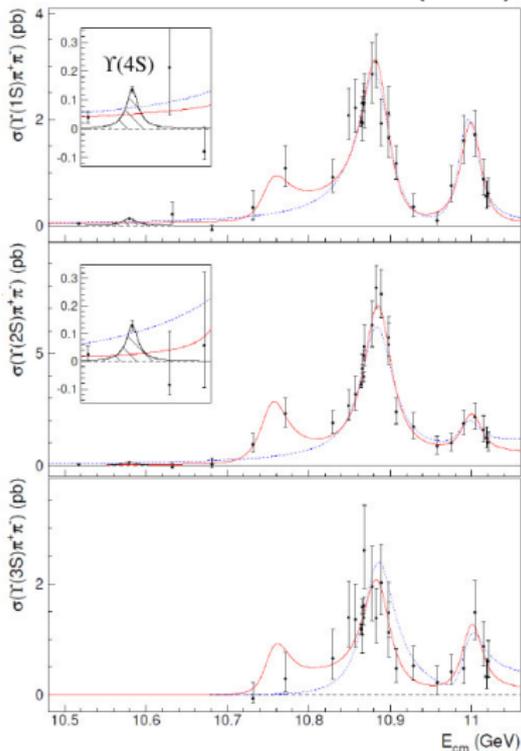


The $\Upsilon(10750)$ is observed by Belle in the scan data in the channel $\Upsilon(nS)\pi^+\pi^-$. Can be done:

1. A study with higher statistics will be possible.
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- The expected Belle II data sample of 50 ab^{-1} will provide a lot of new opportunities for physics analyses in the area of quarkonium.
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For further details about Belle II physics prospects, see the Belle II Physics Book (PTEP **2019**, 123C01 (2019)).