



Measurement of Hadronic Vacuum Polarization contributions to muon $(g-2)$ at Belle (II)

A.Kuzmin/B.Shwartz
BINP/NSU

Motivations for precise hadronic cross section measurements

- Tests of perturbative QCD
 - QCD sum rules, quark masses, quark and gluon condensates
 - Higher order QCD corrections - Λ_{QCD} , $\alpha(s)$
- Hadronic corrections to fundamental parameters:
 - Running fine structure constant - $\alpha(M_Z^2)$
 - **Anomalous magnetic moment of the muon**
- measurement of parameters of light vector mesons ρ , ω , φ , ρ' , ρ'' ,
- Search of and study of the exotic resonance states (X, Y, Z, ...)
- Study of the final states dynamics and test of theoretical models
- comparison with spectral functions of the hadronic tau decays via CVC
- Study of nucleon-antinucleon pair production – nucleon electromagnetic form factors, search for NNbar resonances, ..

Lepton dipole moments

$$\mathcal{H} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

Magnetic Dipole Moment

$$\vec{\mu} = g \left(\frac{q}{2m} \right) \vec{s}$$

Electric Dipole Moment

$$\vec{d} = \eta \left(\frac{q}{2mc} \right) \vec{s}$$

An essential difference between μ and d is:

μ - is calculated and precisely measured while $d \approx 0$.

Anomalous magnetic moments

Particle	$a_l = (g-2)/2$	SM
e	0.001 159 652 180 91 (26)	0.001 159 652 181 64 (76)
μ	0.001 165 920 89 (64)	0.001 165 918 23 (43)
τ	>-0.052 and <0.013 (95%)	0.001 177 21(5)

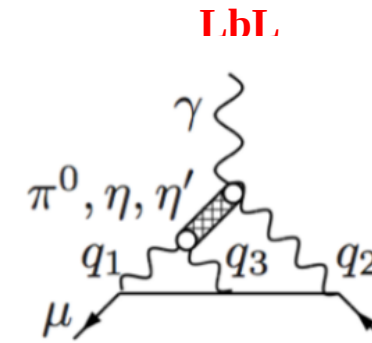
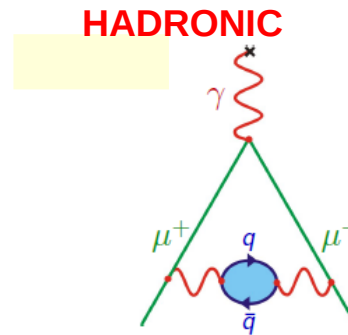
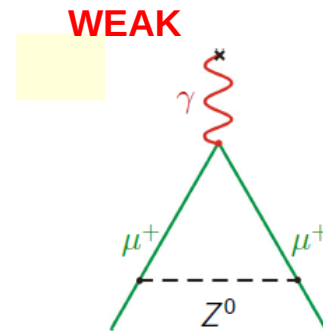
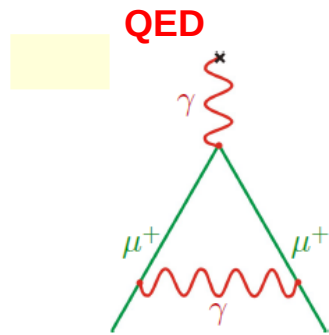
a_e tests QED to the precision of the fine structure constant α .

a_μ is more sensitive to heavy particle exchanges by a factor of $(m_\mu/m_e)^2 \sim 42,000$.

a_μ - SM calculations and experiment

Muon anomaly, $a_\mu = (g-2)_\mu/2$

$$a_\mu^{\text{theory(SM)}} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{had}}$$



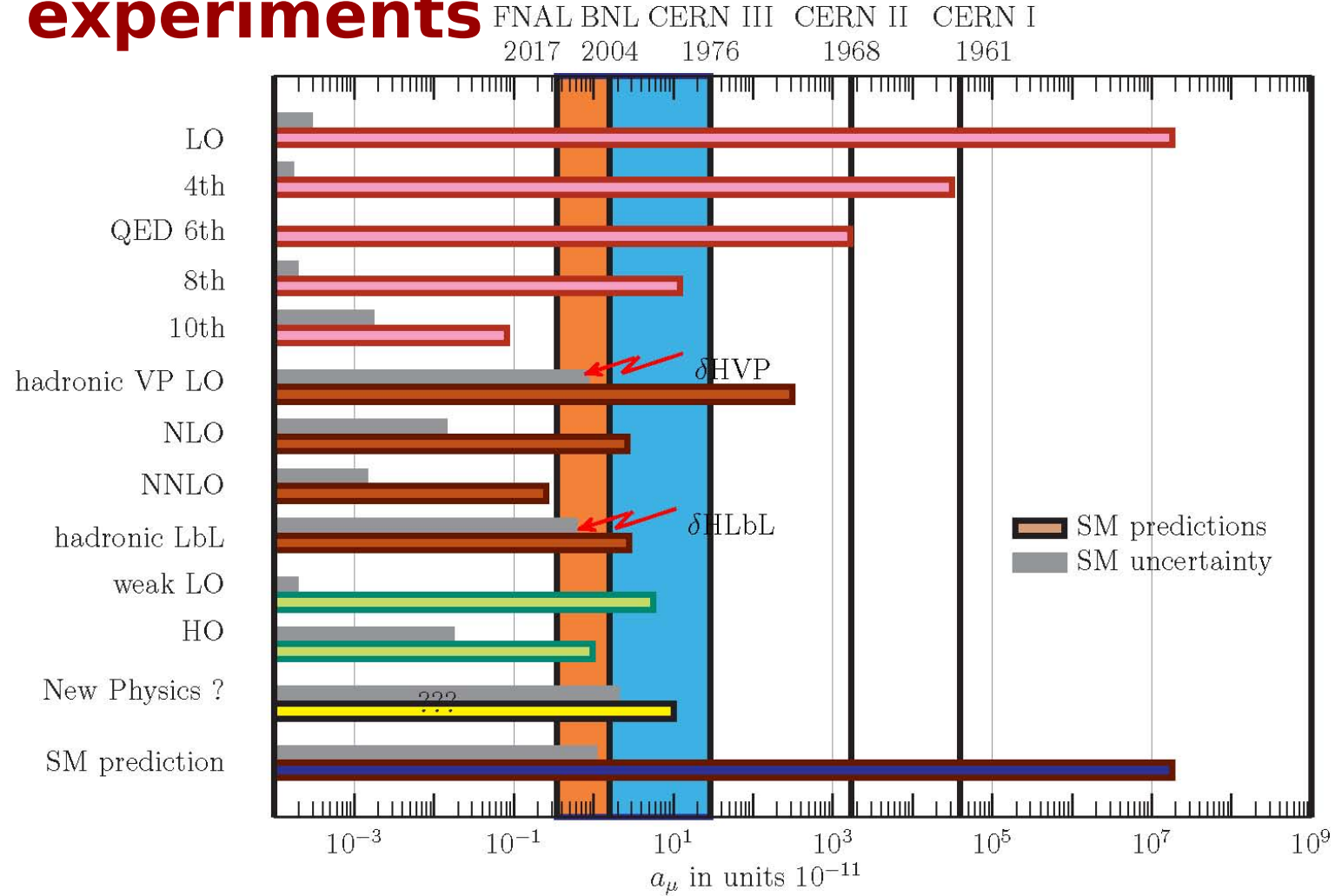
Source	Value (10^{-10})	Uncertainty (10^{-10})
QED	11 658 471.895	0.008
Weak	15.4	0.2
Hadronic + <i>LbL</i>	693.0	4.9
BNL E821	11 659 208.9	6.4
BNL – SM Theory	28.7	8.0

$$a_\mu^{\text{had}} = \frac{\alpha^2}{3 \cdot \pi^2} \int_{4m_\pi^2}^{\infty} ds \cdot \frac{K(s)}{s} \cdot R(s)$$

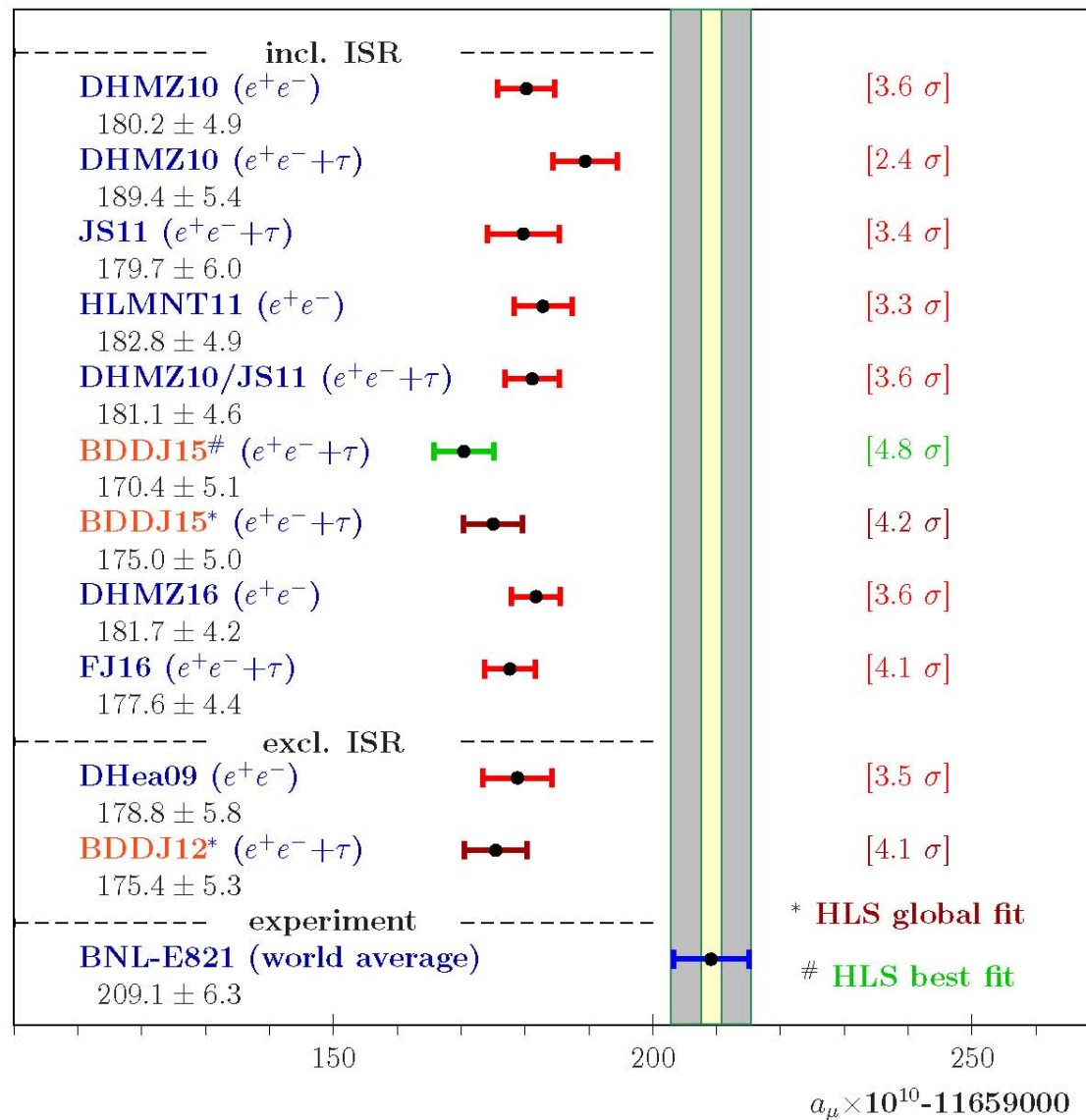
$$R(s) = \frac{\sigma(e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

$$a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = 3.6\sigma \quad (\text{M. Davier et al., EPJC71(2011)1515})$$

Past and future of muon ($g - 2$) experiments

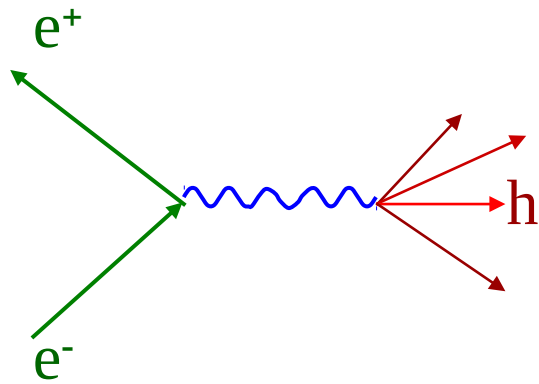


Fred Jegerlehner, arXiv:1705.00263v1 [hep-ph] 30 Apr 2017

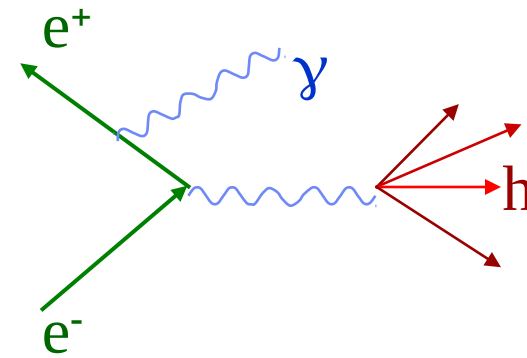


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Present data: Direct energy scan and ISR



$$E_{CM}^h = \sqrt{s}$$



$$E_{CM}^h = M_{inv}^h = \sqrt{\sqrt{s}(\sqrt{s} - 2E_\gamma)}$$

Scan: Novosibirsk – scan (CMD-2/SND at VEPP-2M, $0.36 < \sqrt{s} < 1.4$ GeV, CMD-3/SND at VEPP-2000, $2m < \sqrt{s} < 2.0$ GeV)

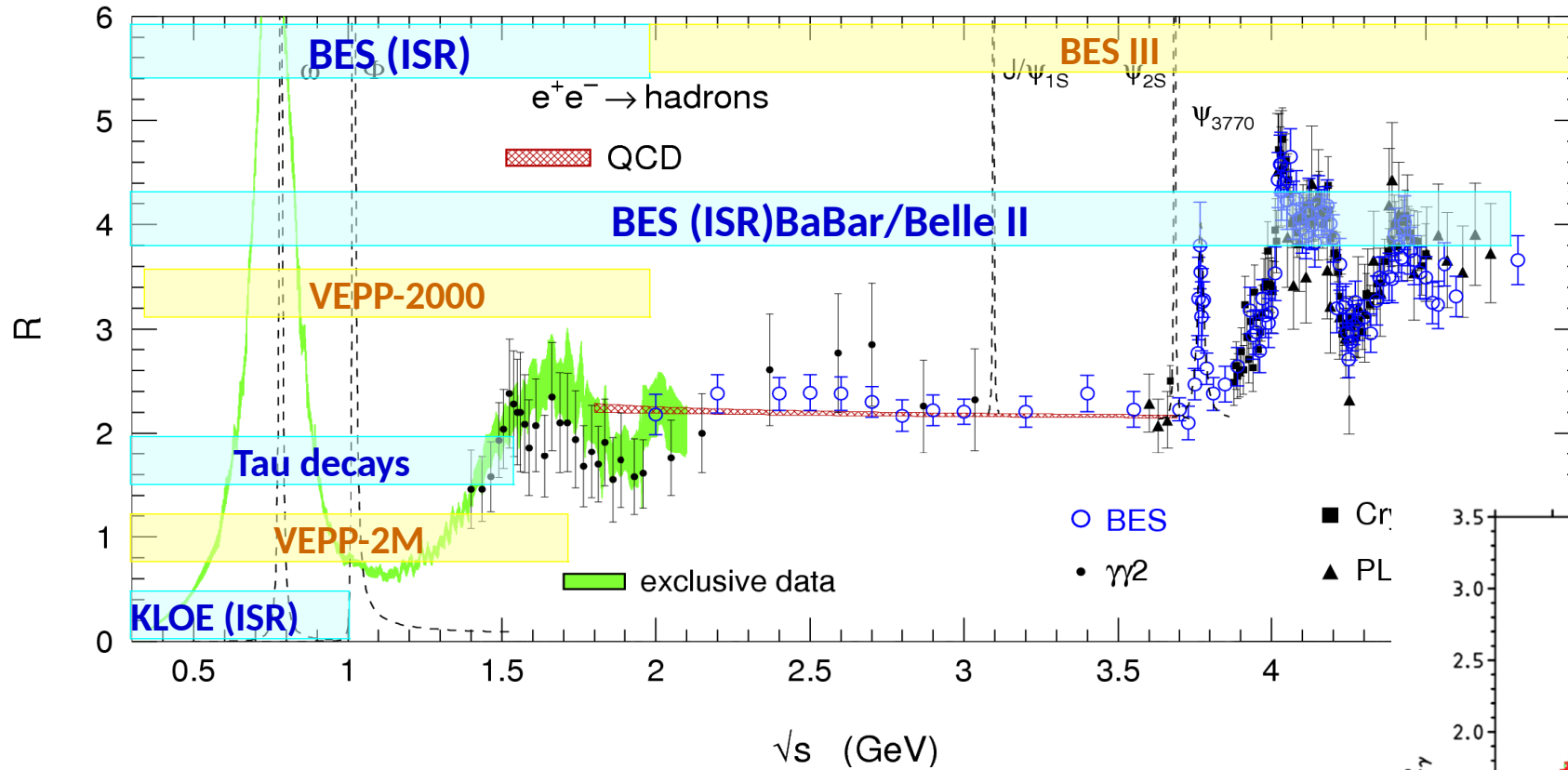
BES, BES II, BES III – Beijing 2-5 GeV

ISR: SLAC – ISR (BaBar at PEP-II, $2m < \sqrt{s} < 5$ GeV)

Frascati – ISR (KLOE/KLOE-2 at DAFNE, $2m < \sqrt{s} < 1.02$ GeV)

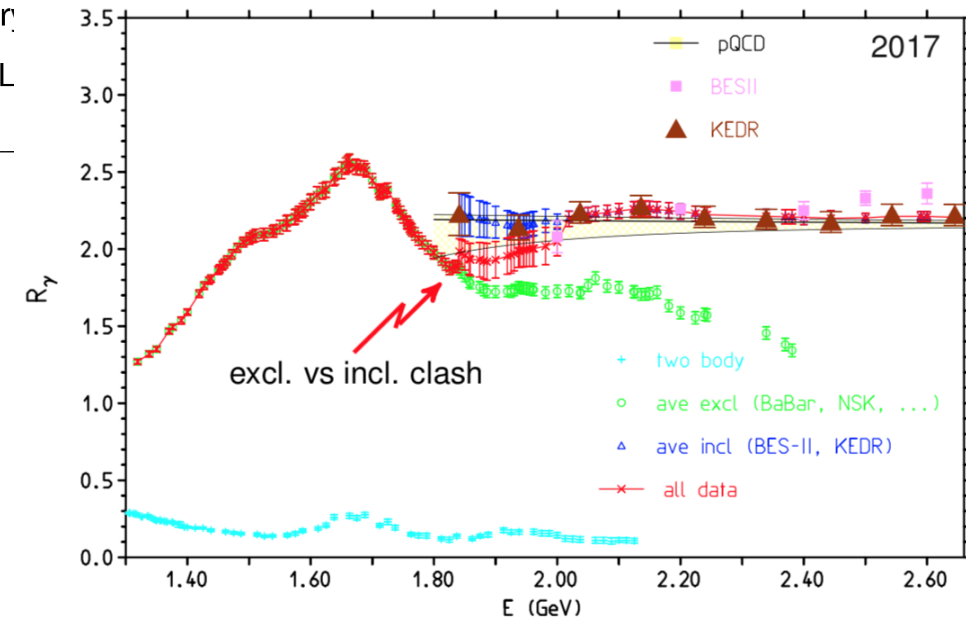
BES III

Inclusive vs exclusive measurements

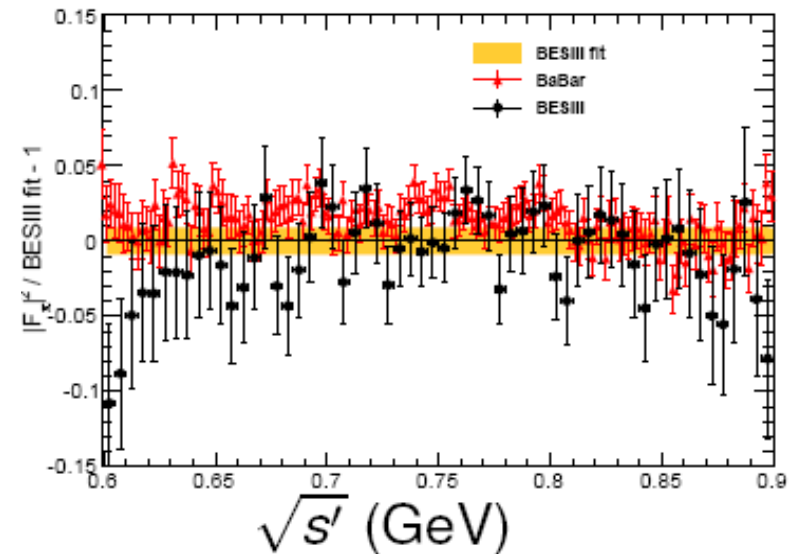
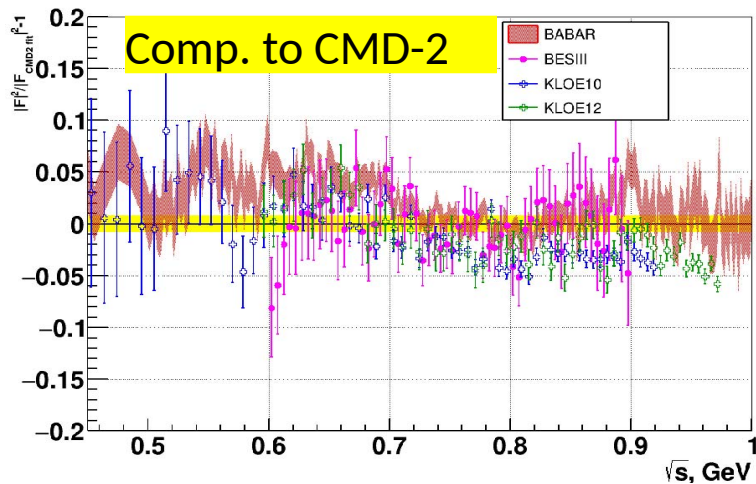
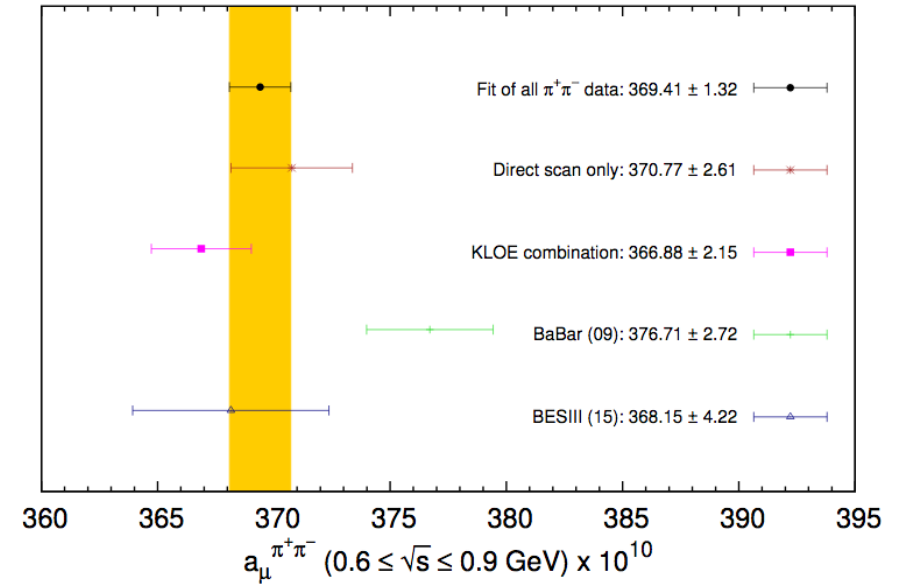
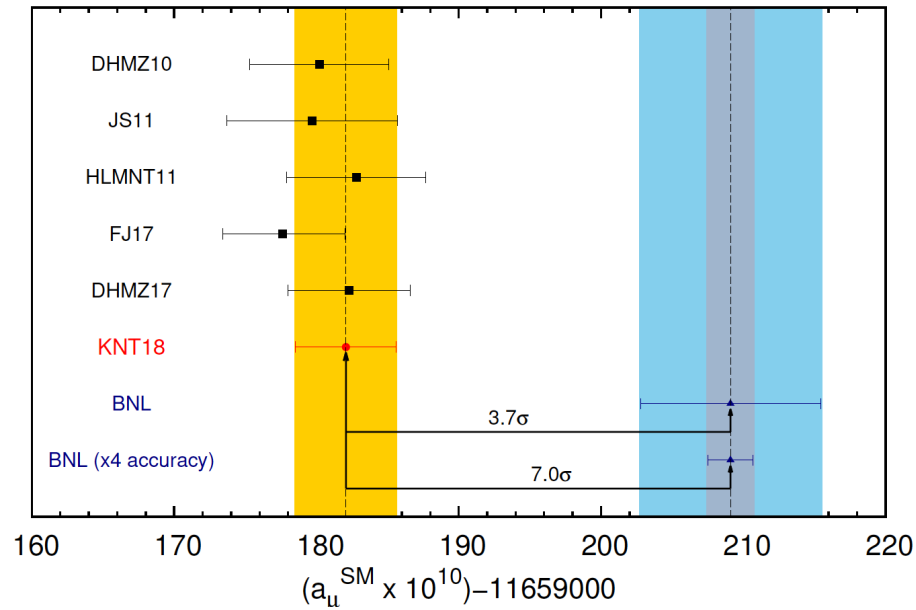


F.Jegerlehner arXiv:1804.07409

Below 2 GeV R is determined as a sum of the exclusive cross section. At higher ECM – inclusive cross section (systematics?)

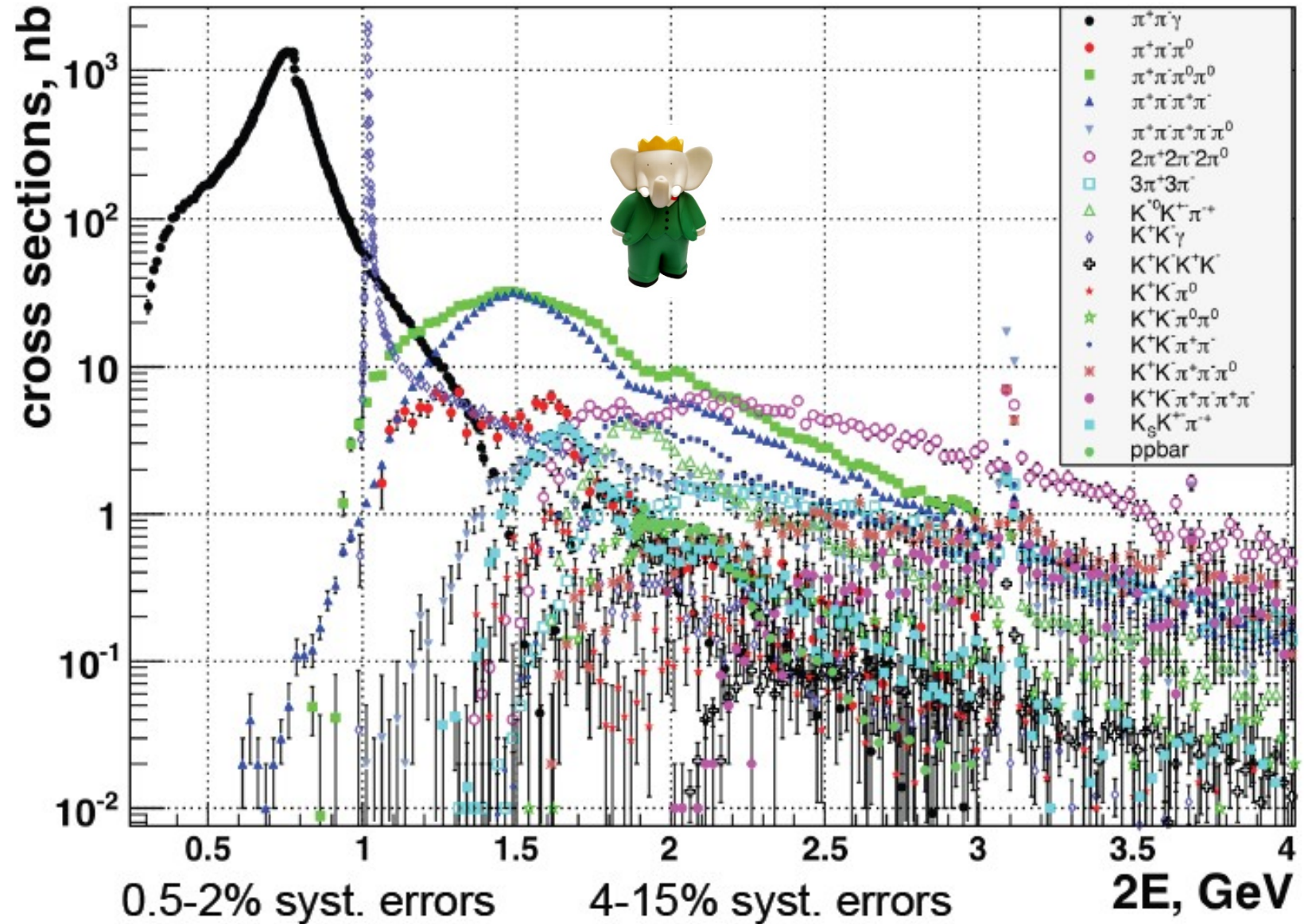


Why new more precise measurements are necessary?



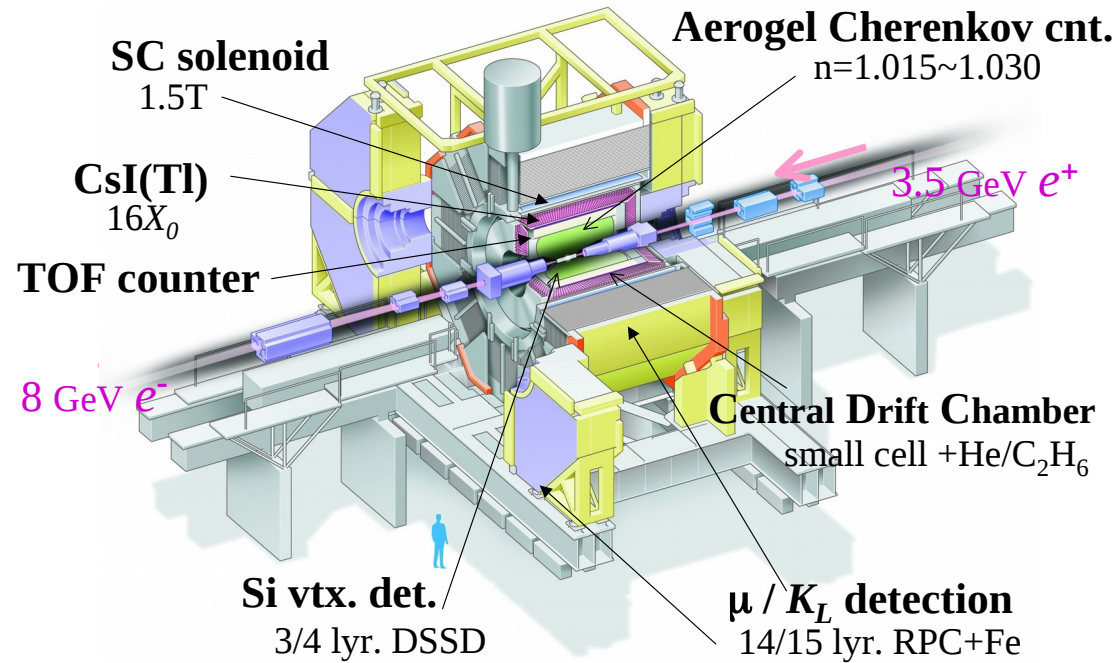
BaBar ISR analyses

22 final states were studied, ~20 papers on low energy ISR studies were published





Belle Detector



The primary goal of the Belle and BaBar experiments was to discover the CP violation in B mesons and to measure the parameters of CPV. This was achieved by both experiments in 2001

Peak lumi record at KEKB:
L=2.1 x 10³⁴/cm²/sec with crab cavities

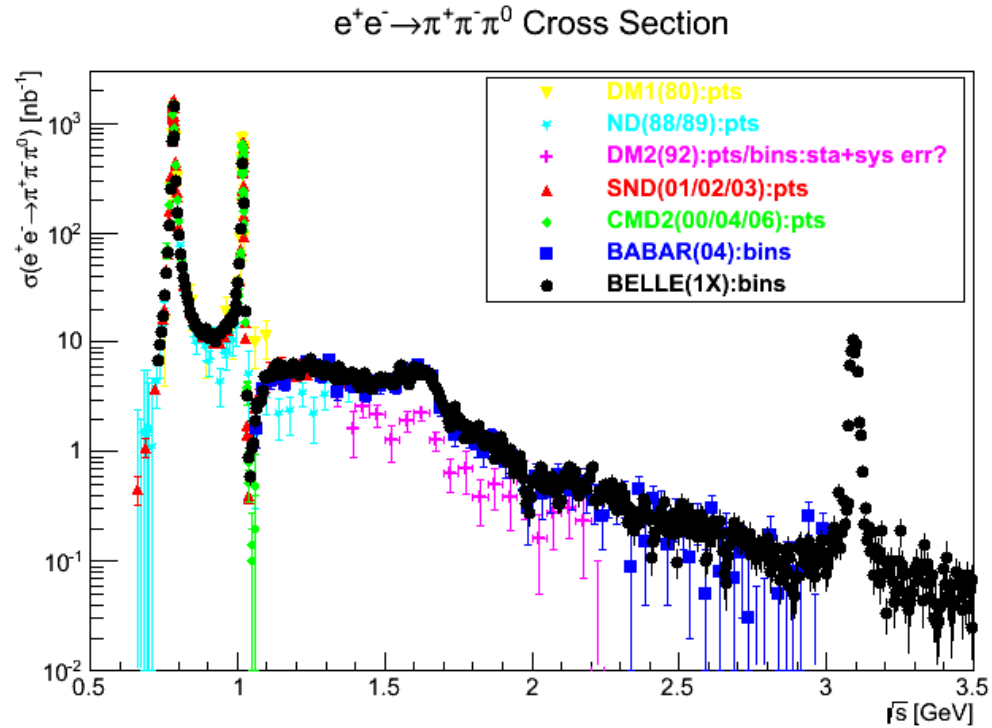
$E^- = 8 \text{ GeV}, E^+ = 3.5 \text{ GeV}, \sqrt{s} = 10.58 \text{ GeV}, \beta\gamma = 0.42$

F/B asymmetric detector

High vertex resolution, magnetic spectrometry, excellent calorimetry and sophisticated particle ID ability

$$\int_{1999}^{2010} L dt = 1 \text{ ab}^{-1}$$

Belle: low mass ISR study



526.6 fb⁻¹

**(preliminary,
suspended?)**

**Belle systematic
error goal is 5%**

**But difficult to
achieve.**

Main problems:

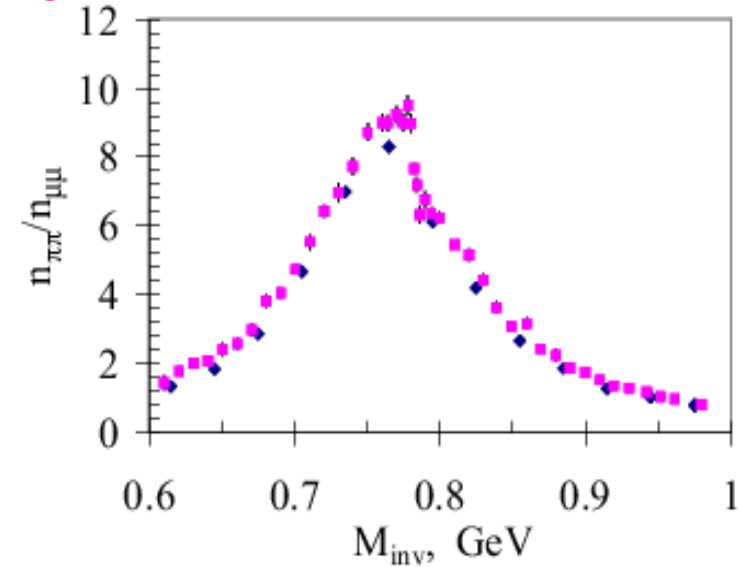
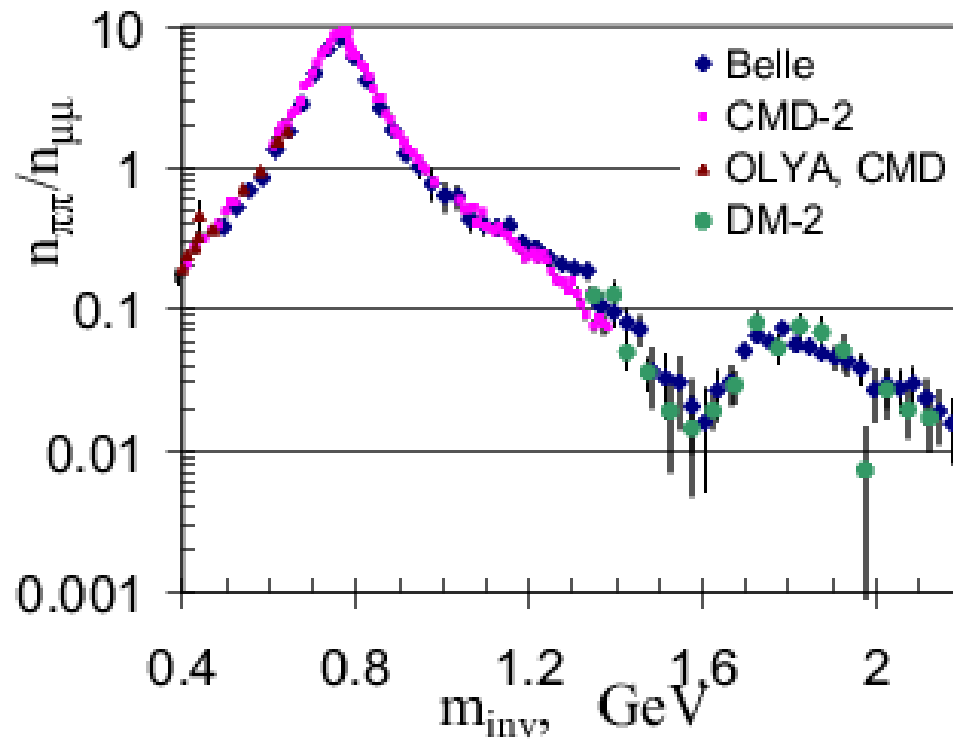
Improper trigger

Lack of manpower: 2-3 people only vs ~20 at BaBar

$N_{\pi\pi}/N_{\mu\mu}$ ratio

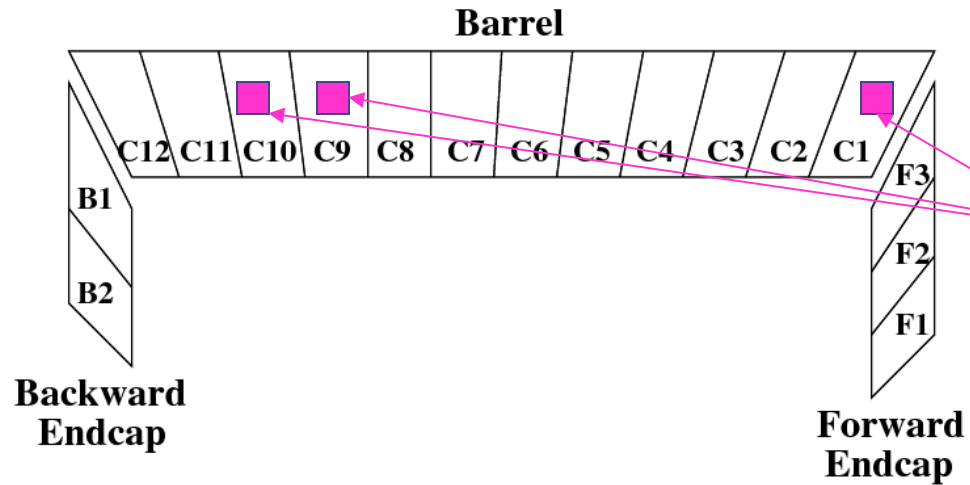
By a simple separation procedure the numbers of $\pi\pi$ and $\mu\mu$ events are obtained and ratio is calculated

(just demonstration, not for usage!)

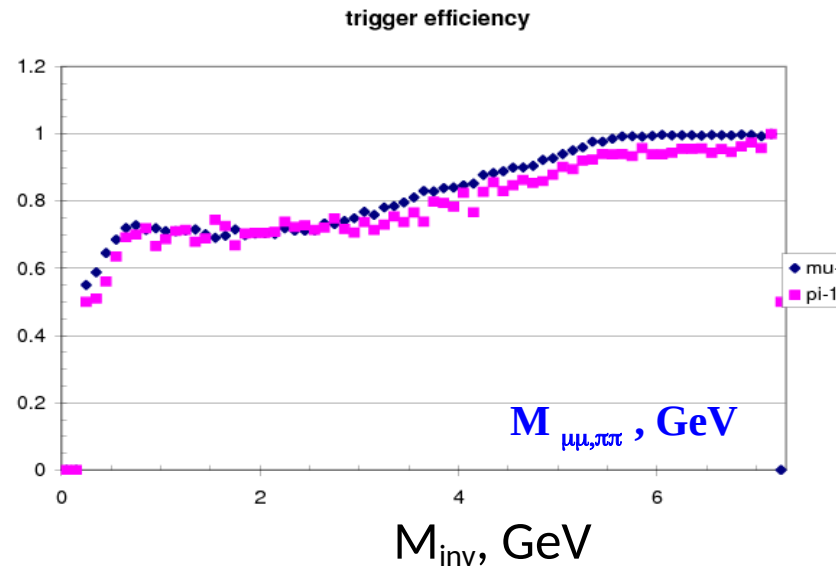


The difference $\sim 5\%$ can be caused by the different trigger efficiency for pion and muon events. This is a measure of systematics.

Bhabha veto



	Sum of rings	E_{th}, GeV
1	F1+F2+B1+B2	5
2	F2+F3+B1+B2+C11	5.5
3	F2	5
4	F3+C10+C11	5
5	C1+C9+C10	5
6	C1+C2+C9	5
7	C2+C8+C9	5
8	C3+C7+C8	5
9	C4+C6+C7	5
10	C5+C6	5
11	C10	3



Advanced Bhabha veto based on the cluster identification at the trigger level will be implemented at Belle II

Design Concept of SuperKEKB

- Increase the luminosity by **40 times** based on **"Nano-Beam" scheme**, which was first proposed for SuperB by P. Raimondi.

- Vertical β function at IP: 5.9 \rightarrow 0.27/0.30 mm (Luminosity Gain $\times 20$)
- Beam current: 1.7/1.4 \rightarrow 3.6/2.6 A ($\times 2$)
- Beam-beam parameter: .09 \rightarrow .09 ($\times 1$)

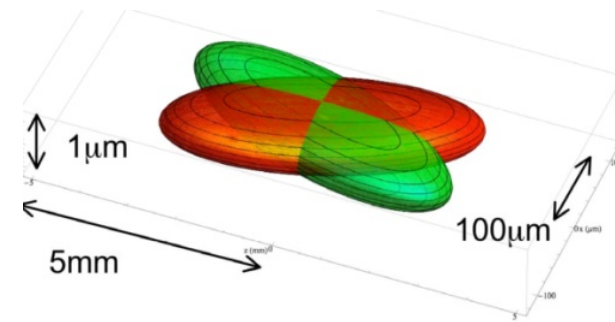
$$L = \frac{\gamma_{\pm}}{2er_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*} \left(\frac{I_{\pm} \xi_{\pm y}}{\beta_y^*} \right) \left(\frac{R_L}{R_y} \right) \right) = 8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$$

- Beam energy: 3.5/8.0 \rightarrow 4.0/7.0 GeV

LER : Longer Touschek lifetime and mitigation of emittance growth due to the intra-beam scattering

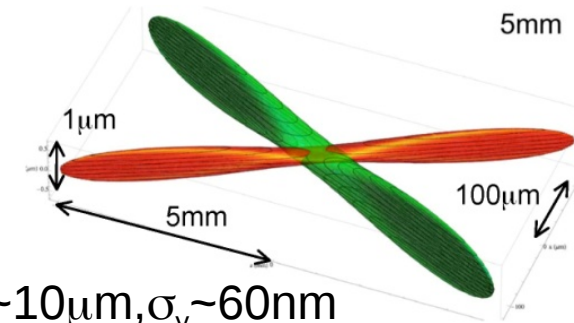
HER : Lower emittance and lower SR power

KEKB



$$\sigma_x \sim 100 \mu\text{m}, \sigma_y \sim 2 \mu\text{m}$$

Nano-Beam SuperKEKB



$$\sigma_x \sim 10 \mu\text{m}, \sigma_y \sim 60 \text{ nm}$$

	E (GeV) LER/HER	β_y^* (mm) LER/HER	β_x^* (cm) LER/HER	ϕ (mrad)	I (A) LER/HER	L ($\text{cm}^{-2}\text{s}^{-1}$)
KEKB	3.5/8.0	5.9/5.9	120/120	11	1.6/1.2	2.1×10^{34}
SuperKEKB	4.0/7.0	0.27/0.30	3.2/2.5	41.5	3.6/2.6	80×10^{34}

Belle II Detector

EM Calorimeter:

CsI(Tl), waveform sampling
electronics (barrel)
Pure CsI + waveform
sampling (end-caps) later

electrons (7GeV)

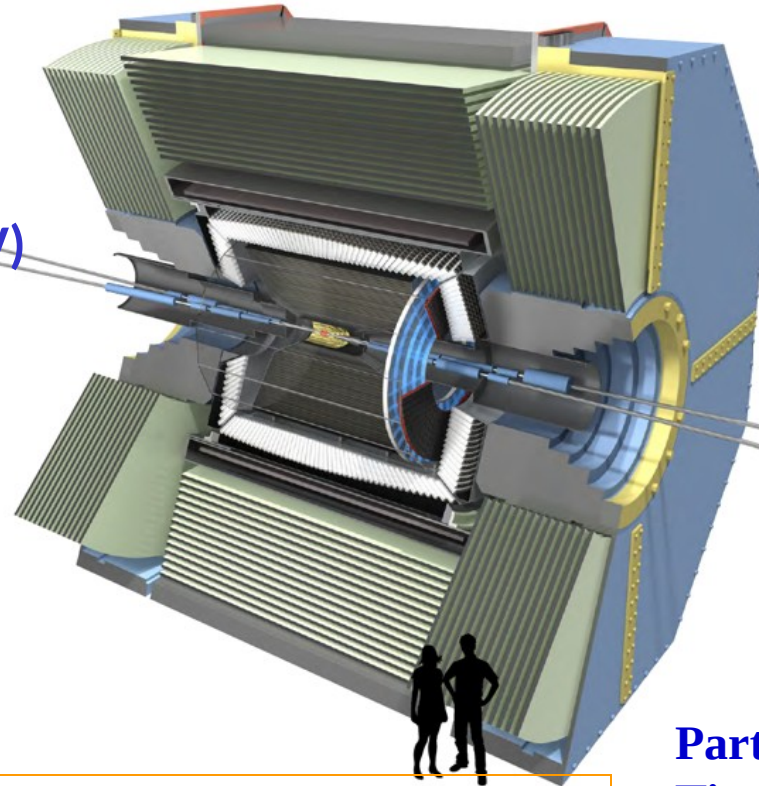
Central Drift Chamber

Smaller cell size, long lever
arm

Vertex Detector

2 layers Si Pixels (DEPFET) +
4 layers Si double sided strip
DSSD

+ New software, improved tracking, ...
+ Optimization for low multiplicity trigger
+ Improved simulation, generators and GRID



KL and muon detector:

Resistive Plate Counter
(barrel outer layers)
Scintillator + WLSF + MPPC
(end-caps, inner 2
barrel layers)

positrons (4GeV)

Particle Identification

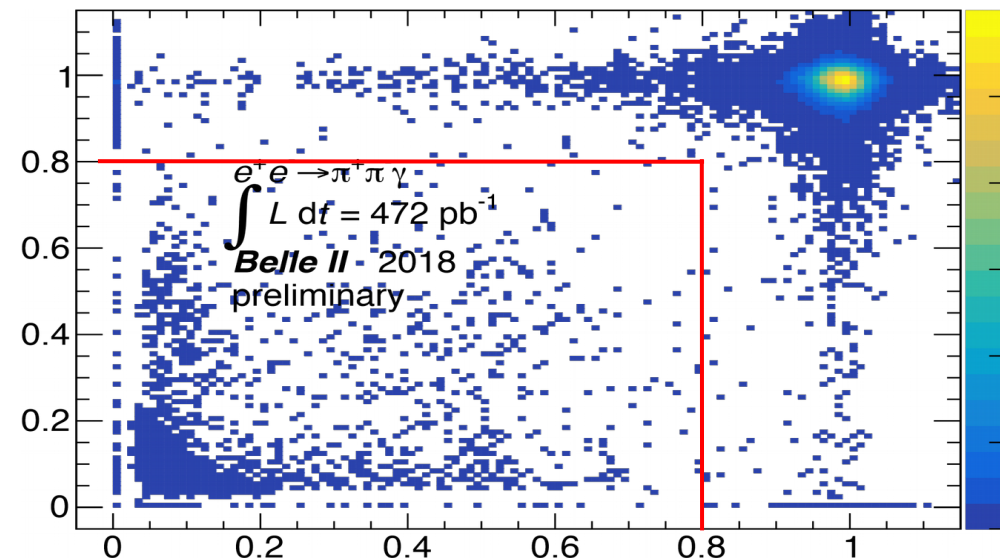
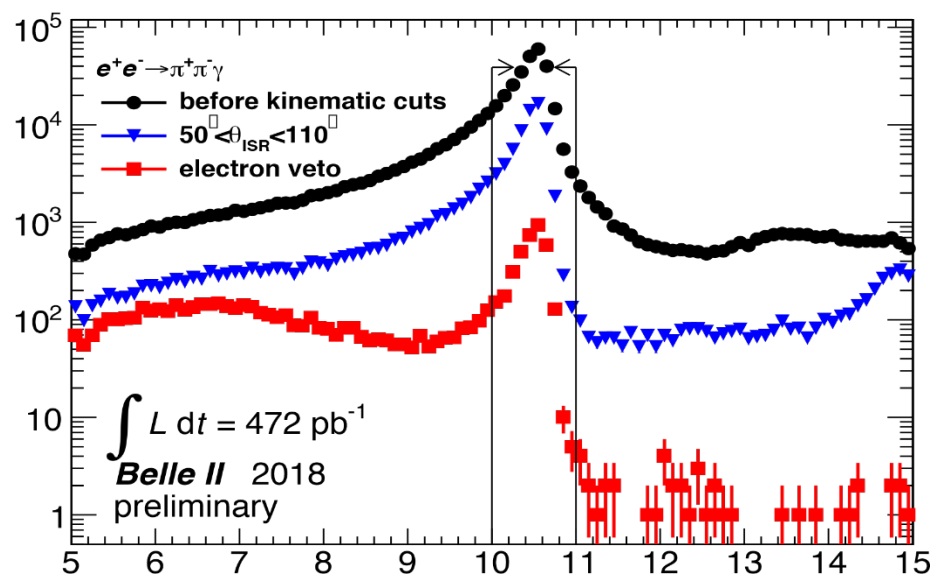
Time-of-Propagation
counter (barrel)
Prox. focusing Aerogel
RICH (forward)

Belle II first look to ISR (Phase II)

Events with one photon
($E_\gamma > 3$ GeV, $50 < \theta < 110$)
and 2 tracks from IP were
selected and $10 < E_{\text{tot}} < 11$
GeV.

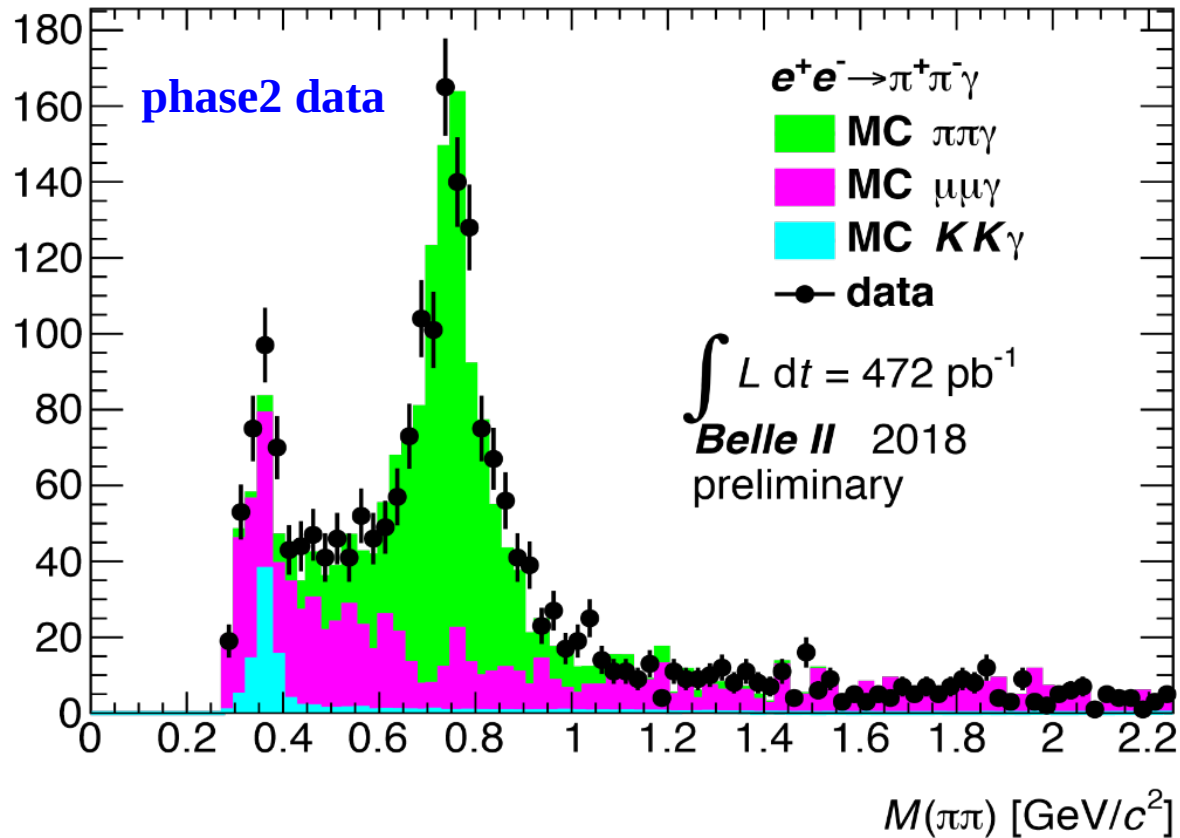
Analysis done by Y.Maeda

E/p ratio for
each of
positive and
negative
charged tracks.



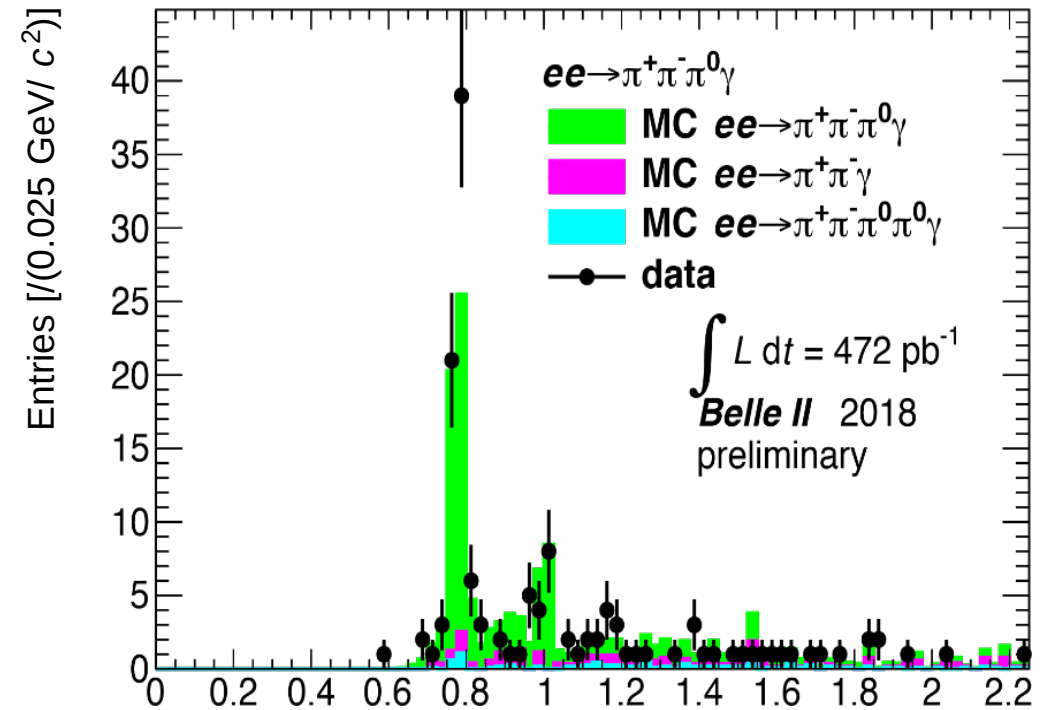
full data of 472 pb-1 was used

$\pi\pi$ mass spectrum



MC cross sections are taken from the Phokhara generator output, $\text{data}/\text{MC}(\pi\pi) = 1.065 \pm 0.037(\text{stat})$

$\pi\pi\pi\gamma$ process with phase-2 data



Influence of the Bhabha veto

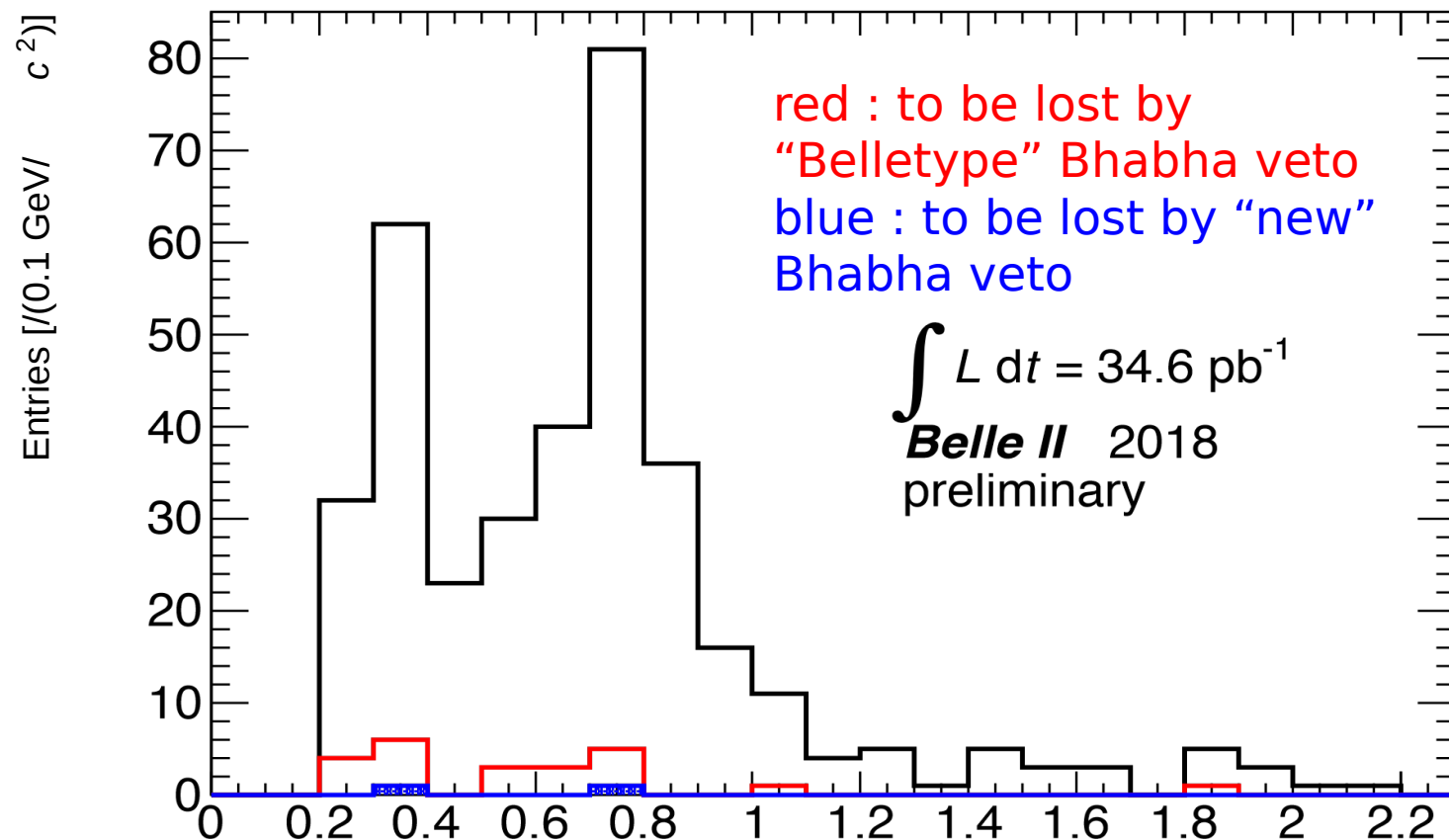
Two kinds of Bhabha veto logic:

1. Modified “Belle-type” Bhabha veto
2. Clusterized “new” Bhabha veto

1.: $(6.4 \pm 1.3_{\text{stat}})\%$

2.: $(0.6 \pm 0.4_{\text{stat}})\%$

the “new” Bhabha veto logic is feasible for future runs



Conclusion

- At present the discrepancy between experiment and SM in the muon ($g-2$) is, probably, the largest among observed.
- Two experiments on muon ($g-2$) measurement are in progress. We anticipate 3-4 times better precision in several years.
- Measurement of $e^+e^- \rightarrow \pi^+\pi^-$ cross section in Belle II with ISR method is critical to reduce uncertainty of theoretical value for muon ($g-2$)
- Analysis of the Phase 2 data provided the $e^+e^- \rightarrow \pi^+\pi^-$ and $\pi^+\pi^-\pi^0$ in a good agreement with MC simulation
- It was found that the new trigger logic provides high efficiency and low loss of the ISR event caused by the Bhabha veto
- New and more precise experimental data on the hadronic cross-sections are been waiting from Belle II in the Phase 2.