

Inclusive $B \rightarrow X_u l \nu$ at Belle II

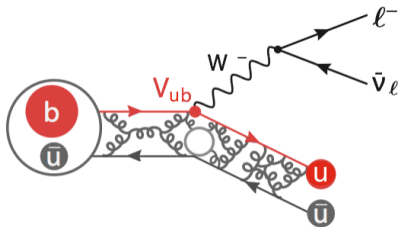
Raynette van Tonder,
on behalf of the Belle II Collaboration

Karlsruhe Institute of Technology

10th International Workshop on the CKM Unitarity Triangle
18 September 2018



$$B \rightarrow X_u l \bar{\nu} \text{ and } |V_{ub}|$$



- $|V_{ub}| = \sqrt{\frac{\Delta\mathcal{B}}{\tau_B \Delta\Gamma}}$

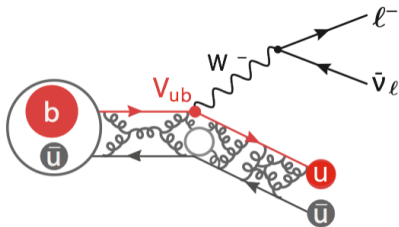
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- $\bar{B} \rightarrow \pi l \bar{\nu}$
- Needs input from non-perturbative methods, i.e. lattice QCD.

Inclusive V_{ub}

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- Total decay rate determined from the Heavy Quark Expansion (HQE).

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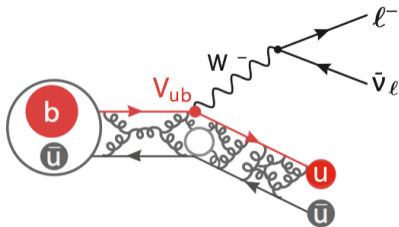
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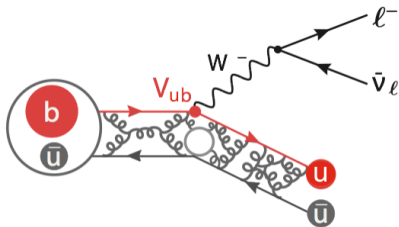
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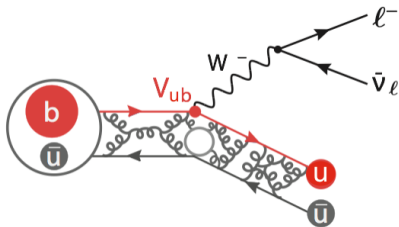
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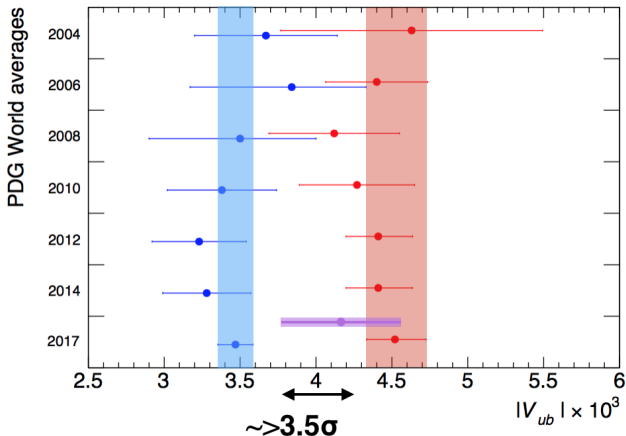
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Current status



Exclusive

$$\bar{B} \rightarrow \pi l \bar{\nu}, \bar{B} \rightarrow D^* l \bar{\nu},$$
$$\Lambda_b \rightarrow p \mu \nu_\mu$$

Inclusive

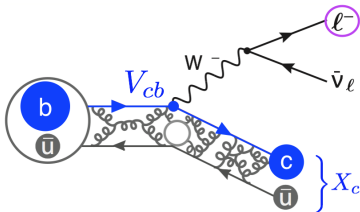
$$\bar{B} \rightarrow X_u l \bar{\nu}$$

Leptonic

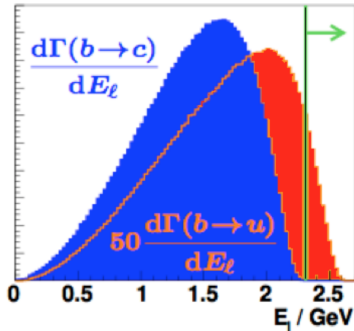
$$\bar{B} \rightarrow \tau \nu_\tau$$

Why is it hard to measure V_{ub} ?

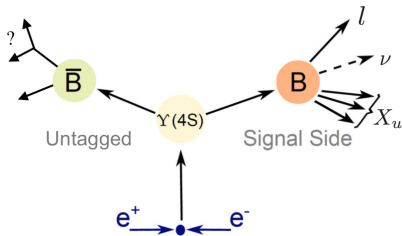
Dominant background: $\bar{B} \rightarrow X_c l \nu$



$\rightarrow \mathcal{O}(100)$ times more abundant than signal!

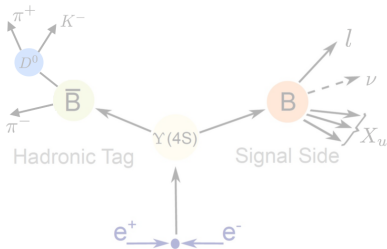


Analysis strategy



Inclusive tagging

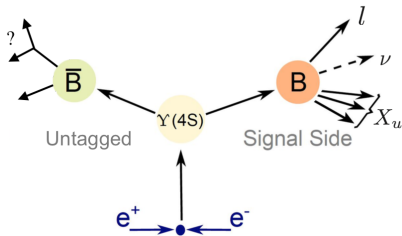
- Use the initial event information and the reconstructed visible momenta to constrain the neutrino momentum.



Hadronic tagging

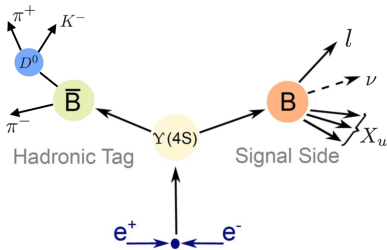
- Use the information from the B-tag side to reconstruct the neutrino momentum.
- Low efficiency, but high purity.

Analysis strategy



Inclusive tagging

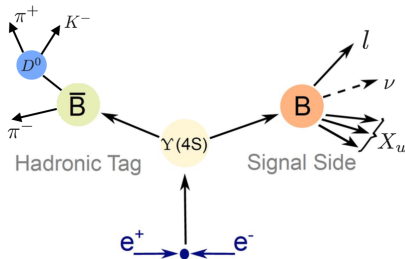
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Hadronic tagging

- Use the information from the B-tag side to reconstruct the neutrino momentum.
- Low efficiency, but high purity.

Typical selection



Signal lepton

Select one lepton with $p_{l^*} > 1$ GeV.

Missing mass

$$MM^2 = m_\nu^2 =$$
$$p_\nu^2 = (p_{\Upsilon(4S)} - p_{B_{tag}} - p_X - p_l)^2$$

$B \rightarrow D^* l \nu$ vetoes

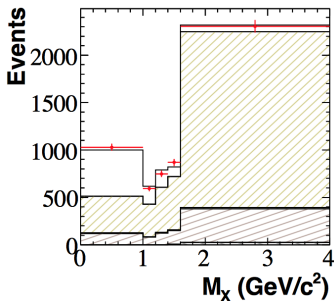
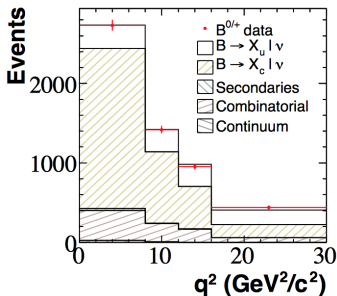
- Partially reconstruct D^* with slow pions.
- $E_{D^*} \approx m_{D^*} \times E_\pi / \Delta m$
- $MM_{veto}^2 =$
 $(p_{B_{sig}} - p_{D^*} - p_l)^2$

Alternative: separation with MVA

Most recent Belle analysis

- Separates $B \rightarrow X_u l \nu$ from $B \rightarrow X_c l \nu$ with Boosted Decision Trees.
- Makes use of 17 different kinematic variables as feature inputs.
- Accesses $\approx 90\%$ of the $B \rightarrow X_u l \nu$ phase space!
- Minimises shape function dependence.

Phys. Rev. Lett. 104.2, 021801
(2010)



A look at systematics

Source	Error on \mathcal{B} (irreducible limit)
$\mathcal{B}(D^{(*)}\ell\nu)$	1.2 (0.6)
Form factors ($D^{(*)}\ell\nu$)	1.2 (0.6)
Form factors & $\mathcal{B}(D^{(**)}\ell\nu)$	0.2
$B \rightarrow X_u\ell\nu$ (SF)	3.6 (1.8)
$B \rightarrow X_u\ell\nu(g \rightarrow s\bar{s})$	1.5
$\mathcal{B}(B \rightarrow \pi/\rho/\omega\ell\nu)$	2.3
$\mathcal{B}(B \rightarrow \eta^{(\prime)}\ell\nu)$	3.2
$\mathcal{B}(B \rightarrow X_u\ell\nu)$ unmeasured/fragmentation	2.9 (1.5)
Continuum & Combinatorial	1.8
Secondaries, Fakes & Fit	1.0
PID& Reconstruction	3.1
BDT/Normalisation	3.1 (2.0)
Total	8.1
(Total reducible)	7.4
(Total irreducible)	3.2

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Inclusive MC modelling

MC hybrid mix

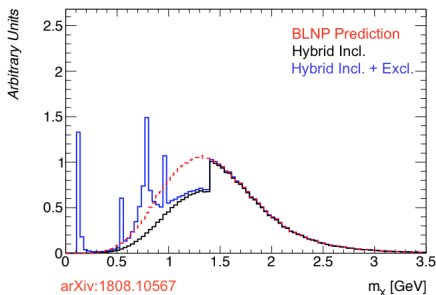
- Consists of inclusive and resonant contributions.

Room for improvement:

- Resonant contributions ($X_u = \pi, \rho, \eta, \omega$) only account for 20% of the total rate.

Belle II to the rescue!

- Larger data set will aid to constrain uncertainties on signal modelling.

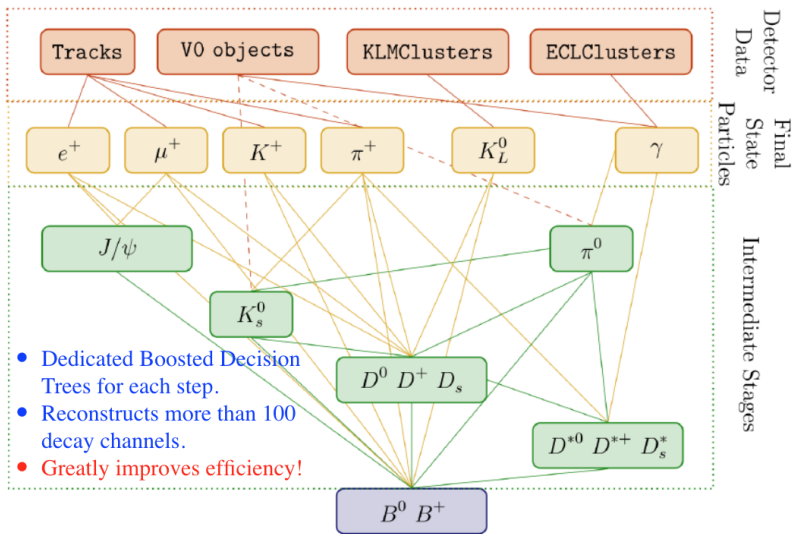


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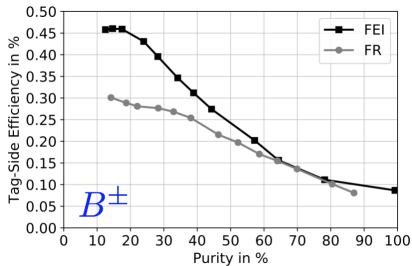
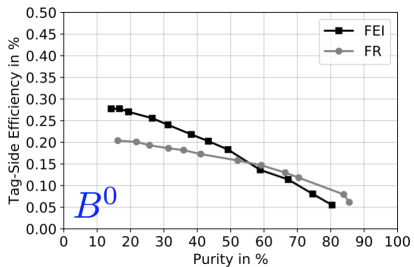
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Introducing the Full Event Interpretation!

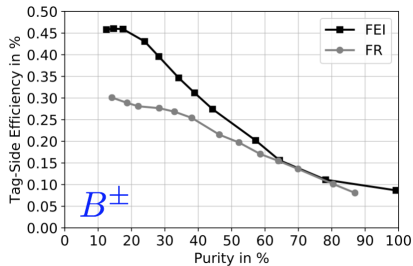
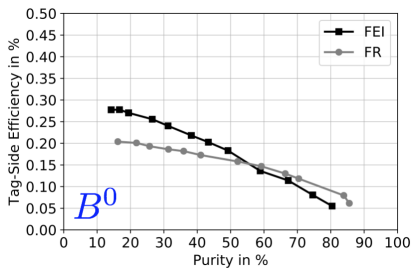


Estimated improved hadronic tagging



	Method	Efficiency	Purity
Belle	Cut-based	0.1%	0.25%
Belle FR	Neurobayes	0.2%	0.25%
Belle II FEI	BDTs	0.5%	0.25%

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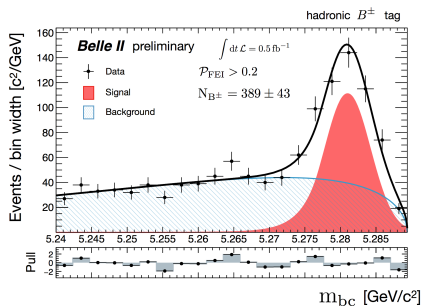
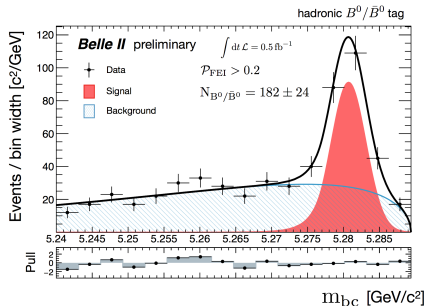


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Belle FR	Neurobayes	0.2%	0.25%
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Phase II FEI performance

Phase II at Belle II

- Commissioning run from Feb 2018 to July 2018.
- First e^+e^- collisions during April 2018.

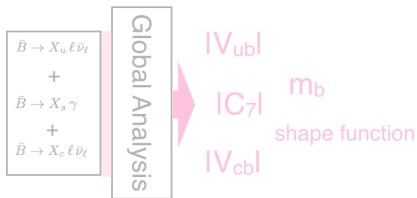


- $N = 182 \pm 24$ neutral and $N = 389 \pm 43$ charged candidates.

Expected performance at Belle II

Approximate shape function

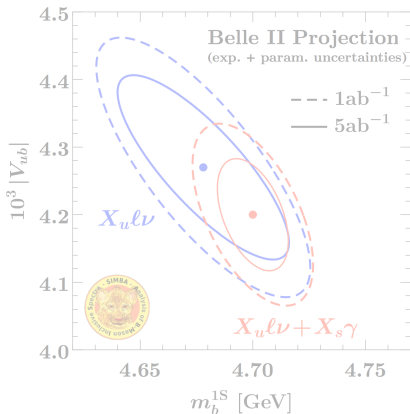
$$\hat{F}(p_b) = (\sum_n c_n f_n(p_b))^2$$



Relative error: 2-3%

As done by:

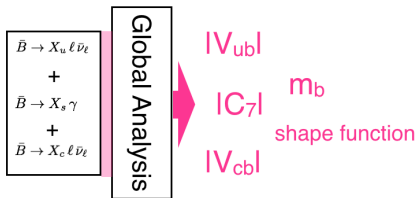
SIMBA & NN V_{ub}



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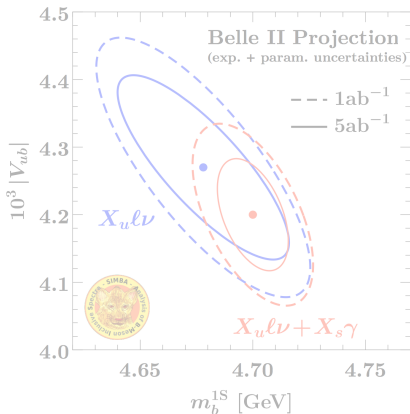
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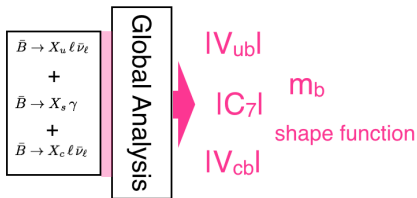
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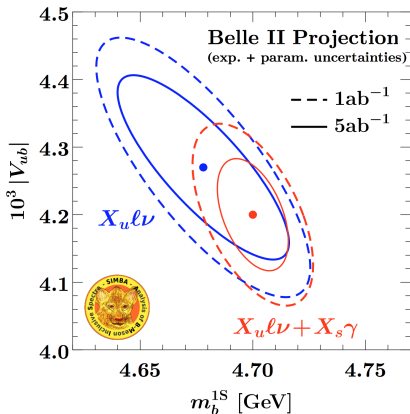
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Relative error: 2-3%

As done by:

SIMBA & NN V_{ub}



Summary

Measuring $|V_{ub}|$ is crucial to the current exclusive vs. inclusive problem.

Difficult to measure in tiny pockets of phase space where background is suppressed, which then become sensitive to the shape function.

Precision of measurements can be improved at the Belle II experiment with much higher luminosity, better and smarter reconstruction algorithms and state-of-the-art theory models.

Additionally, global data-driven fits would yield a model independent measurement of $|V_{ub}|$, which improve precision of measurements by reducing model uncertainties from the shape function.

Back up!

Very specific numbers for finicky questions

	Statistical	Systematic (reducible, irreducible)	Total Exp	Theory	Total
<hr/>					
$ V_{ub} $ exclusive (had. tagged)					
711 fb ⁻¹	3.0	(2.3, 1.0)	3.8	7.0	8.0
5 ab ⁻¹	1.1	(0.9, 1.0)	1.8	1.7	3.2
50 ab ⁻¹	0.4	(0.3, 1.0)	1.2	0.9	1.7
<hr/>					
$ V_{ub} $ exclusive (untagged)					
605 fb ⁻¹	1.4	(2.1, 0.8)	2.7	7.0	7.5
5 ab ⁻¹	1.0	(0.8, 0.8)	1.2	1.7	2.1
50 ab ⁻¹	0.3	(0.3, 0.8)	0.9	0.9	1.3
<hr/>					
$ V_{ub} $ inclusive					
605 fb ⁻¹ (old B tag)	4.5	(3.7, 1.6)	6.0	2.5–4.5	6.5–7.5
5 ab ⁻¹	1.1	(1.3, 1.6)	2.3	2.5–4.5	3.4–5.1
50 ab ⁻¹	0.4	(0.4, 1.6)	1.7	2.5–4.5	3.0–4.8
<hr/>					
$ V_{ub} B \rightarrow \tau\nu$ (had. tagged)					
711 fb ⁻¹	18.0	(7.1, 2.2)	19.5	2.5	19.6
5 ab ⁻¹	6.5	(2.7, 2.2)	7.3	1.5	7.5
50 ab ⁻¹	2.1	(0.8, 2.2)	3.1	1.0	3.2
<hr/>					
$ V_{ub} B \rightarrow \tau\nu$ (SL tagged)					
711 fb ⁻¹	11.3	(10.4, 1.9)	15.4	2.5	15.6
5 ab ⁻¹	4.2	(4.4, 1.9)	6.1	1.5	6.3
50 ab ⁻¹	1.3	(2.3, 1.9)	2.6	1.0	2.8