



NEW SEMILEPTONIC $B \rightarrow X_{c/u} l \nu$ RESULTS AT $e^+ e^-$ EXPERIMENTS

Svenja Granderath (University of Bonn)

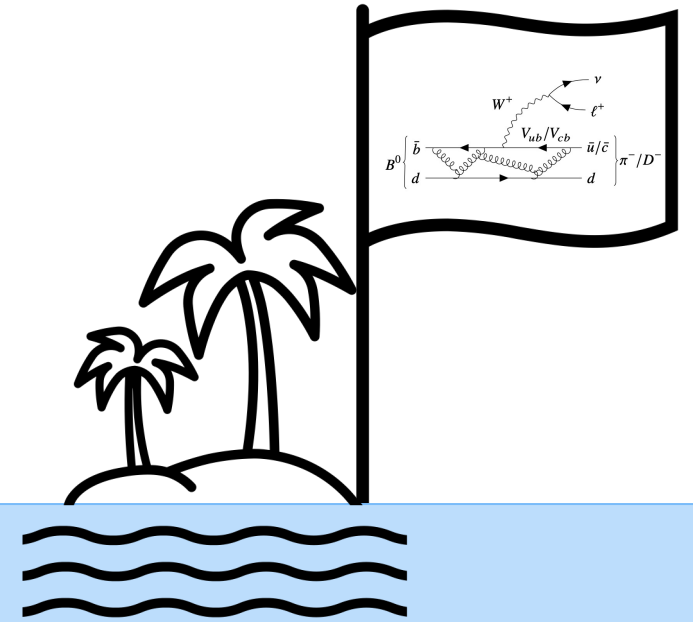
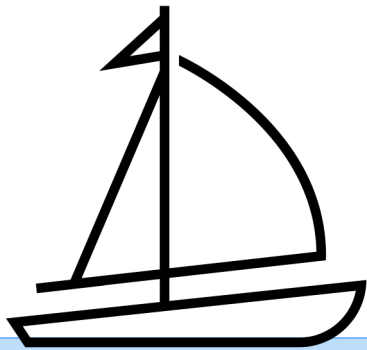
on behalf of the Belle II collaboration

(with material from the Belle collaboration)

FPCP 2023 - Lyon - May 29, 2023

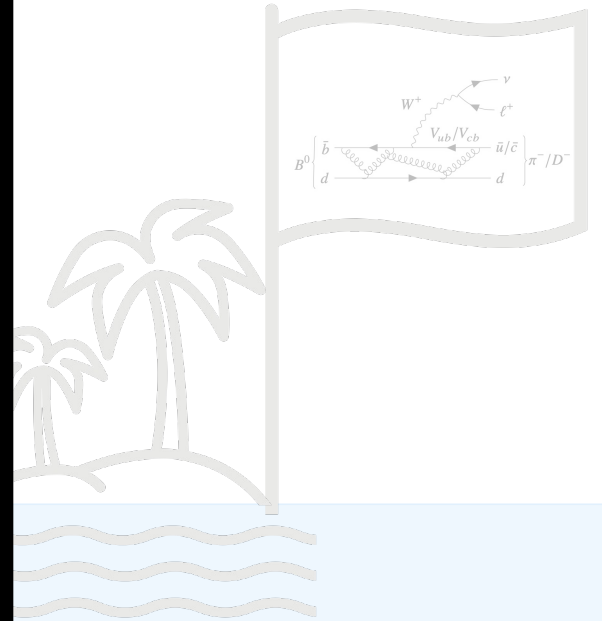
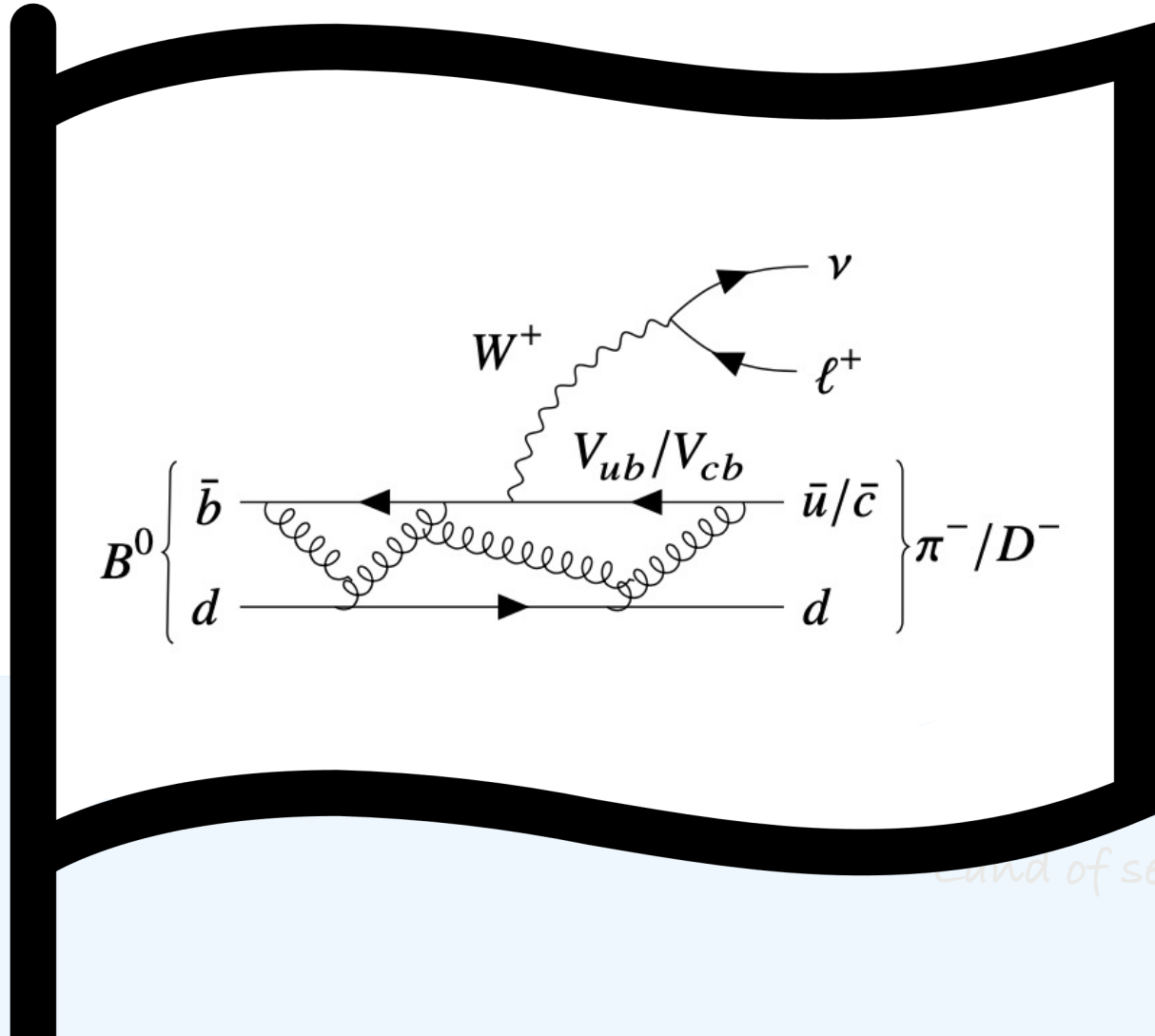


SEMILEPTONIC B DECAYS



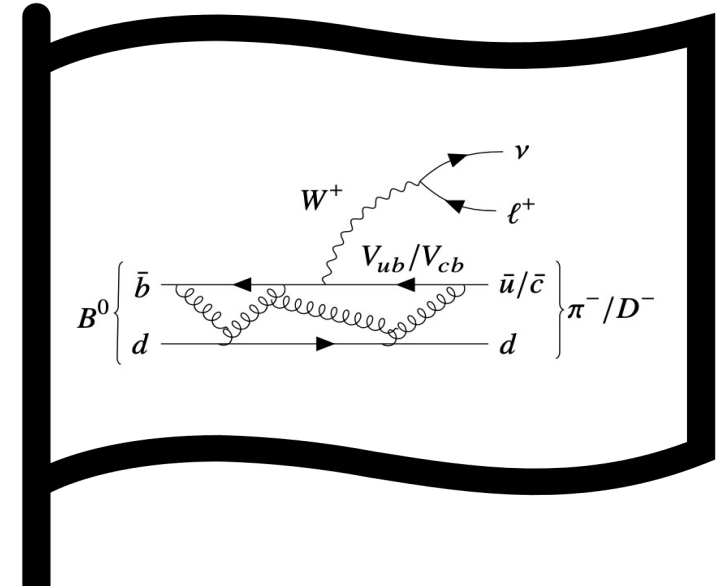
Land of semileptonic B decays

SEMILEPTONIC B DECAYS



and of semileptonic B decays

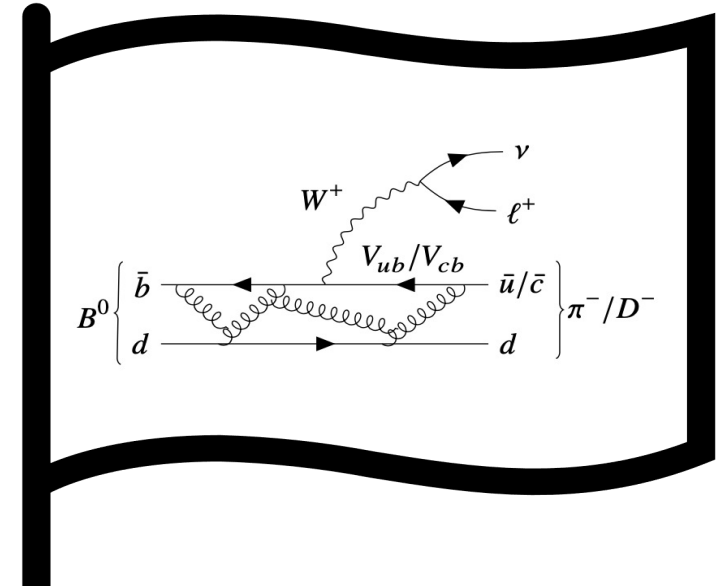
SEMILEPTONIC B DECAYS



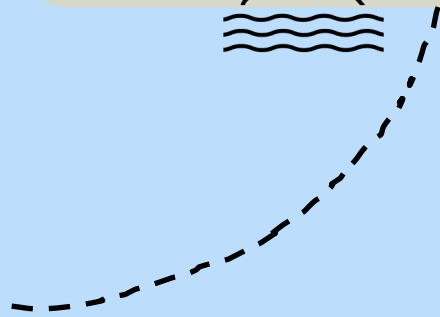
SEMILEPTONIC B DECAYS

$$\underbrace{\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}}_{\text{CKM Matrix}}$$

Form-factor
measurements



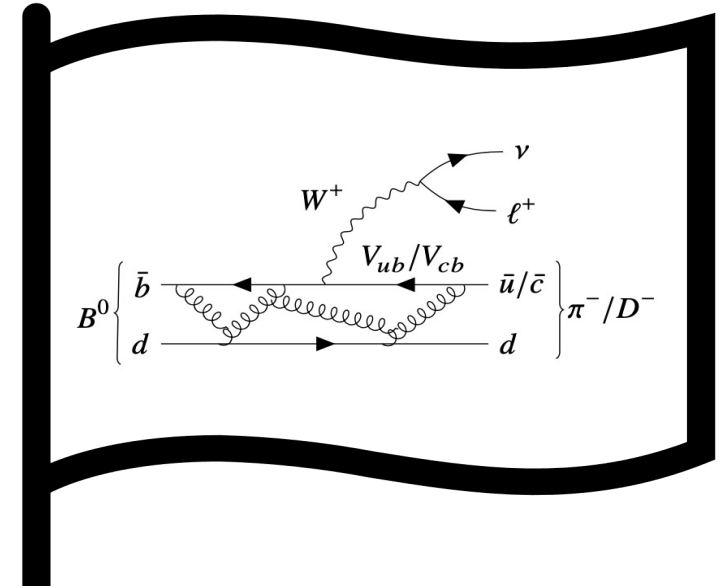
SM precision
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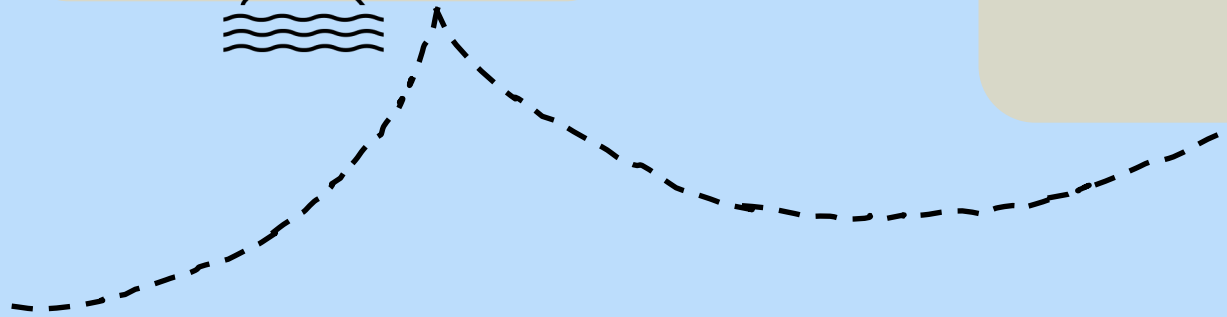


Lepton universality
(LU) tests



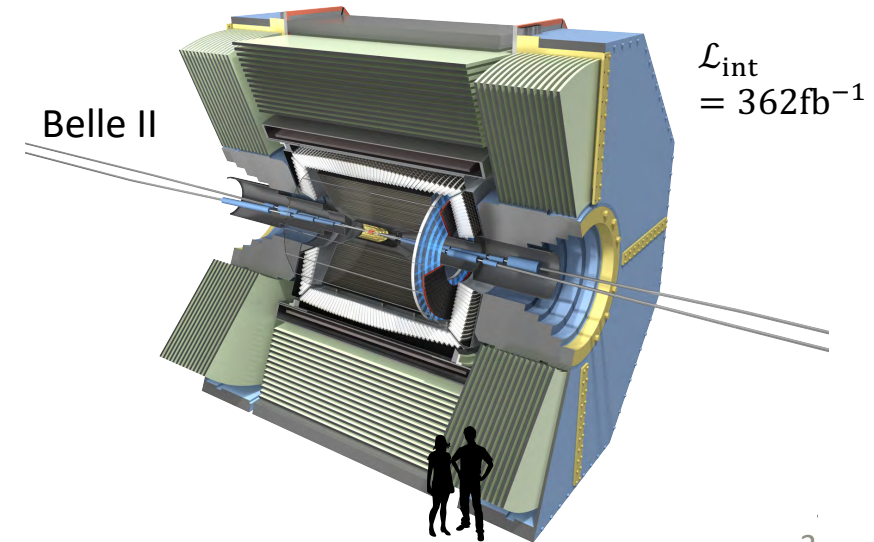
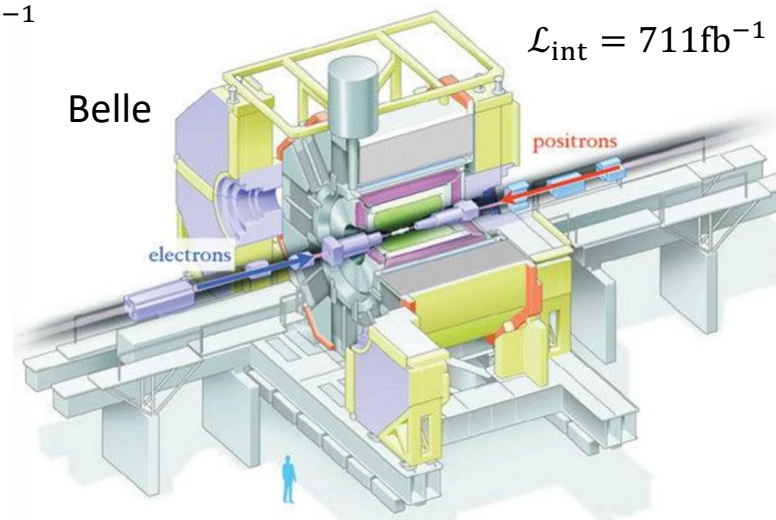
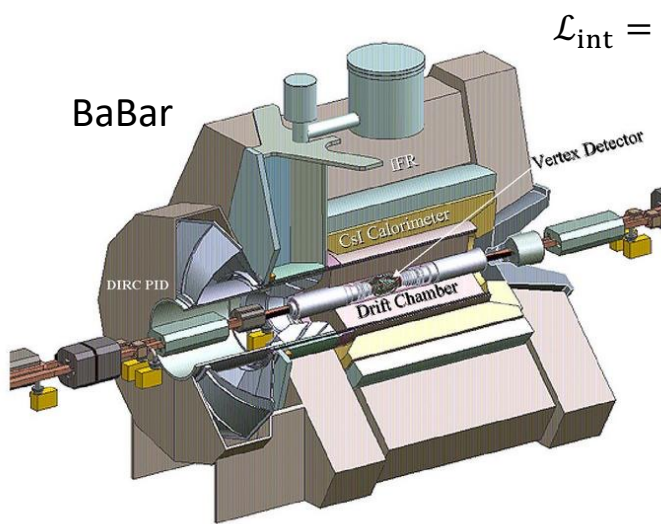
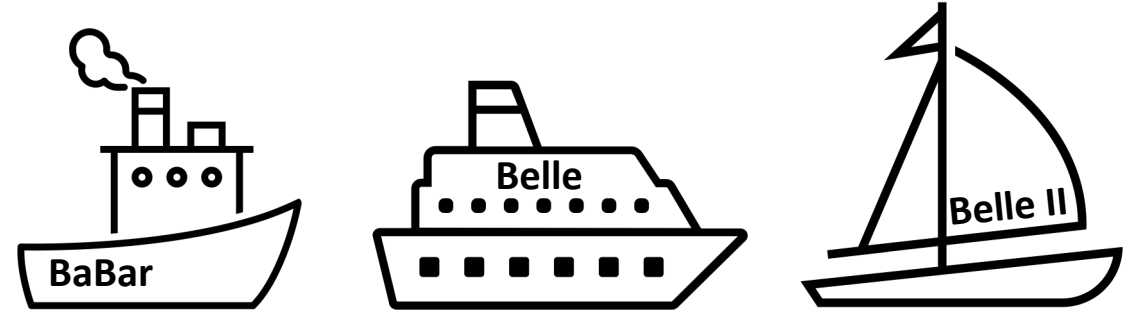
Angular
observables

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} l \nu)}$$



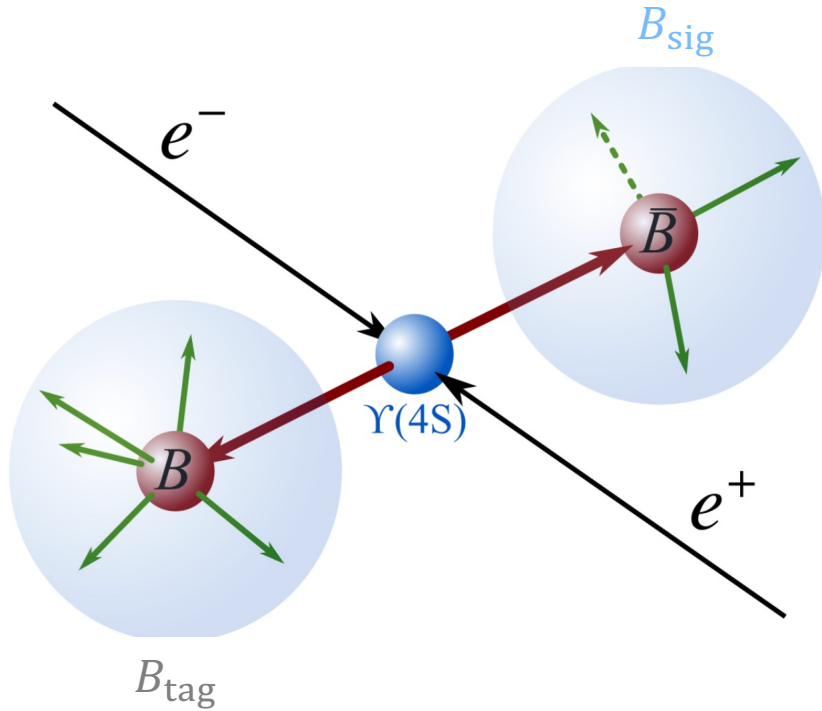
B-FACTORY EXPERIMENTS

- BaBar, Belle and Belle II
- Detectors located at the interaction points of electron-positron colliders
- Center-of-mass energy corresponding to $\Upsilon(4S)$ resonance



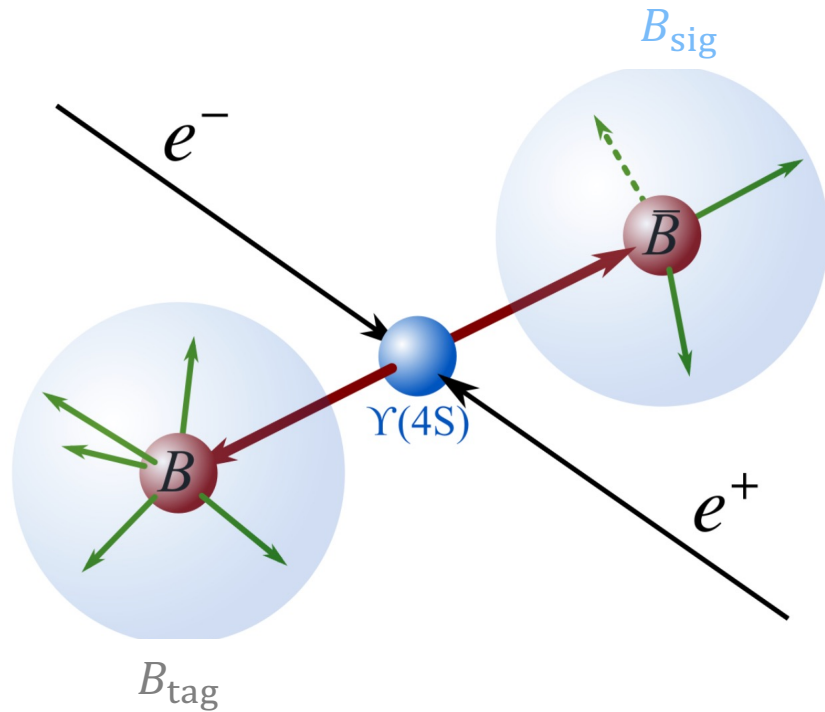
RECONSTRUCTION: TAGGING

$$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B_{\text{sig}} B_{\text{tag}}$$



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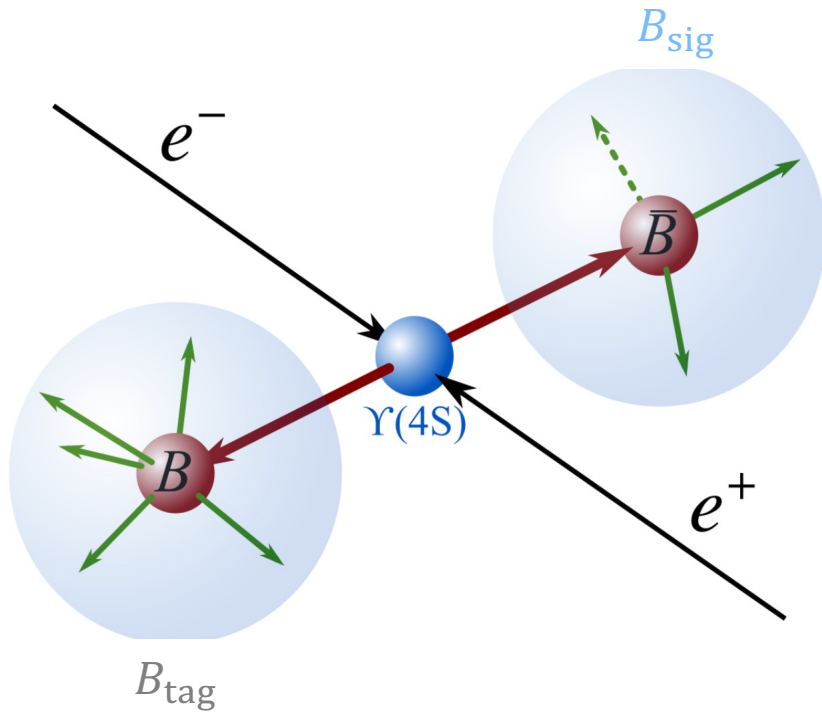


Tagged:

- B_{sig} and B_{tag} reconstructed
- Reconstruct B_{tag} in hadronic or semileptonic modes
- Using multivariate methods

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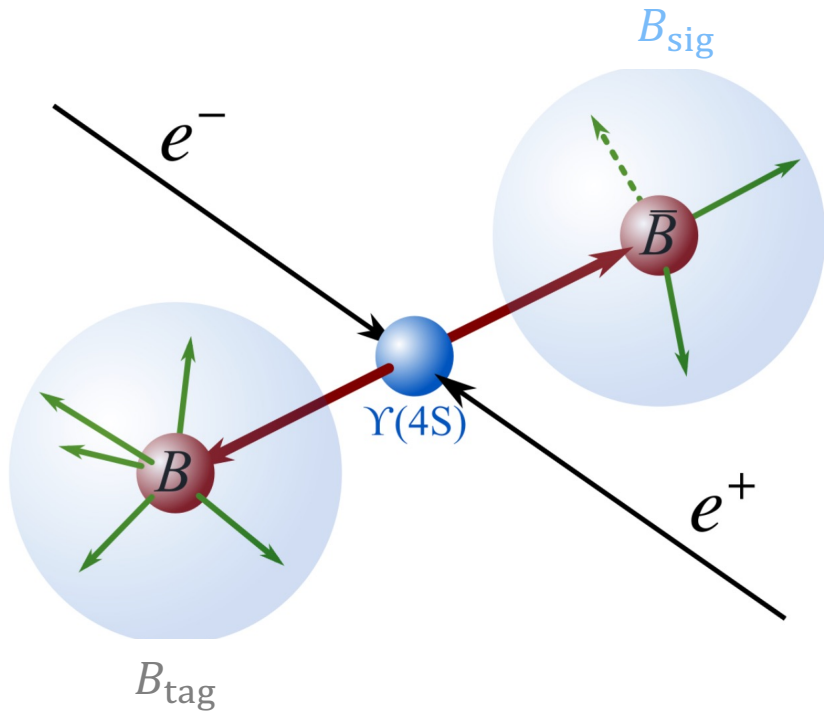
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Untagged (inclusive tag):

- Only B_{sig} reconstructed

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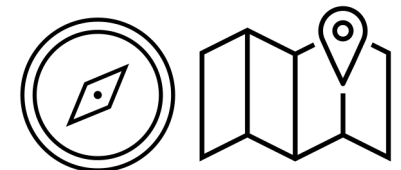


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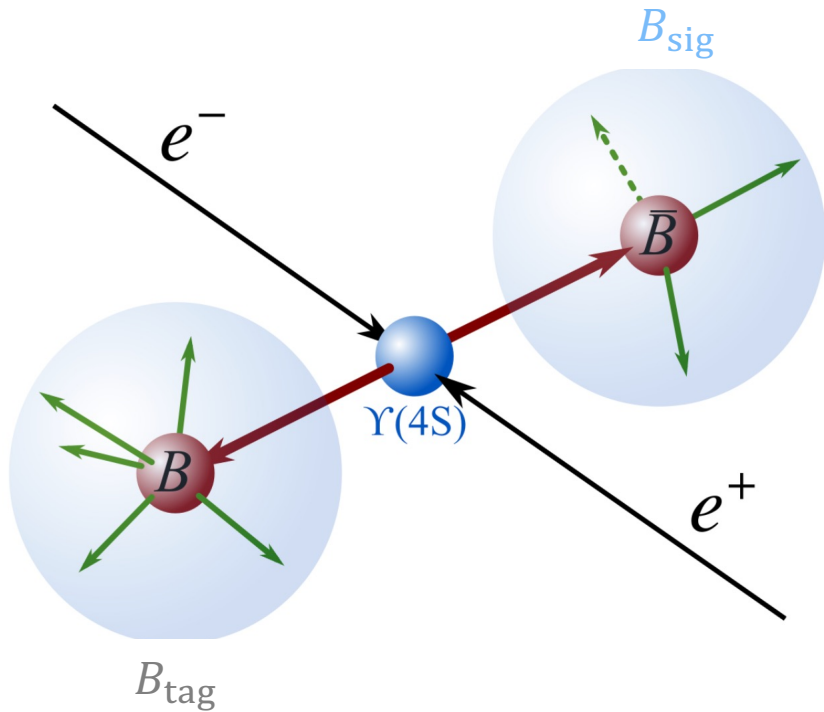
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RECONSTRUCTION: EXCLUSIVE/INCLUSIVE

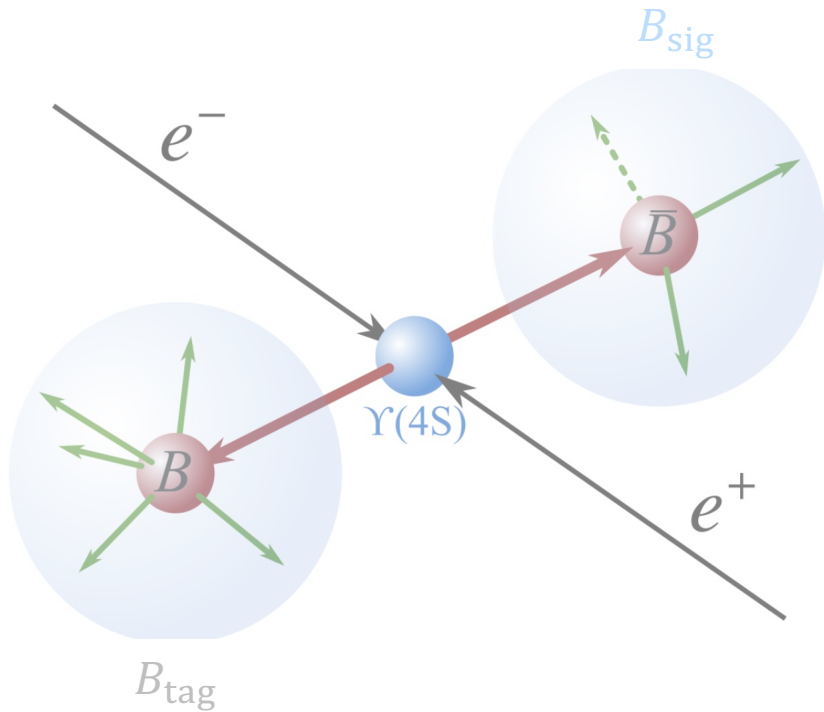
$$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B_{\text{sig}} B_{\text{tag}}$$



	$B \rightarrow D^* l \nu$	$B \rightarrow D l \nu$	$B \rightarrow D^* l \nu$	
$B \rightarrow D^* l \nu$	$B \rightarrow D l \nu$	$B \rightarrow D l \nu$	$B \rightarrow D l \nu$	
	$B \rightarrow D l \nu$	$B \rightarrow X_c l \nu$	$B \rightarrow D l \nu$	
$B \rightarrow X_c l \nu$	$B \rightarrow D l \nu$		$B \rightarrow D^* l \nu$	$B \rightarrow X_c l \nu$
	$B \rightarrow D l \nu$	$B \rightarrow D^* l \nu$		$B \rightarrow X_c l \nu$
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$$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B_{\text{sig}} B_{\text{tag}}$$



Exclusive:

- B_{sig} reconstructed as specific final state

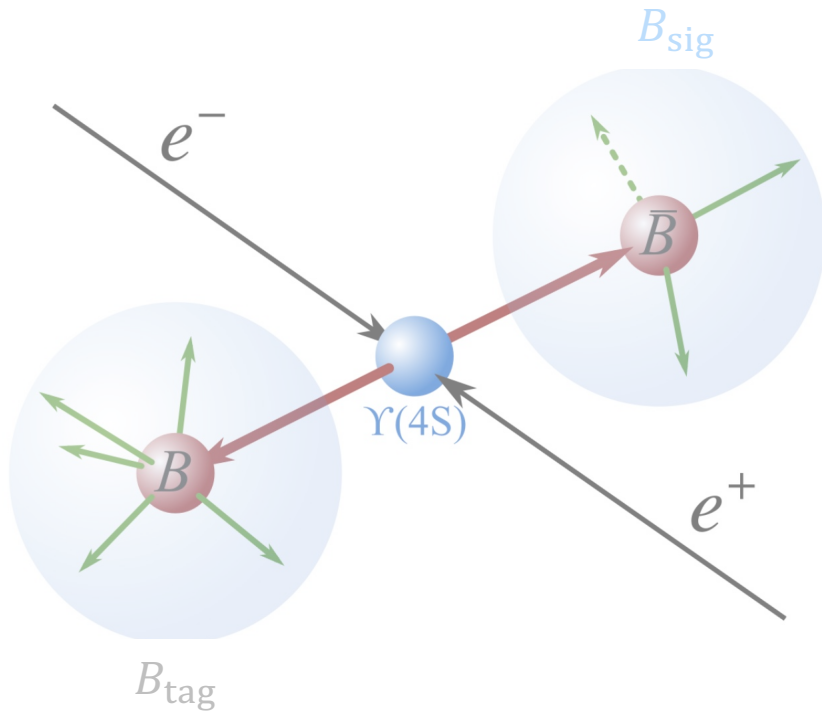
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- B_{sig} reconstructed as sum of modes

$B \rightarrow D^*lv$ $B \rightarrow Dlv$ $B \rightarrow D^*lv$
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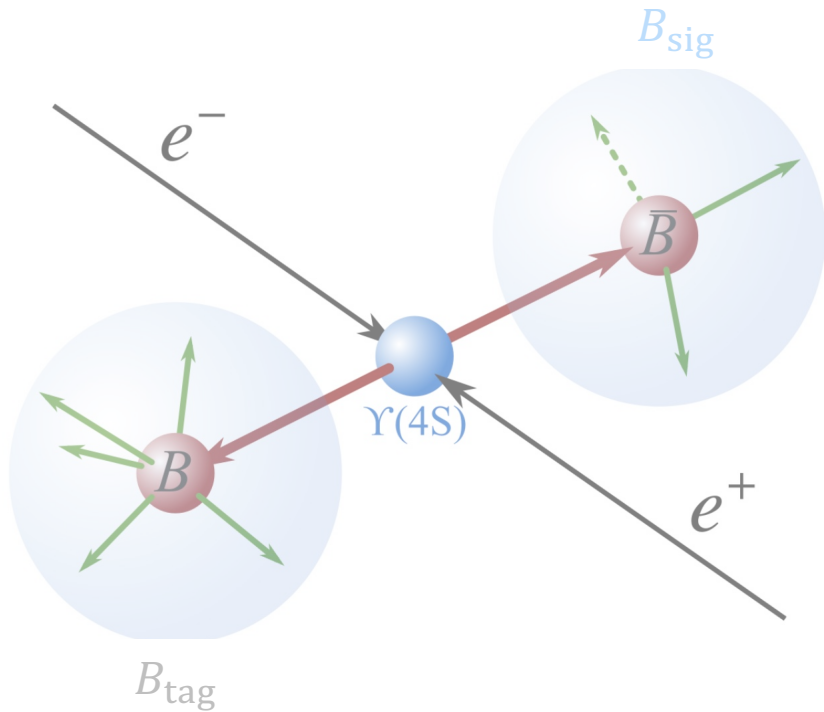
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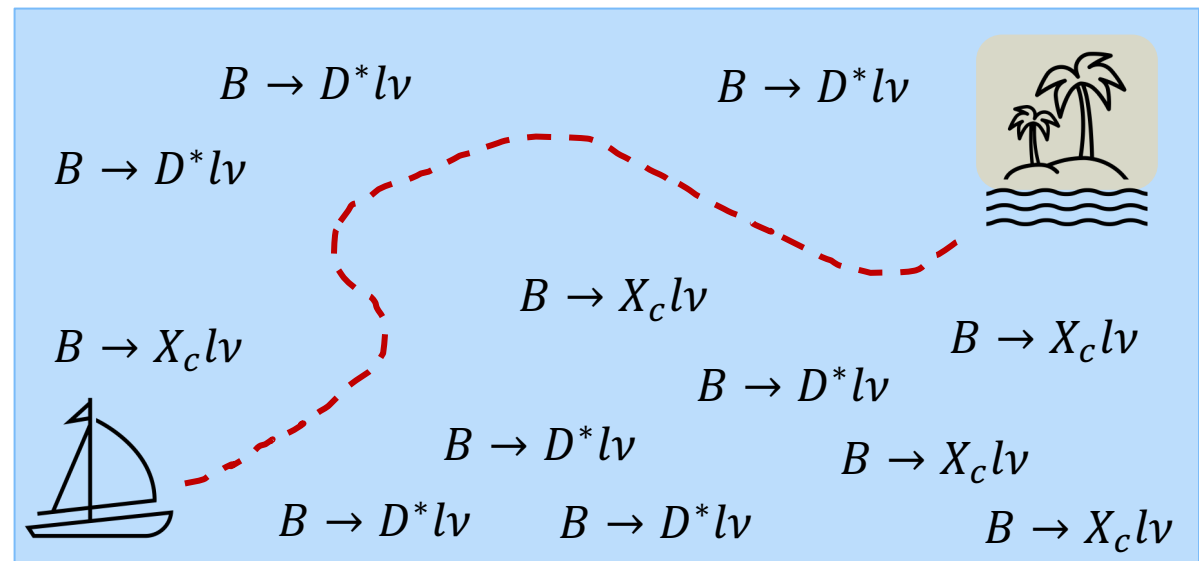


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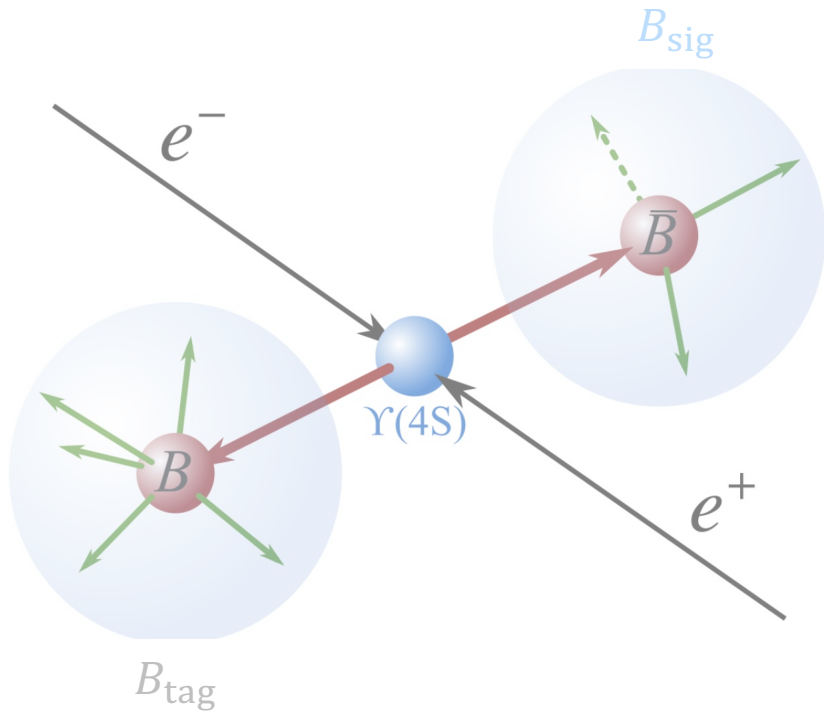
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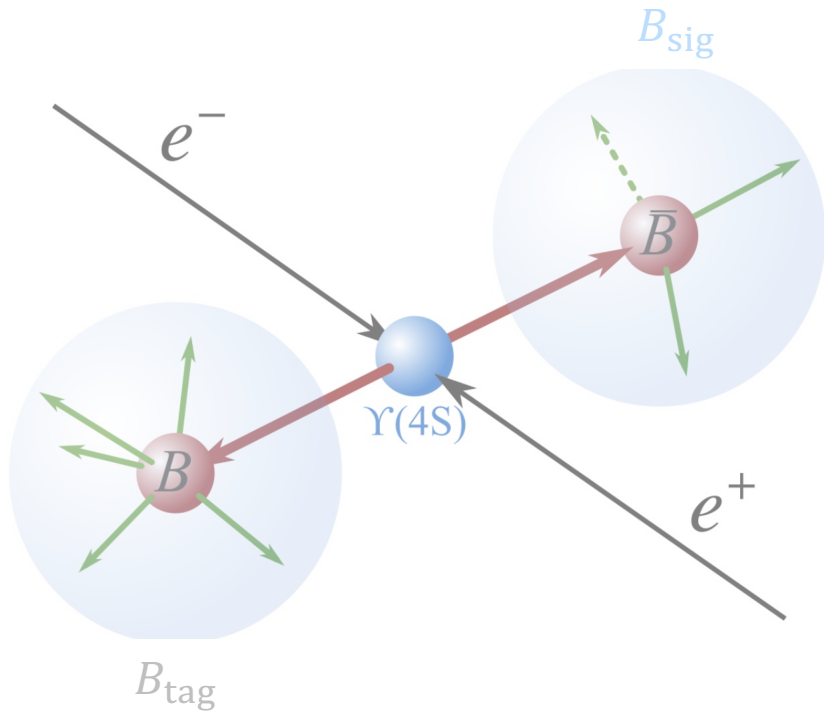
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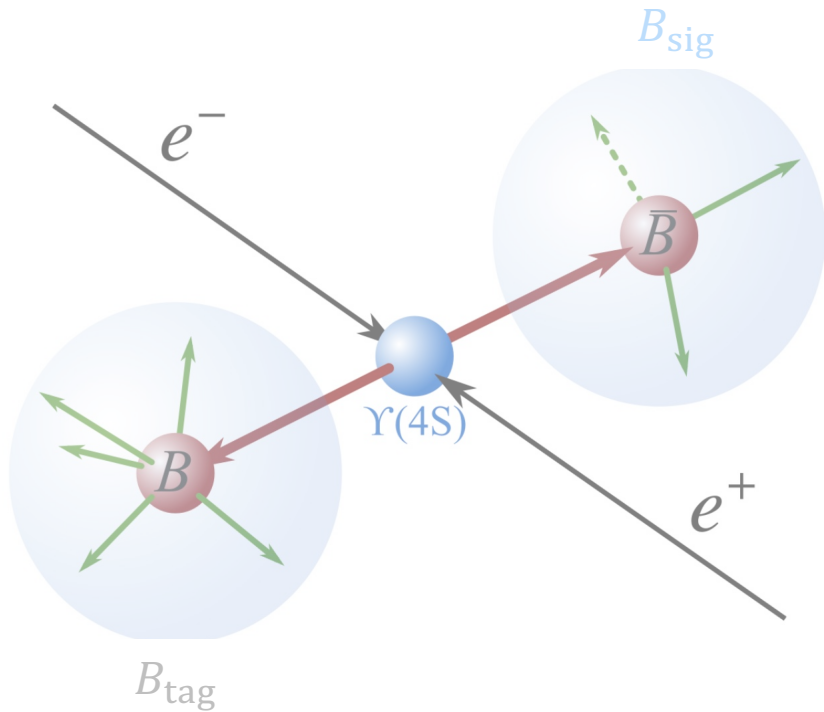
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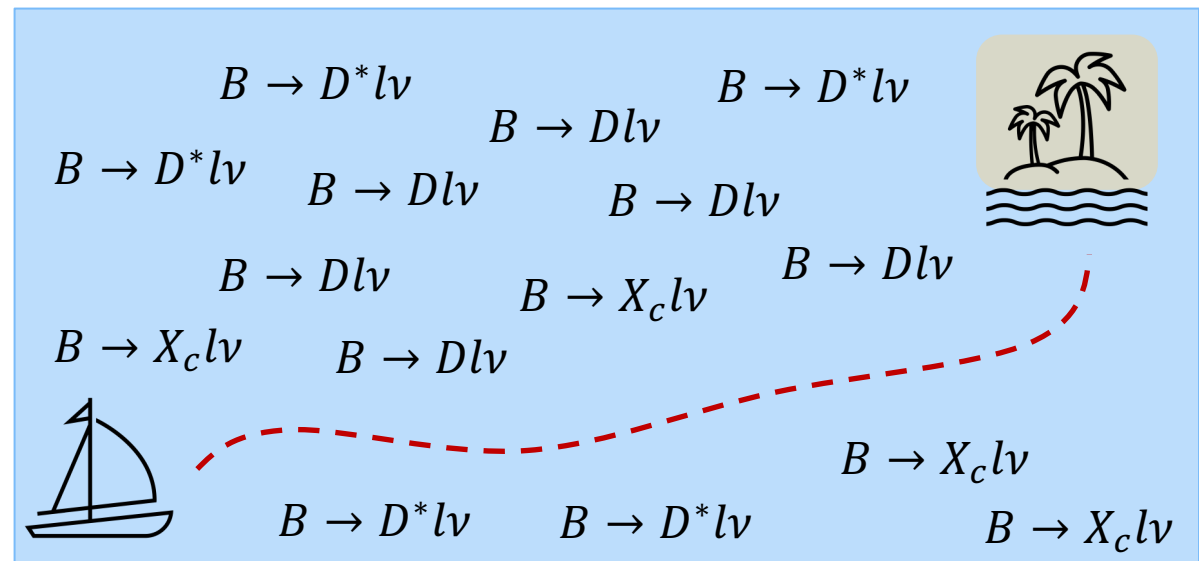


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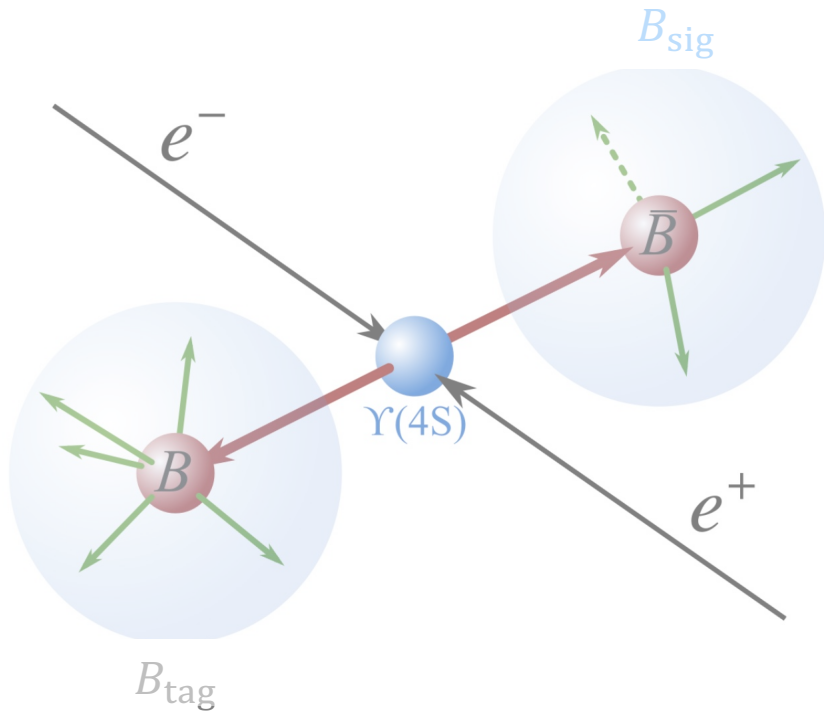
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Approaches are theoretically and experimentally independent

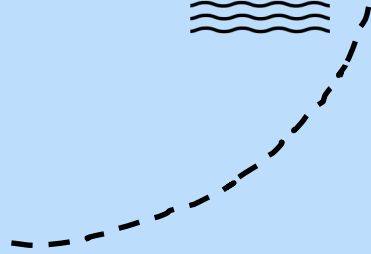
SM PRECISION MEASUREMENTS

$$\begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

CKM Matrix

Form-factor
measurements

SM precision
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CKM Matrix

Form-factor measurements



Untagged $B \rightarrow D^* l \nu$ at Belle II



Tagged $B \rightarrow D^* l \nu$ at Belle



Other $|V_{cb}|$ at Belle II

$|V_{cb}|$

SM precision measurements



SM PRECISION MEASUREMENTS

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Other $|V_{cb}|$ at Belle II

$|V_{cb}|$



Untagged $B \rightarrow \pi l \nu$ at Belle II



Other $|V_{ub}|$ at Belle II



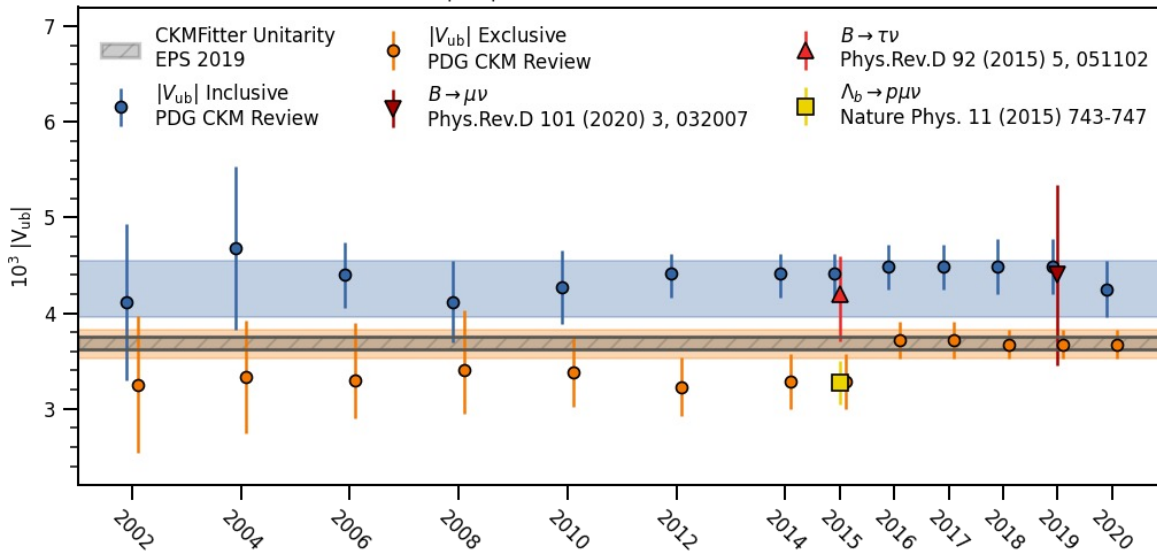
Tagged simultaneous exclusive and inclusive measurement of $|V_{ub}|$ at Belle

$|V_{ub}|$

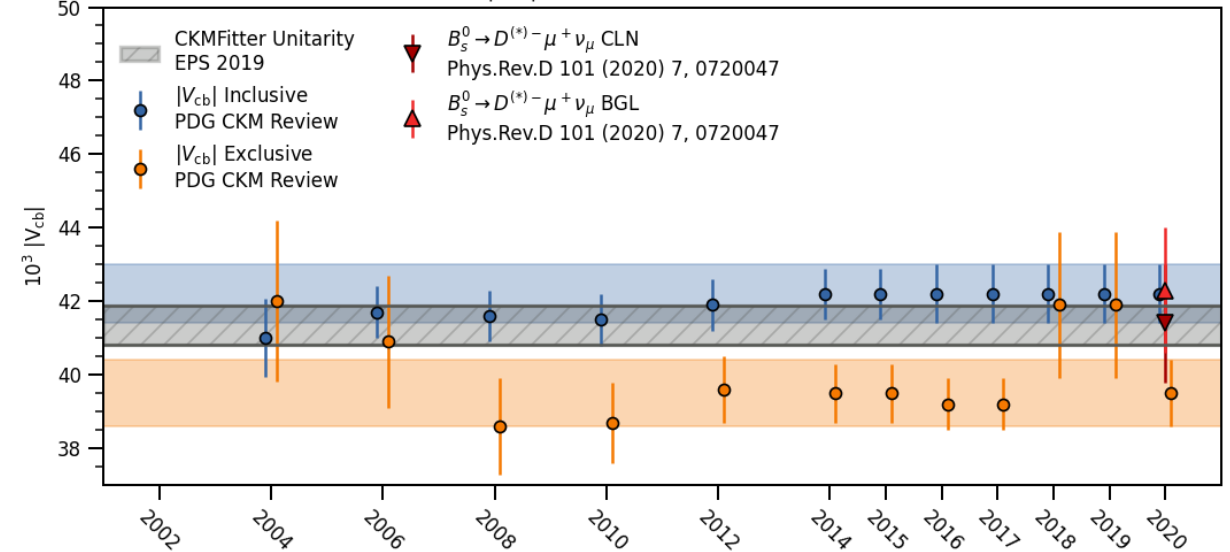
MOTIVATION: CKM MATRIX ELEMENTS

- Test SM by over-constraining unitarity triangle using CKM matrix elements
- Important inputs to SM rates of ultra rare decays
- Tension between **exclusive** and **inclusive** $|V_{xb}|$ measurements at level of $2-3\sigma$

$|V_{ub}|$ Measurements over Time



$|V_{cb}|$ Measurements over Time



$|V_{XB}|$ FROM SEMILEPTONIC DECAYS

– Semileptonic: leptonic and hadronic currents factorize

– Describe kinematics using

Hadronic recoil:

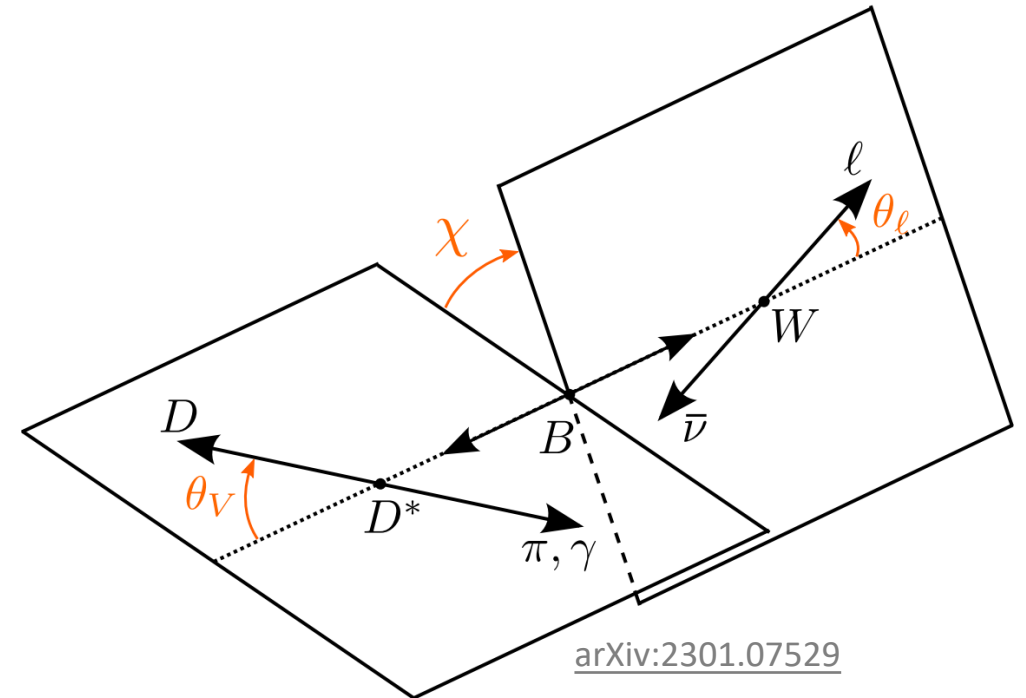
$$W = \frac{p_B \cdot p_X}{m_B m_X}$$

or

Momentum transfer squared:

$$q^2 = (p_B - p_X)^2$$

and the angles $\theta_l, \theta_\nu, \chi$



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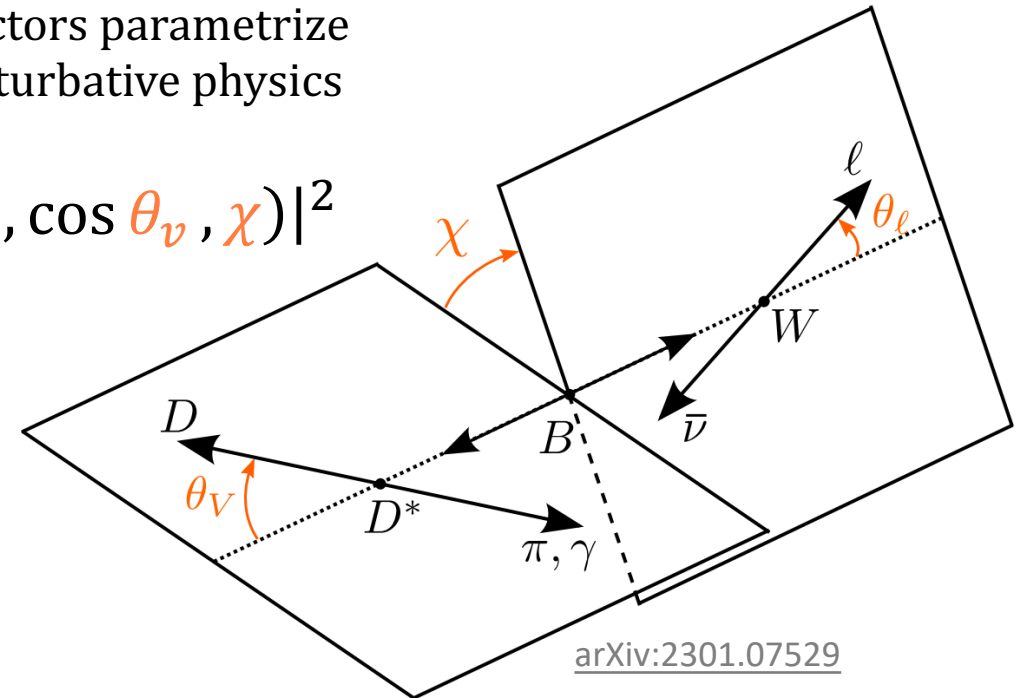
$$q^2 = (p_B - p_X)^2$$

and the angles θ_l, θ_v, χ

– Exclusive:

Form factors parametrize non-perturbative physics

$$\frac{dB}{dq^2/w d \cos \theta_l d \cos \theta_v d \chi} \propto |V_{xb}|^2 \times |\text{FF}(q^2/w, \cos \theta_l, \cos \theta_v, \chi)|^2$$



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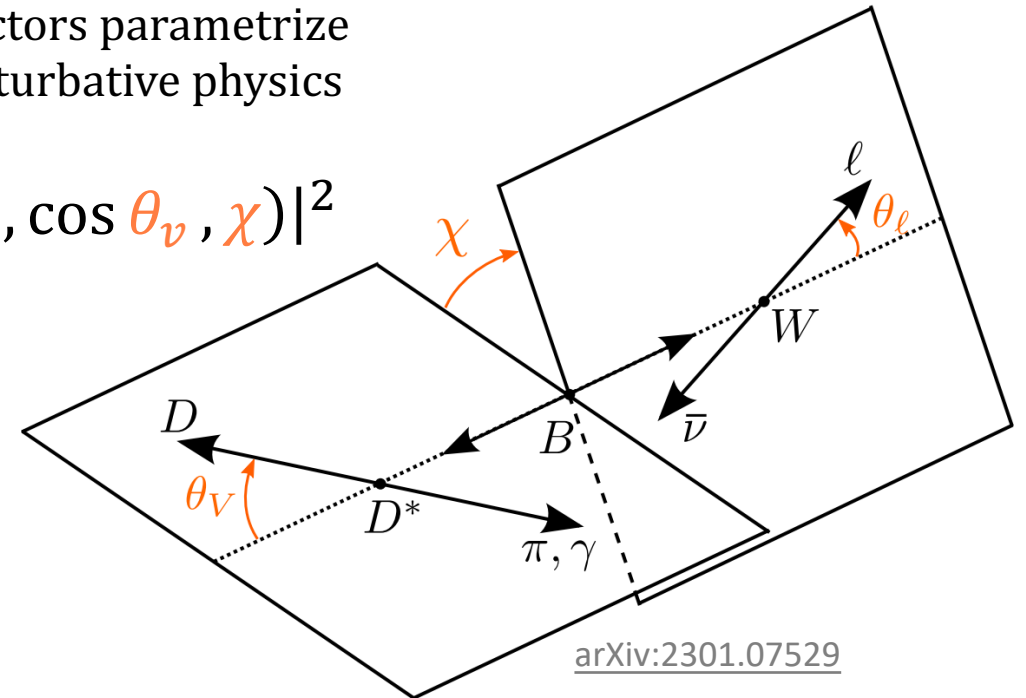
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– Inclusive:

Operator product expansion

$$B \propto |V_{xb}|^2 \times \left[\Gamma(b \rightarrow ql\bar{\nu}_l) + \frac{1}{m_b} + \alpha_s + \dots \right]$$



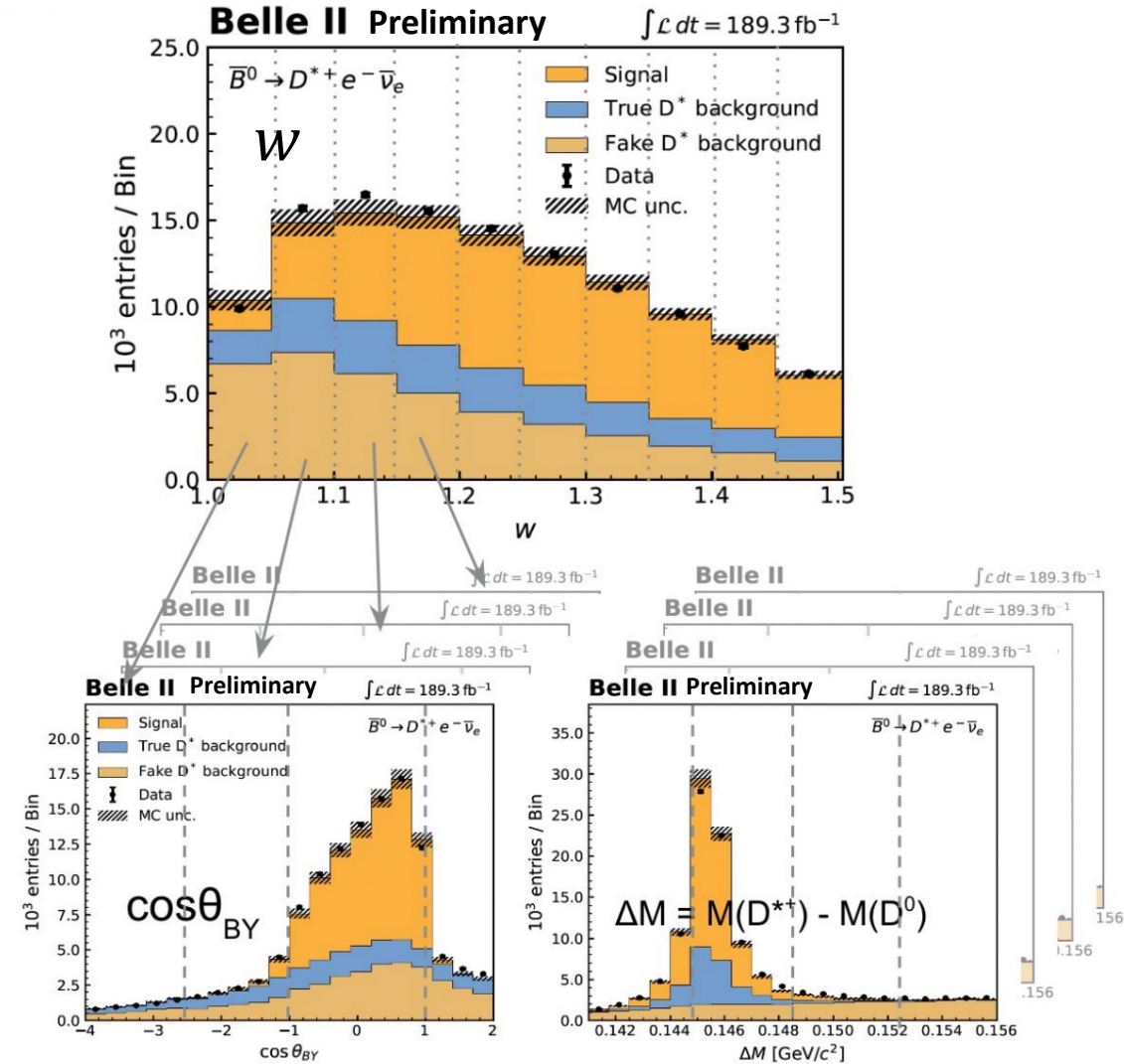
[arXiv:2301.07529](https://arxiv.org/abs/2301.07529)

UNTAGGED $B \rightarrow D^* l \nu$ AT BELLE II

- Untagged reconstruction of $B^0 \rightarrow D^{*+} l^- \bar{\nu}_l$
 - $D^{*+} \rightarrow D^0 \pi^+$ and $D^0 \rightarrow K^- \pi^+$
- Extract signal yields independently in 8(10) bins of $\cos\theta_l$, $\cos\theta_\nu$, χ and w
- Perform 2D fits of $\cos\theta_{BY}$ ($Y = D^* l$) and ΔM

$$\cos\theta_{BY} = \frac{2E_B E_Y - m_B^2 - m_Y^2}{2p_B p_Y}$$

$$\Delta M = M(D^*) - M(D^0)$$



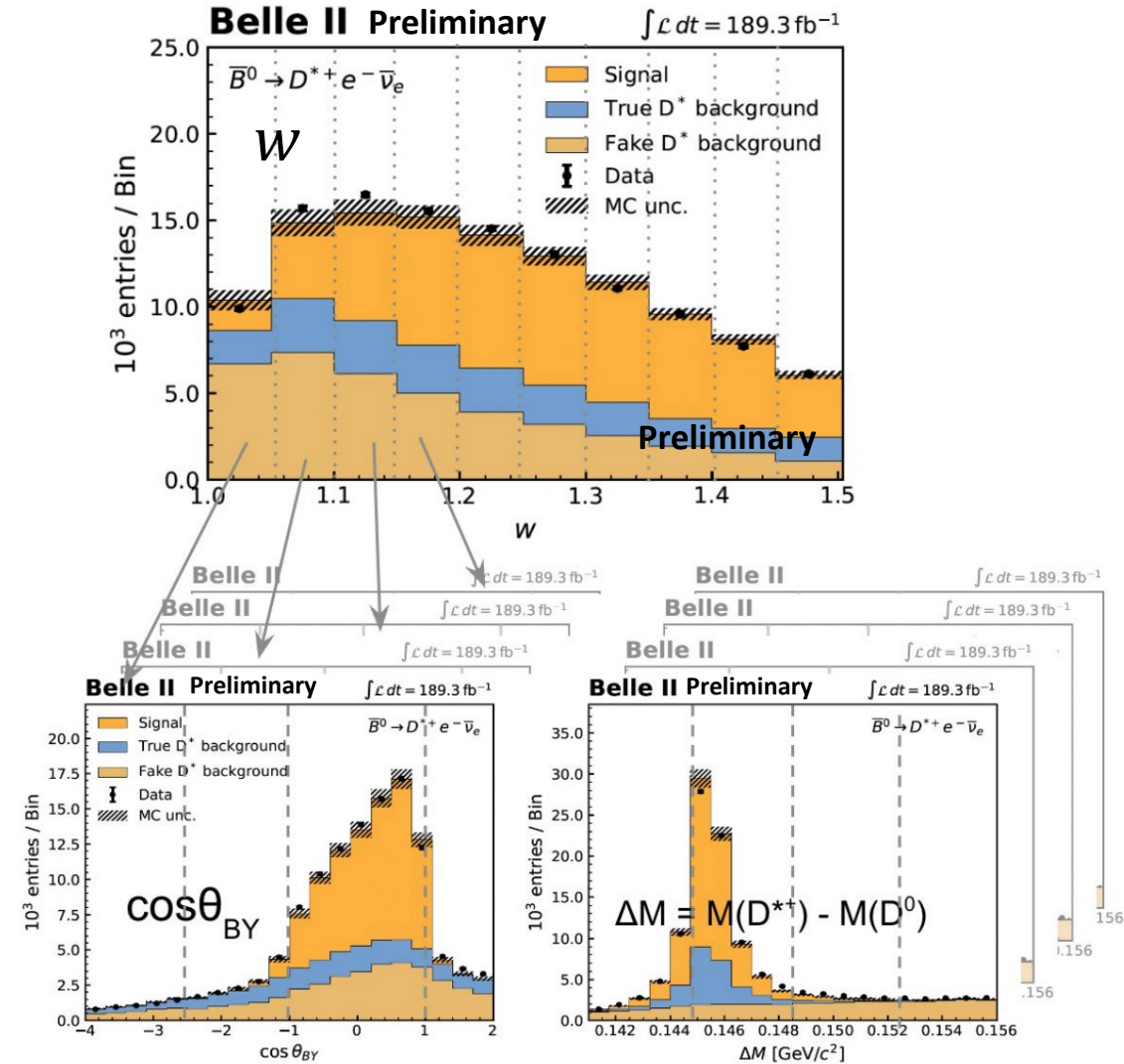
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$$\cos\theta_{BY} = \frac{2E_B E_Y - m_B^2 - m_Y^2}{2p_B p_Y} \quad \Delta M = M(D^*) - M(D^0)$$

- Unfolded yields obtained using singular value decomposition [arXiv:hep-ph/9509307](https://arxiv.org/abs/hep-ph/9509307)
- Converted to partial branching fractions $\Delta\Gamma_i$ using reconstruction efficiencies



UNTAGGED $B \rightarrow D^* l \nu$ AT BELLE II

– Determine $|V_{cb}|$ by minimising χ^2 :

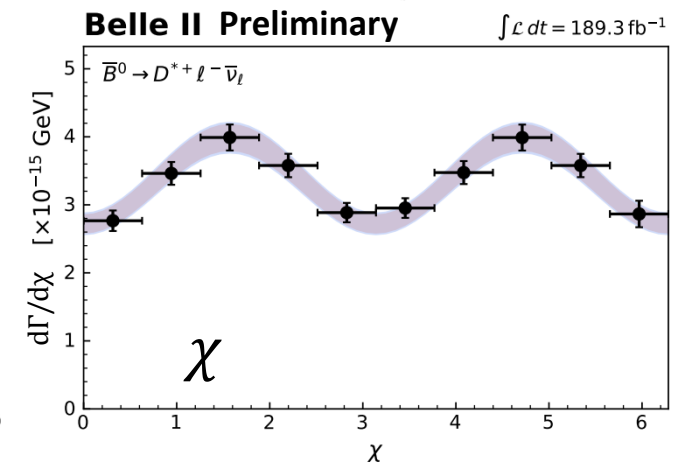
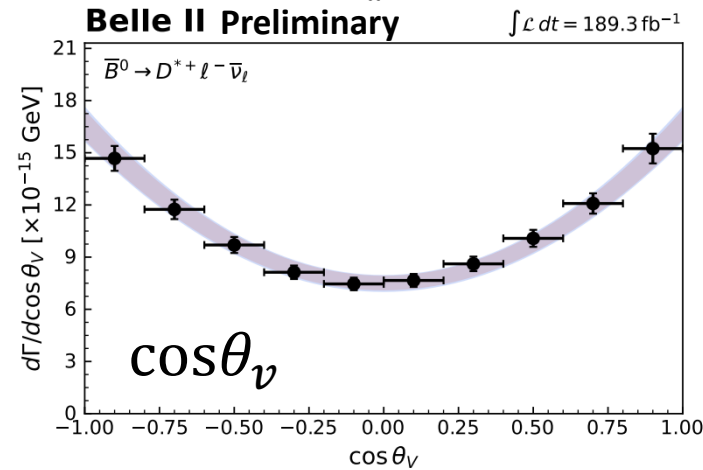
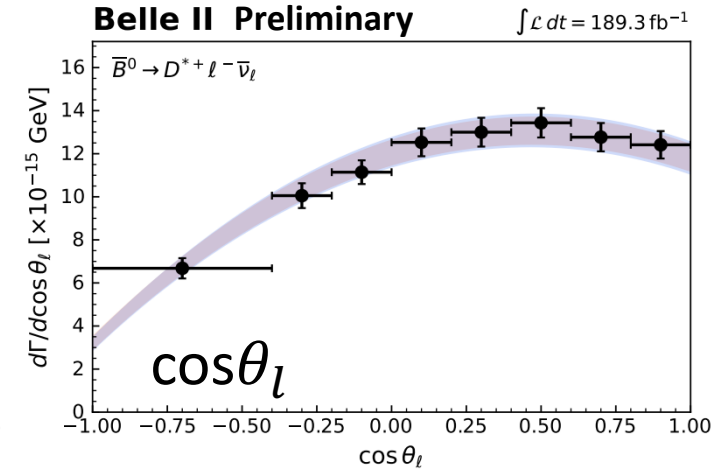
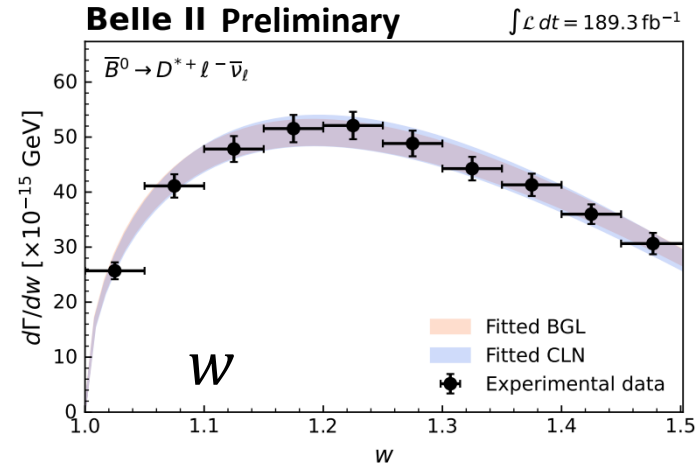
$$\chi^2 = \sum_{i,j}^{34} \left(\frac{\Delta\Gamma_i^{\text{obs}}}{\Gamma^{\text{obs}}} - \frac{\Delta\Gamma_i^{\text{pre}}}{\Gamma^{\text{pre}}} \right) C_{ij}^{-1} \left(\frac{\Delta\Gamma_j^{\text{obs}}}{\Gamma^{\text{obs}}} - \frac{\Delta\Gamma_j^{\text{pre}}}{\Gamma^{\text{pre}}} \right) + \frac{(\Gamma^{\text{obs}} - \Gamma^{\text{pre}})^2}{\sigma_\Gamma^2}$$

- Experimental observation
- Experimental covariance
- Theoretical prediction

– Form-factor parameterizations:

Caprini-Lellouch-Neubert (CLN)
parameterization
Phys. Rev. D 56 (1997) 6895

Boyd-Grinstein-Lebed (BGL)
parameterization
Nucl. Phys. B 530 (1998) 153



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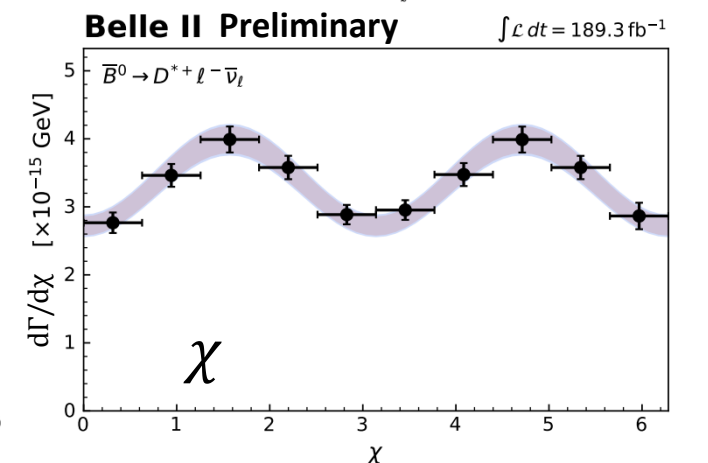
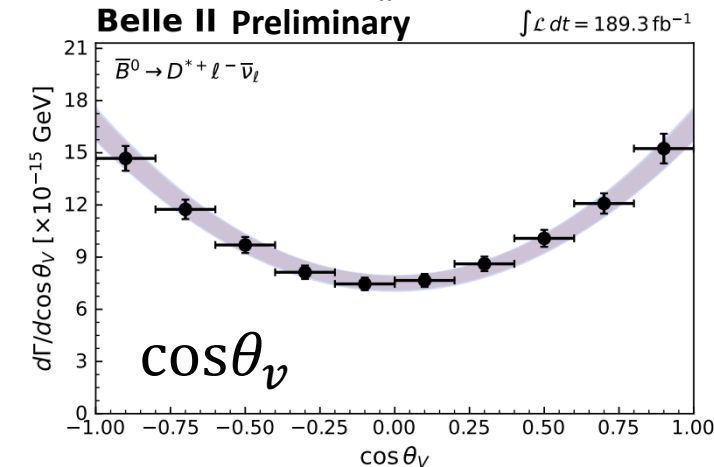
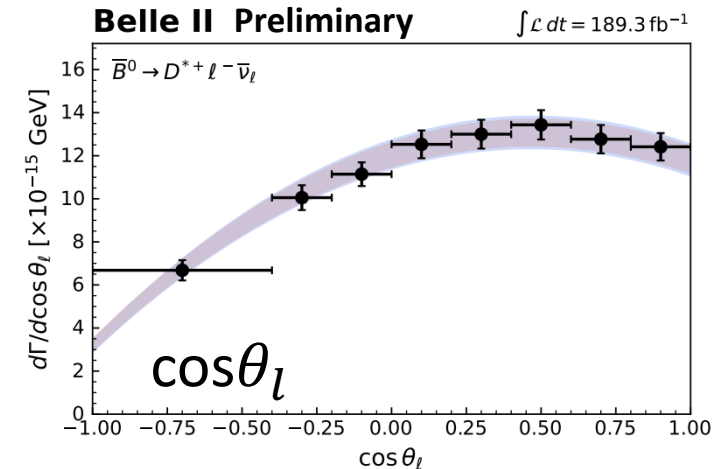
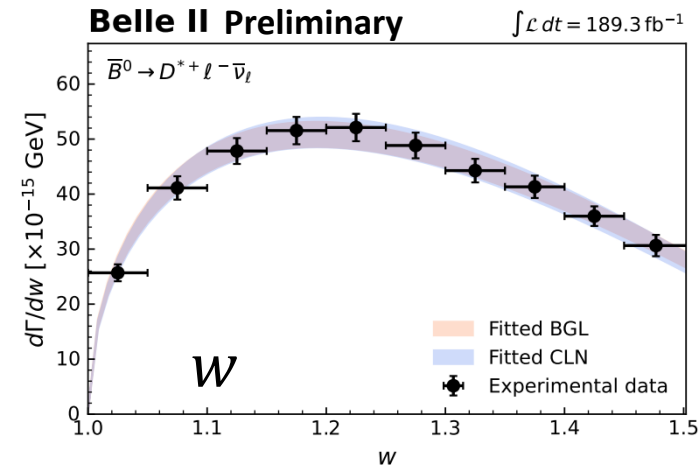
– Form-factor parameterizations:

Caprini-Lellouch-Neubert (CLN)
parameterization
Phys. Rev. D 56 (1997) 6895

Boyd-Grinstein-Lebed (BGL)
parameterization
Nucl. Phys. B 530 (1998) 153

$$|V_{cb}|_{\text{BGL}} = (40.9 \pm 0.3_{\text{stat}} \pm 1.0_{\text{syst}} \pm 0.6_{\text{theo}}) \times 10^{-3}$$

$$|V_{cb}|_{\text{CLN}} = (40.4 \pm 0.3_{\text{stat}} \pm 1.0_{\text{syst}} \pm 0.6_{\text{theo}}) \times 10^{-3}$$

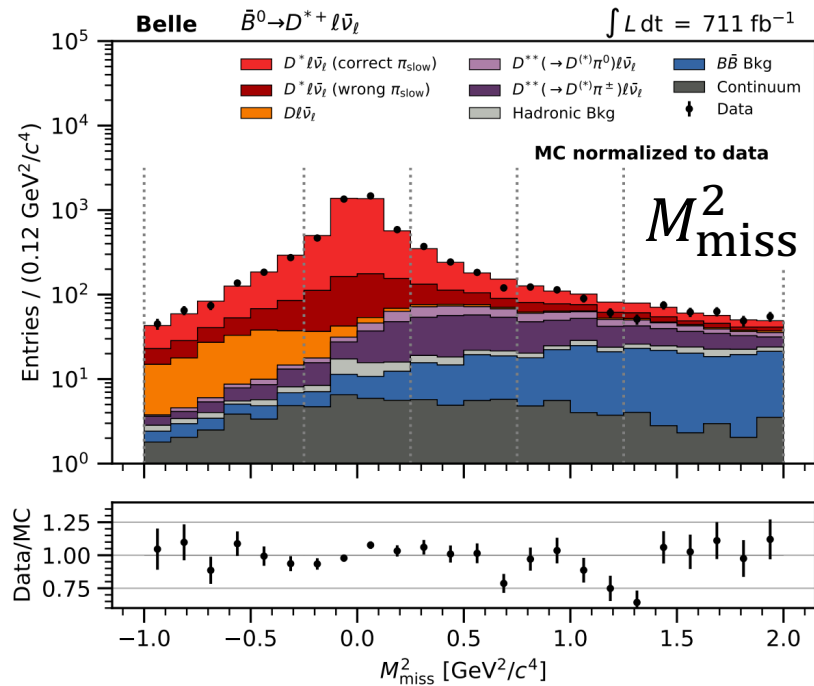


Phys. Rev. D 89 (2014) 114504

- LQCD at zero recoil ($w = 1$) used for normalization
- Shifts exclusive average closer to inclusive average

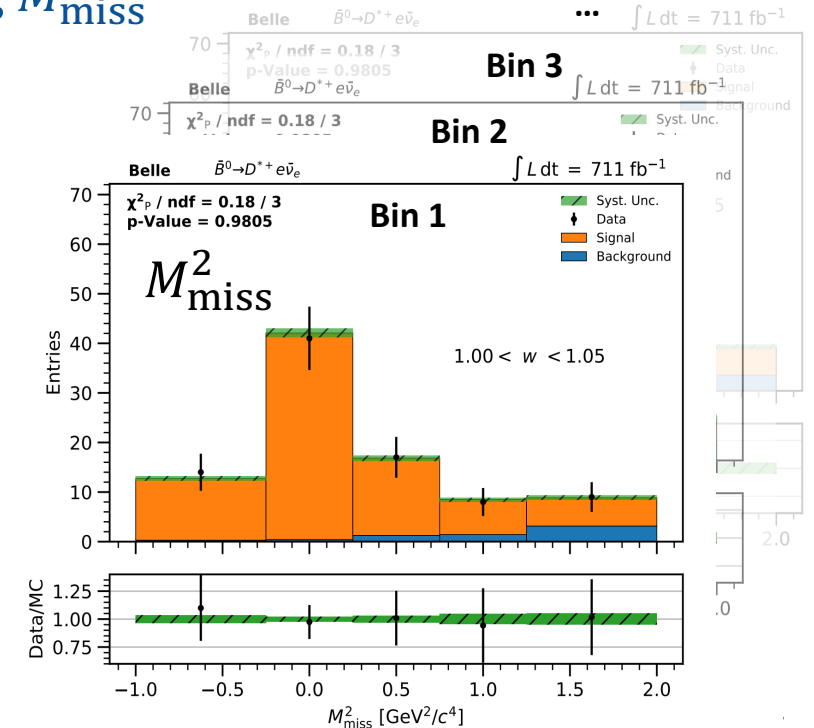
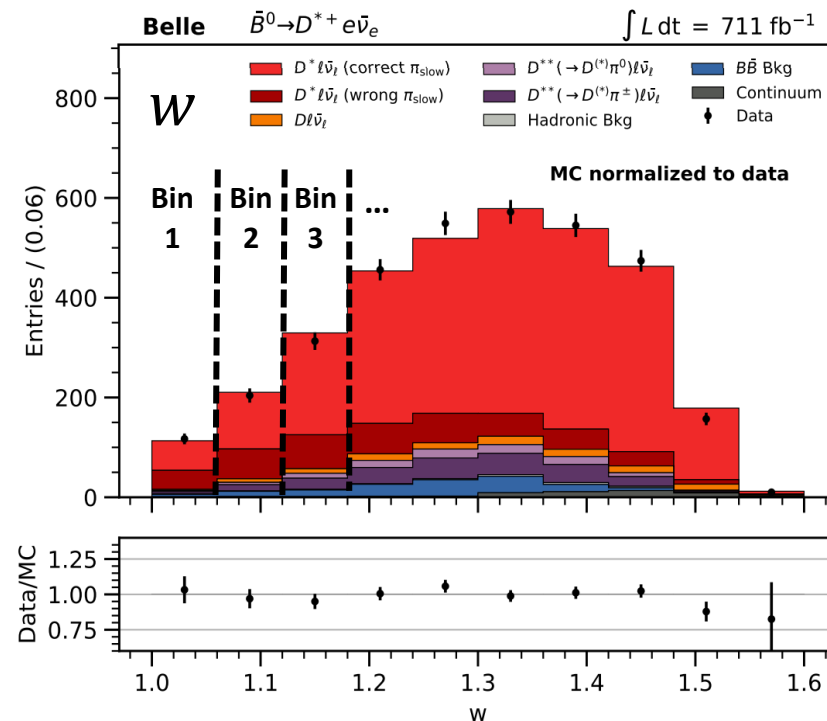
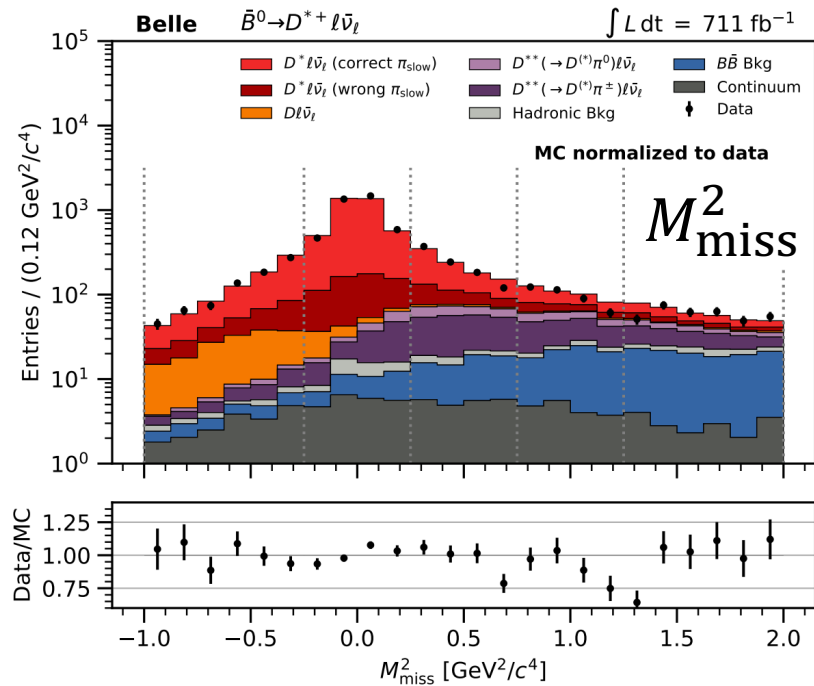
TAGGED $B \rightarrow D^* l \nu$ AT BELLE

- Use Full Event Interpretation to reconstruct B_{tag} Comput Softw Big Sci 3, 6 (2019)
- Reconstruct $B \rightarrow D^* l \bar{\nu}_l$ with $D^{*+} \rightarrow D^{0/+} \pi^{+ / 0}$ and $D^{*0} \rightarrow D^0 \pi^0$ → Reconstruct D in 16 modes
- Missing mass squared: $M_{\text{miss}}^2 = (p_{e^+e^-} - p_{B_{\text{tag}}} - p_{D^*} - p_l)^2 \approx 0$ for signal



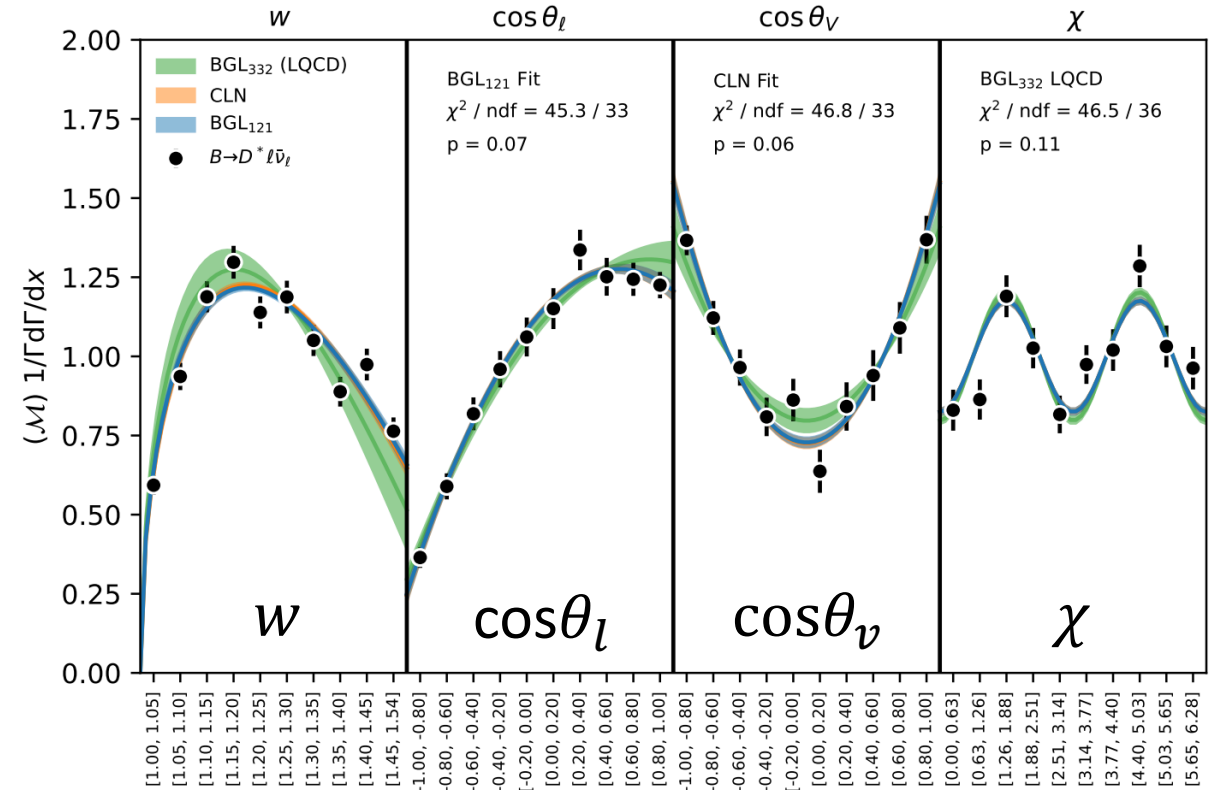
TAGGED $B \rightarrow D^* l \nu$ AT BELLE

- Use Full Event Interpretation to reconstruct B_{tag} Comput Softw Big Sci 3, 6 (2019)
- Reconstruct $B \rightarrow D^* l \bar{\nu}_l$ with $D^{*+} \rightarrow D^{0/+} \pi^{+ / 0}$ and $D^{*0} \rightarrow D^0 \pi^0$ \longrightarrow Reconstruct D^0 in 16 modes
- Missing mass squared: $M_{\text{miss}}^2 = p_{e^+e^-} - p_{B_{\text{tag}}} - p_{\pi} - p_e \approx 0$ for signal
- Extract yields independently in 10 bins of $\cos\theta_l$, $\cos\theta_\nu$, χ and w by fitting M_{miss}^2



TAGGED $B \rightarrow D^* l \nu$ AT BELLE

- Similar procedure to untagged analysis:
 - Unfold yields using matrix inversion
 - Calculate partial branching fractions
 - Determine $|V_{cb}|$ by χ^2 minimisation
- Provide full experimental covariance matrix



TAGGED $B \rightarrow D^* l \nu$ AT BELLE

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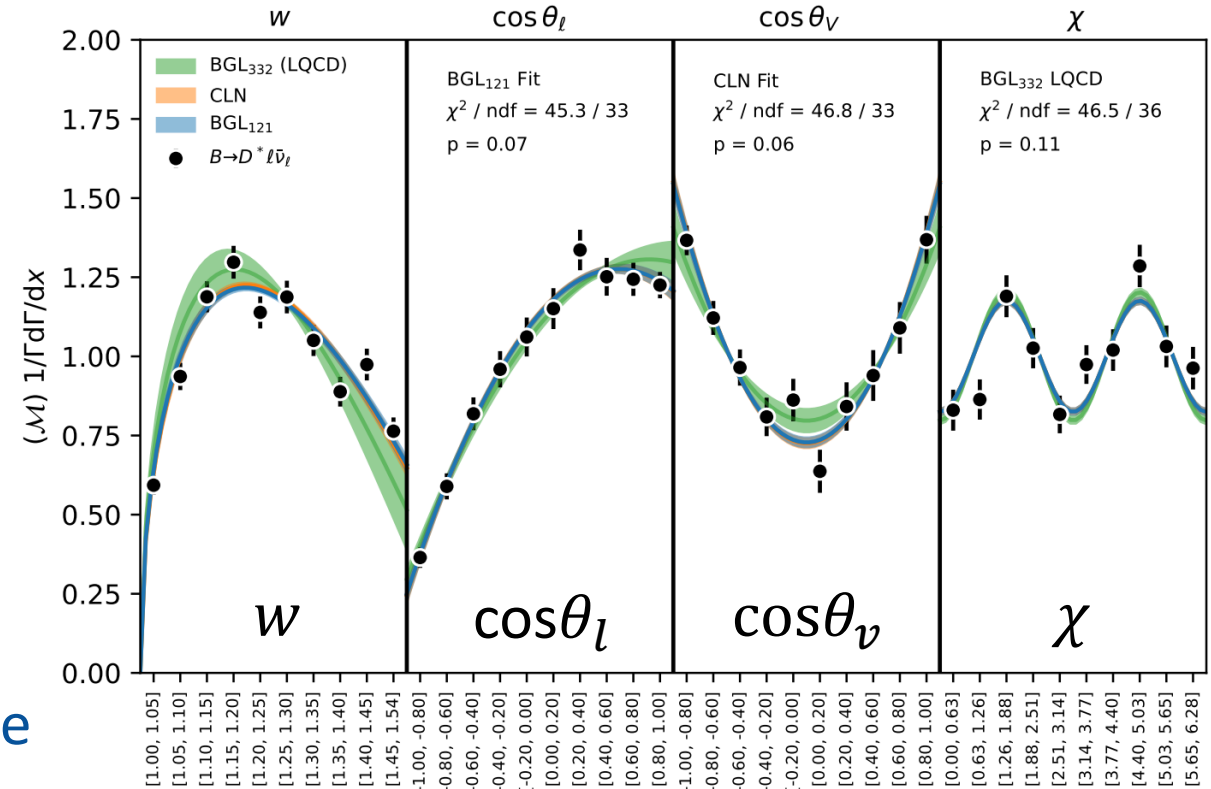
$$|V_{cb}|_{\text{BGL}} = (40.6 \pm 0.9_{\text{tot}}) \times 10^{-3}$$

$$|V_{cb}|_{\text{CLN}} = (40.1 \pm 0.9_{\text{tot}}) \times 10^{-3}$$

- Also shifts exclusive closer to inclusive average

- In addition, include lattice QCD results beyond non-zero recoil [Eur. Phys. J. C 82 \(2022\) 1141](#)

- Including full lattice information results in poor fits and lower $|V_{cb}|$ values



TAGGED $B \rightarrow D^* l \nu$ AT BELLE

- Also measure forward-backward asymmetry A_{FB} :

$$A_{FB} = \left[\int_0^1 - \int_{-1}^0 \right] d \cos \theta_l \frac{d\Gamma}{d \cos \theta_l}$$

\downarrow \downarrow
 $+$ $-$

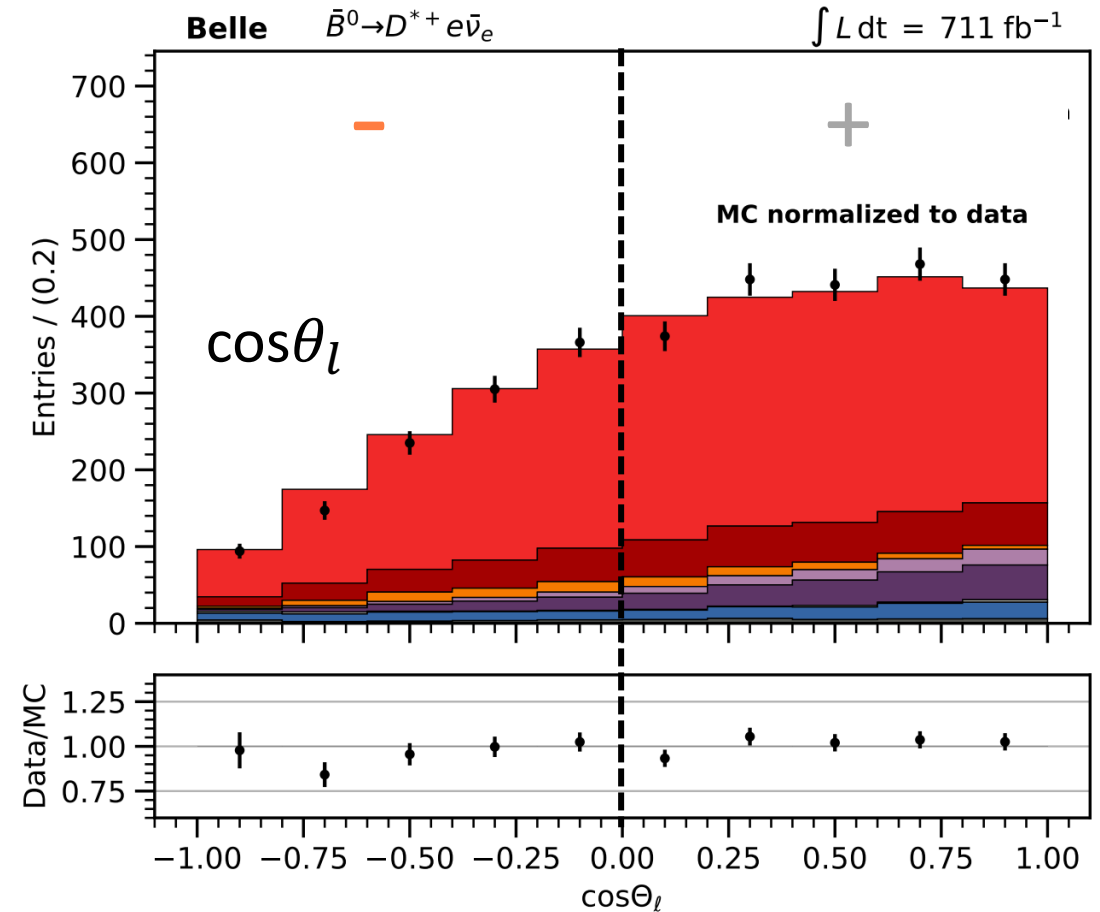
- Test lepton universality by evaluating

$$\Delta A_{FB} = A_{FB}^e - A_{FB}^\mu \quad \text{and} \quad R_{e\mu} = \frac{\mathcal{B}(B \rightarrow D^* e \nu)}{\mathcal{B}(B \rightarrow D^* \mu \nu)}$$

$$\Delta A_{FB} = 0.022 \pm 0.026_{\text{stat}} \pm 0.007_{\text{syst}}$$

$$R_{e\mu} = 0.990 \pm 0.021_{\text{stat}} \pm 0.023_{\text{syst}}$$

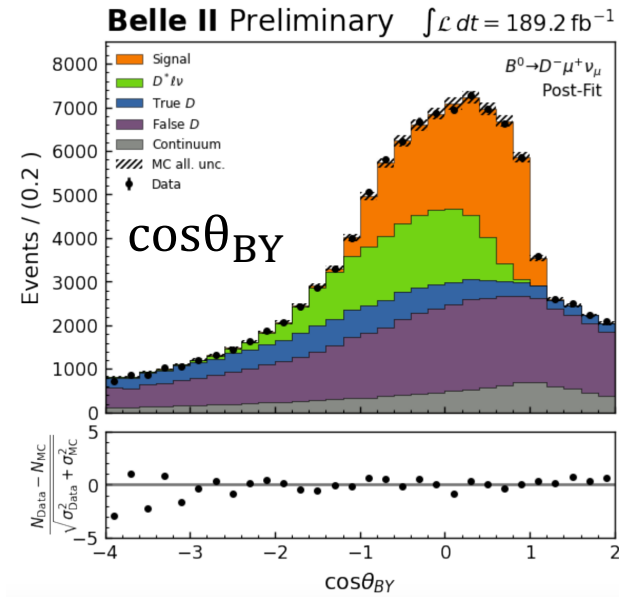
- Agrees with the SM expectation



OTHER $|V_{CB}|$ AT BELLE II

UNTAGGED $B \rightarrow Dlv$ [arXiv:2210.13143](https://arxiv.org/abs/2210.13143)

- Large backgrounds from $B \rightarrow D^*lv$
- Binned fit to $\cos\theta_{BY}$ in ten w bins



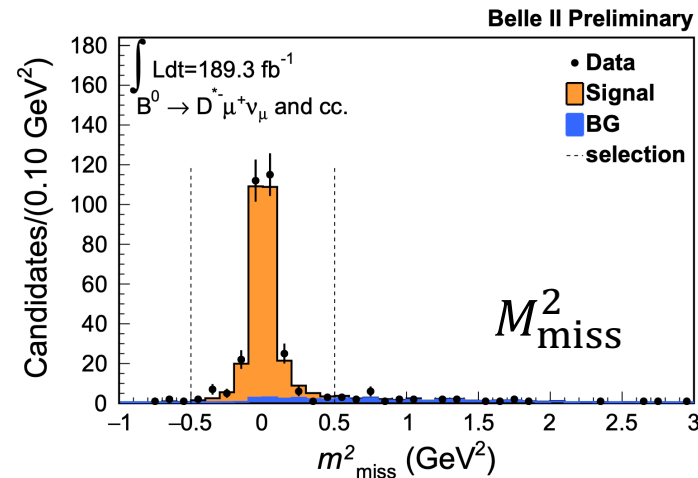
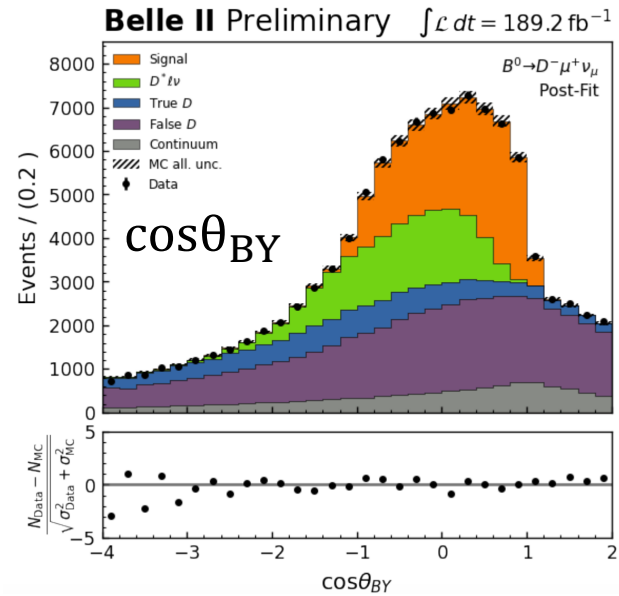
OTHER $|V_{CB}|$ AT BELLE II

UNTAGGED $B \rightarrow D l \nu$ [arXiv:2210.13143](https://arxiv.org/abs/2210.13143)

- Large backgrounds from $B \rightarrow D^* l \nu$
- Binned fit to $\cos\theta_{BY}$ in ten w bins

TAGGED $B^0 \rightarrow D^{*+} l \nu$ [arXiv:2301.04716](https://arxiv.org/abs/2301.04716)

- Fit to M_{miss}^2 in ten w bins



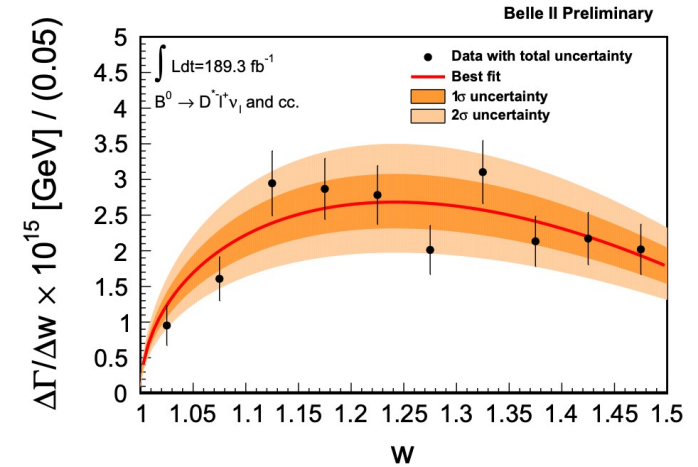
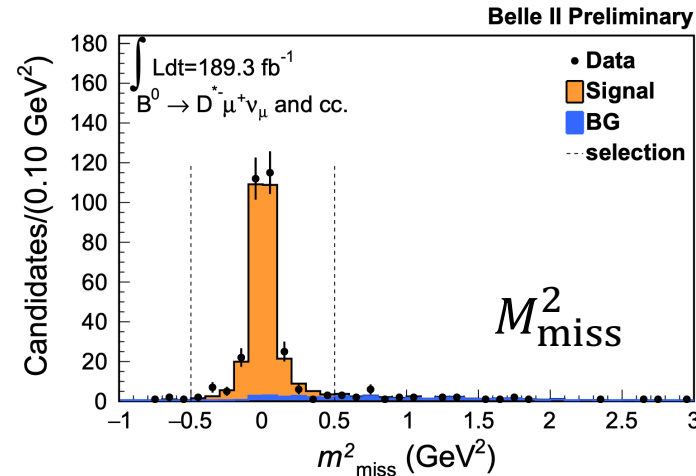
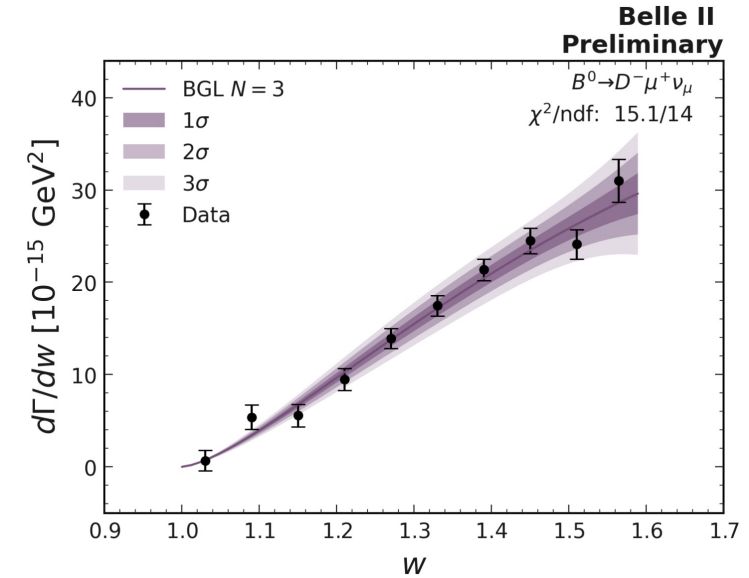
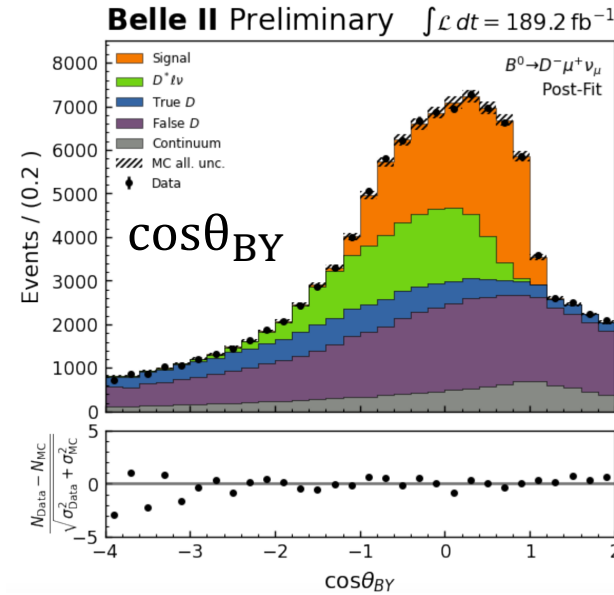
OTHER $|V_{CB}|$ AT BELLE II

UNTAGGED $B \rightarrow D l \nu$ [arXiv:2210.13143](https://arxiv.org/abs/2210.13143)

- Large backgrounds from $B \rightarrow D^* l \nu$
- Binned fit to $\cos\theta_{BY}$ in ten w bins
- Combined fit to BGL expansion and form-factor LQCD constraints [Phys. Rev. D 92, 034506](https://arxiv.org/abs/2205.04506)
[Phys. Rev. D 92, 054510](https://arxiv.org/abs/2205.04510)

TAGGED $B^0 \rightarrow D^{*+} l \nu$ [arXiv:2301.04716](https://arxiv.org/abs/2301.04716)

- Fit to M_{miss}^2 in ten w bins
- Fit CLN-parametrized form factor to differential decay rates



OTHER $|V_{CB}|$ AT BELLE II

UNTAGGED $B \rightarrow D l \nu$ [arXiv:2210.13143](https://arxiv.org/abs/2210.13143)

- Large backgrounds from $B \rightarrow D^* l \nu$
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[Phys. Rev. D 92, 054510](https://arxiv.org/abs/2205.04510)

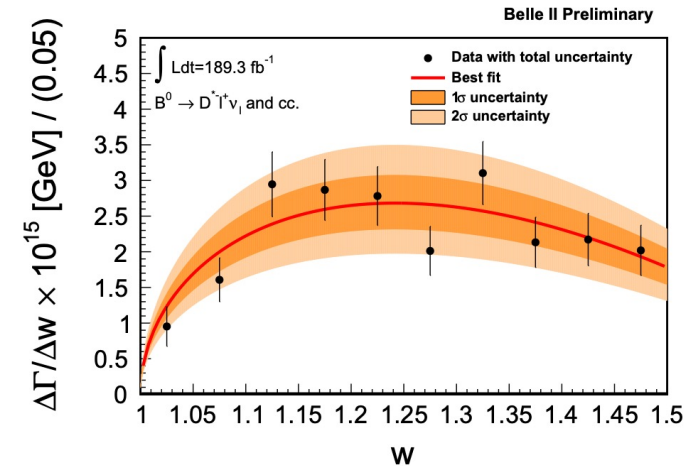
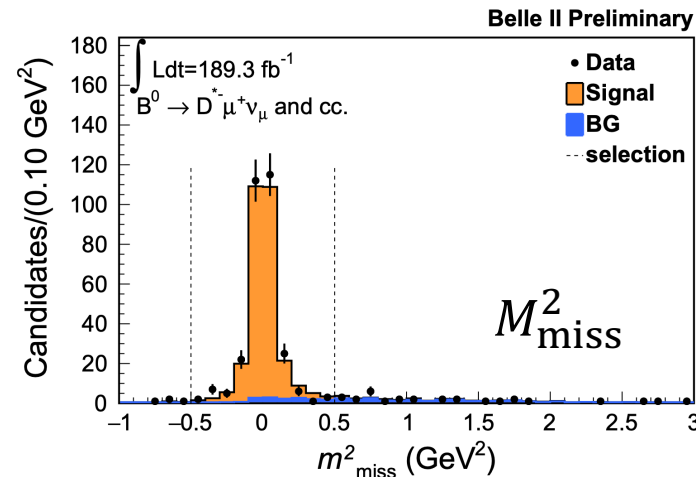
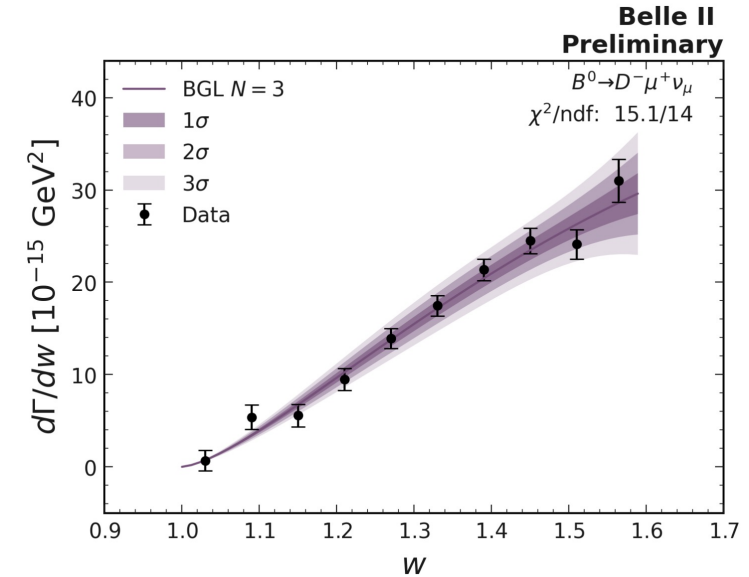
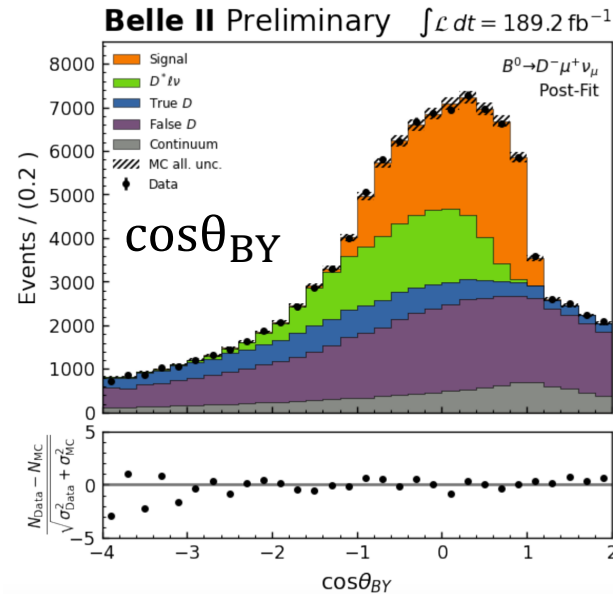
TAGGED $B^0 \rightarrow D^{*+} l \nu$ [arXiv:2301.04716](https://arxiv.org/abs/2301.04716)

- Fit to M_{miss}^2 in ten w bins
- Fit CLN-parametrized form factor to differential decay rates

$$|V_{cb}| = (38.3 \pm 1.2_{\text{tot}}) \times 10^{-3}$$

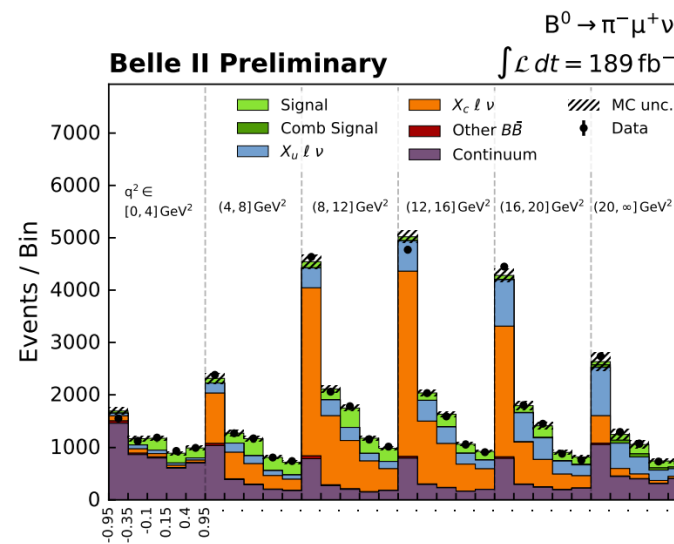
$$|V_{cb}| = (37.9 \pm 2.7_{\text{tot}}) \times 10^{-3}$$

Consistent with exclusive world-average

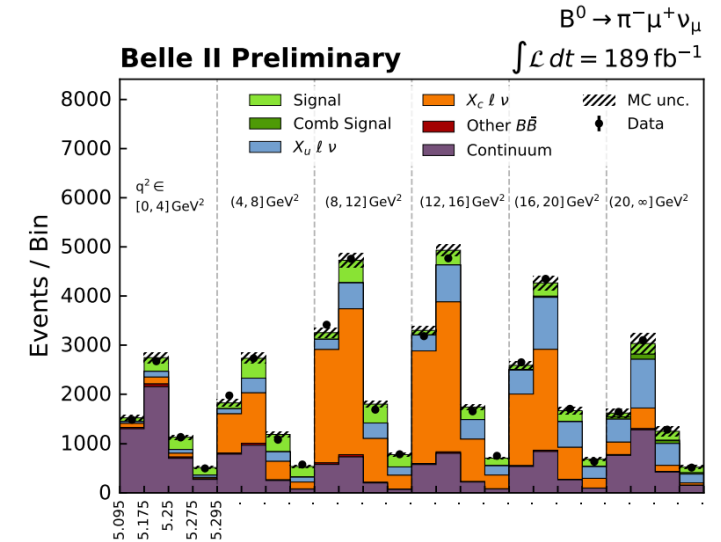


UNTAGGED $B \rightarrow \pi l \nu$ AT BELLE II

- Suffers from large $B \rightarrow X_c l \nu$ and continuum backgrounds
- Suppressed using BDTs
- Binned fit to ΔE and M_{bc} in six q^2 bins



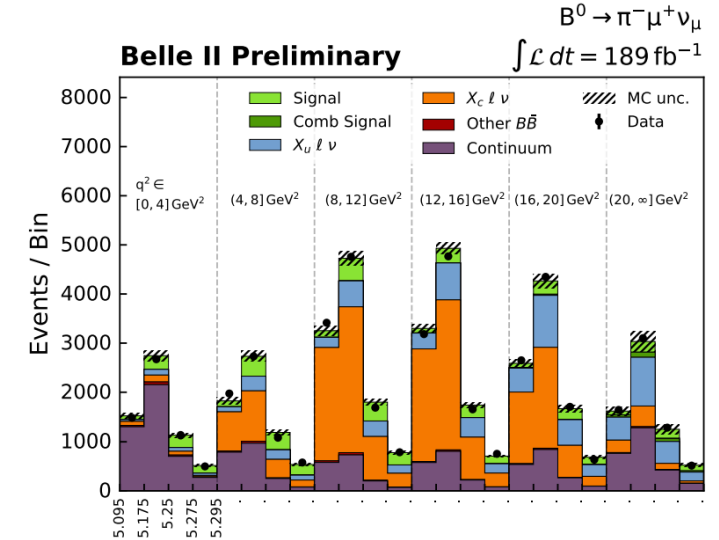
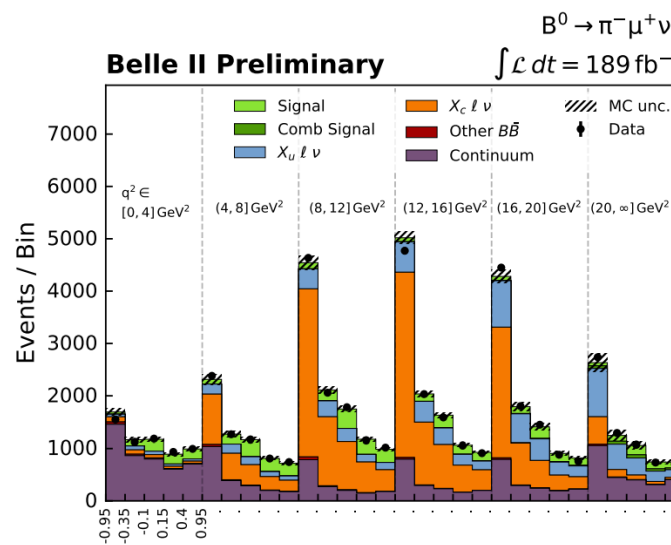
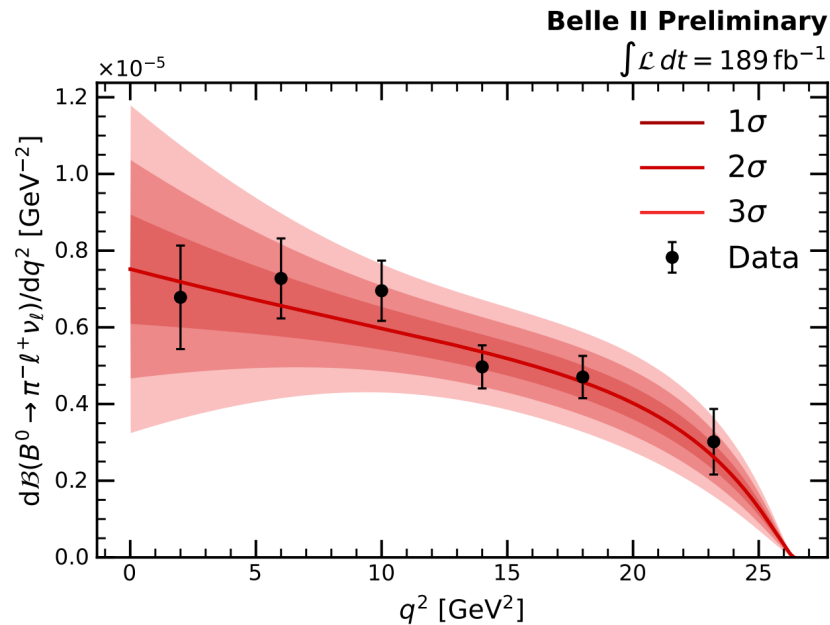
$$\Delta E = E_B - E_{\text{beam}} \text{ (GeV)}$$



$$M_{bc} = \sqrt{E_{\text{beam}}^2 - |\vec{p}_B|^2} \text{ (GeV)}$$

UNTAGGED $B \rightarrow \pi l \nu$ AT BELLE II

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[Phys. Rev. D 82, 099902](#)

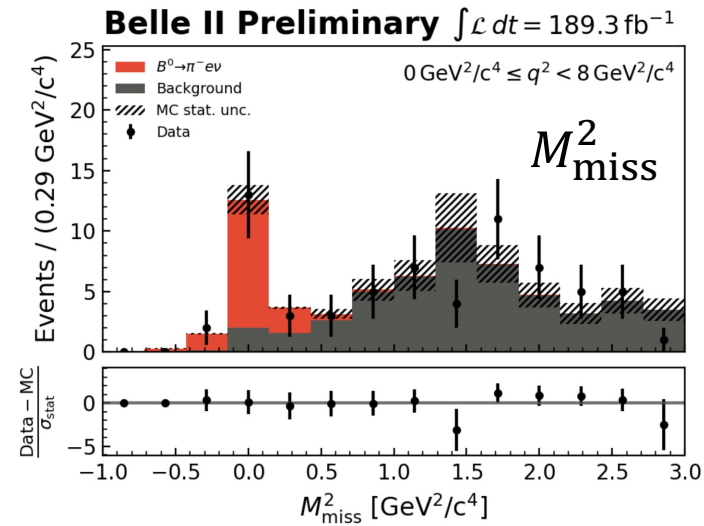
- Combined fit to Bourely-Caprini-Lellouch (BCL) expansion and form-factor LQCD constraints [Phys. Rev. D 92, 014024](#)

$$|V_{ub}| = (3.55 \pm 0.12_{\text{stat}} \pm 0.13_{\text{syst}} \pm 0.17_{\text{theo}}) \times 10^{-3}$$

- In agreement with exclusive world-average

TAGGED $B \rightarrow \pi e \nu$ [arXiv:2206.08102](https://arxiv.org/abs/2206.08102)

- Fit to M_{miss}^2 in three q^2 bins
- Combined fit to BCL expansion and form-factor LQCD constraints

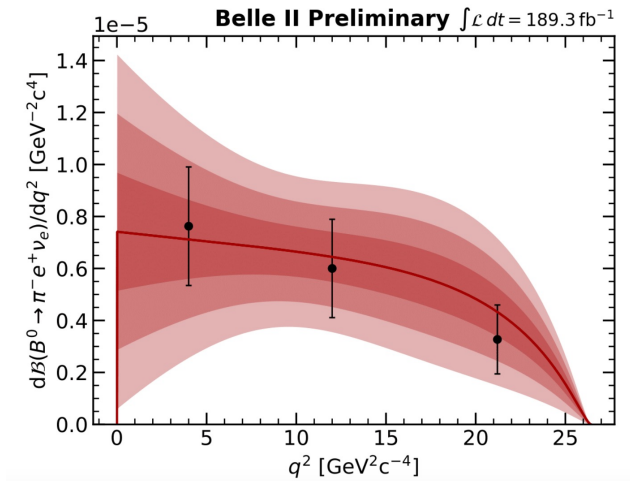
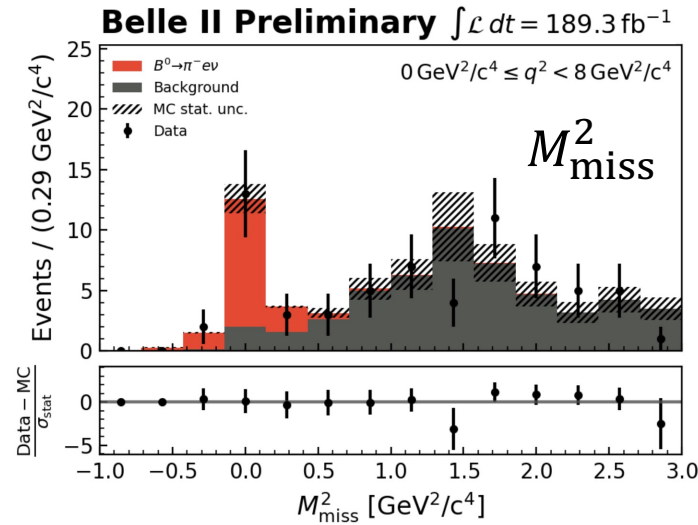


TAGGED $B \rightarrow \pi e \nu$ [arXiv:2206.08102](https://arxiv.org/abs/2206.08102)

- Fit to M_{miss}^2 in three q^2 bins
- Combined fit to BCL expansion and form-factor LQCD constraints

$$|V_{ub}| = (3.88 \pm 0.45_{\text{tot}}) \times 10^{-3}$$

- In agreement with exclusive average



TAGGED $B \rightarrow \pi e \nu$ [arXiv:2206.08102](https://arxiv.org/abs/2206.08102)

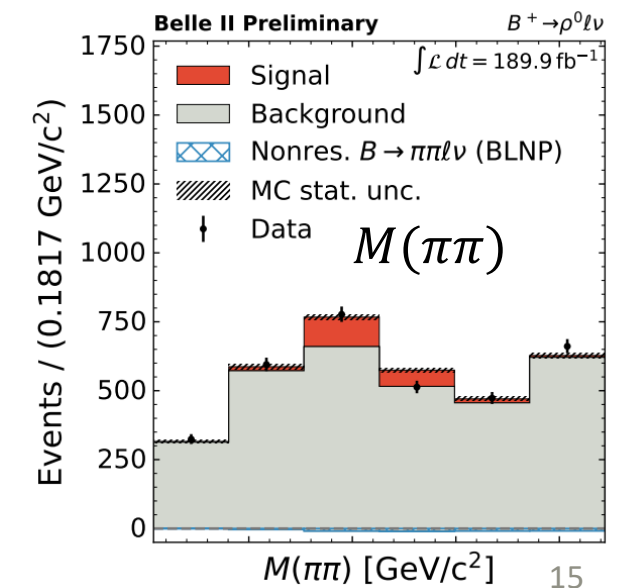
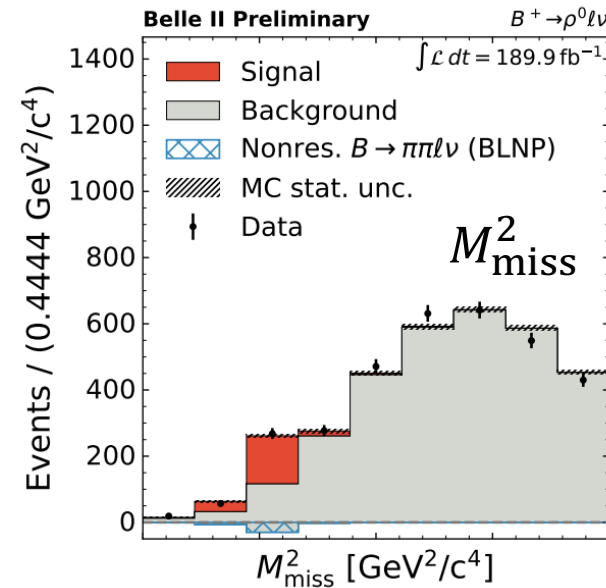
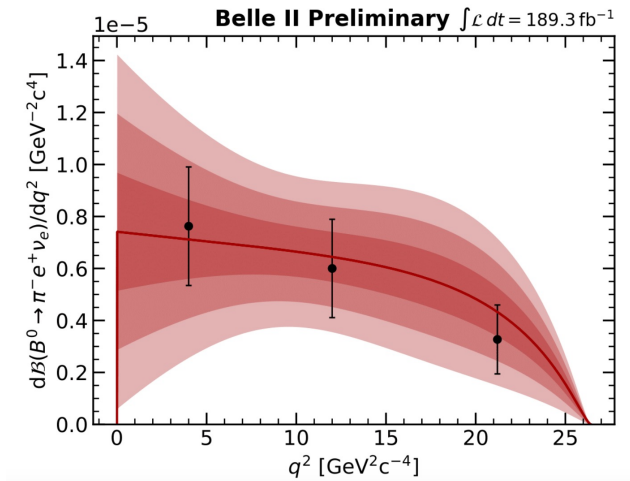
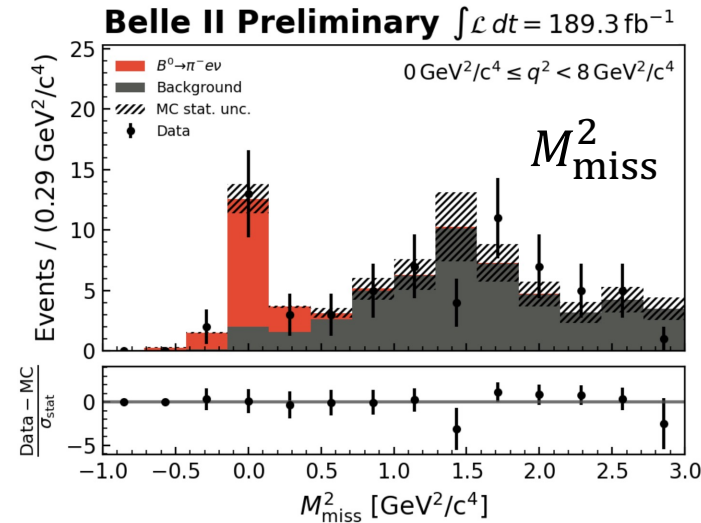
- Fit to M_{miss}^2 in three q^2 bins
- Combined fit to BCL expansion and form-factor LQCD constraints

$$|V_{ub}| = (3.88 \pm 0.45_{\text{tot}}) \times 10^{-3}$$

- In agreement with exclusive average

TAGGED $B \rightarrow \rho l \nu$ [arXiv:2211.15270](https://arxiv.org/abs/2211.15270)

- Fit to M_{miss}^2 and di-pion mass: $M(\pi\pi)$
- Negative nonresonant $B \rightarrow \pi\pi l \nu$ yield



TAGGED $B \rightarrow \pi e \nu$ [arXiv:2206.08102](https://arxiv.org/abs/2206.08102)

- Fit to M_{miss}^2 in three q^2 bins
- Combined fit to BCL expansion and form-factor LQCD constraints

$$|V_{ub}| = (3.88 \pm 0.45_{\text{tot}}) \times 10^{-3}$$

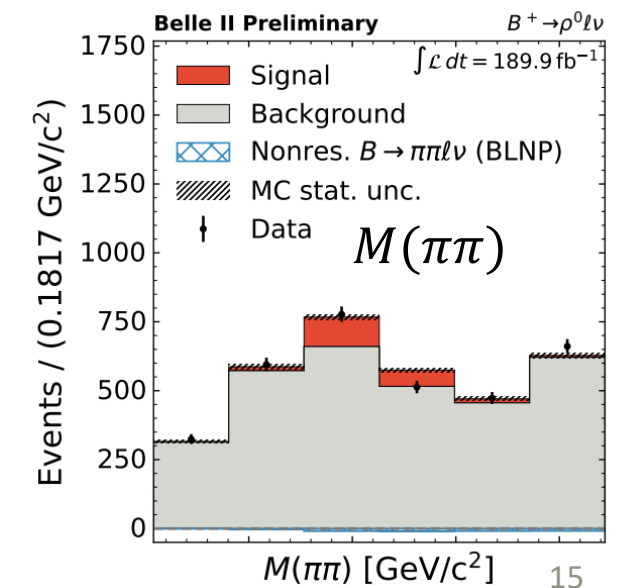
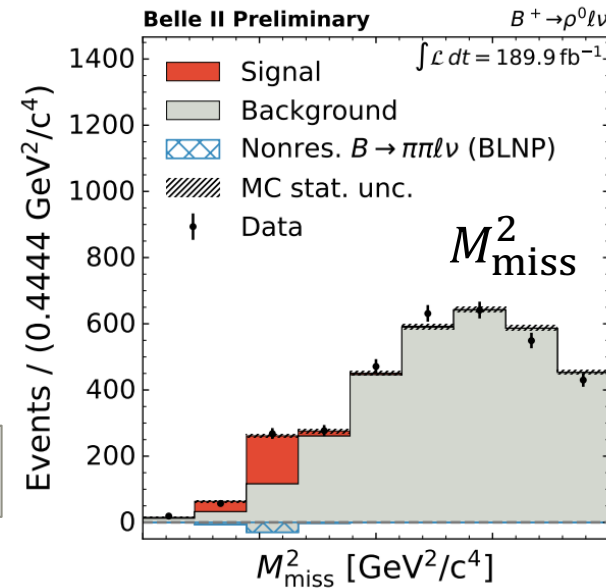
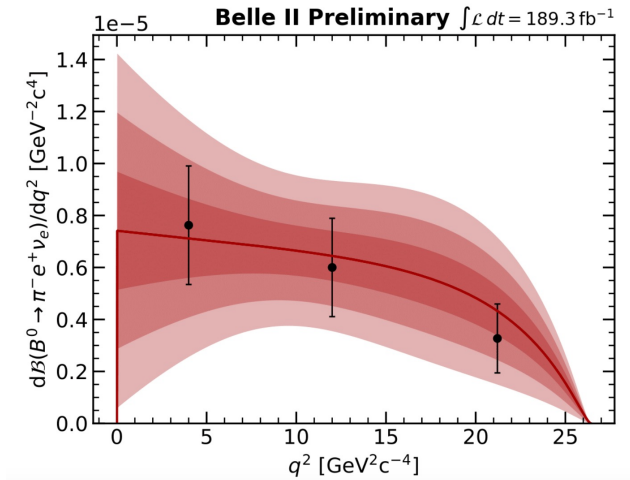
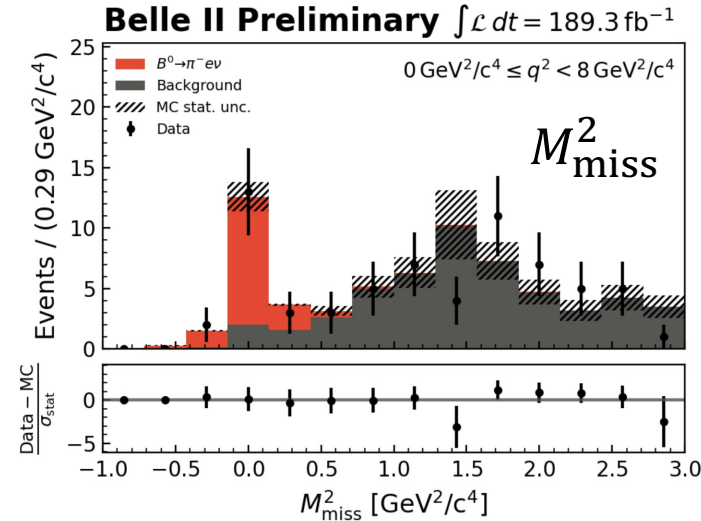
- In agreement with exclusive average

TAGGED $B \rightarrow \rho l \nu$ [arXiv:2211.15270](https://arxiv.org/abs/2211.15270)

- Fit to M_{miss}^2 and di-pion mass: $M(\pi\pi)$
- Negative nonresonant $B \rightarrow \pi\pi l \nu$ yield

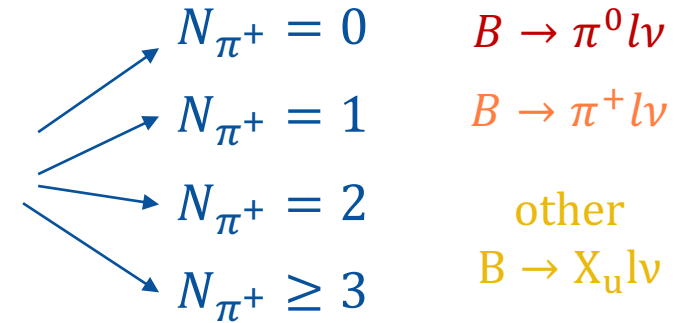
$$\mathcal{B}(B^+ \rightarrow \rho^0 l \nu) = (1.77 \pm 0.23_{\text{stat}} \pm 0.36_{\text{syst}}) \times 10^{-4}$$

- Agrees with world-average



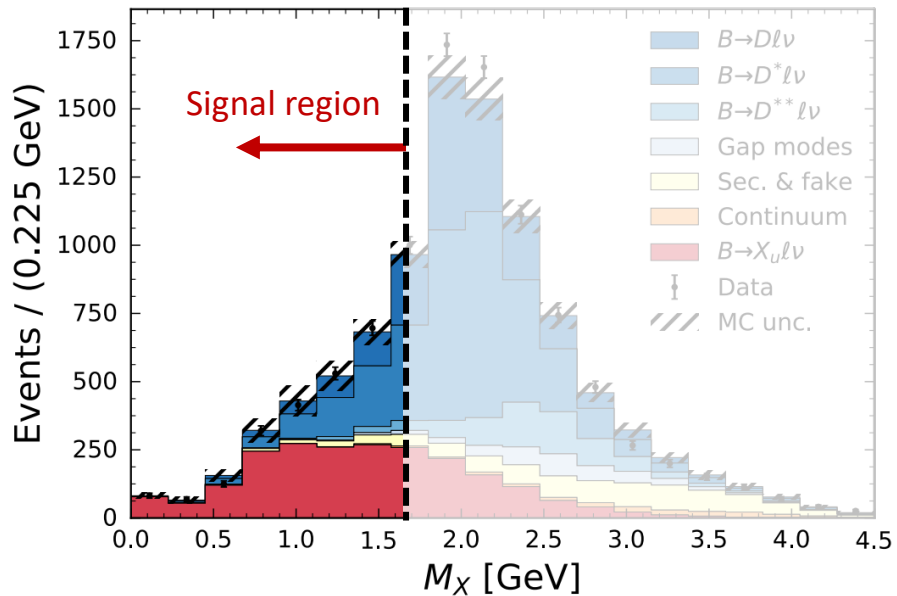
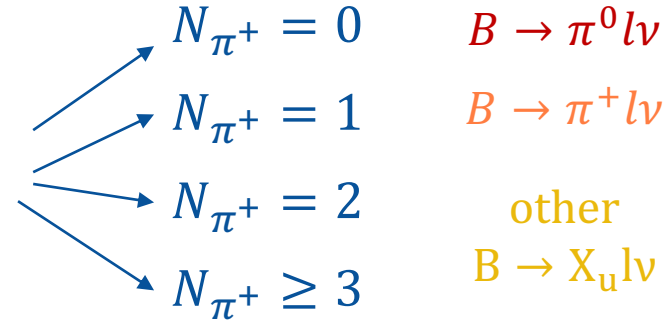
TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLE

- Tagged inclusive reconstruction of $B \rightarrow X_u l \nu$
- New idea: bin events by number of charged pions:



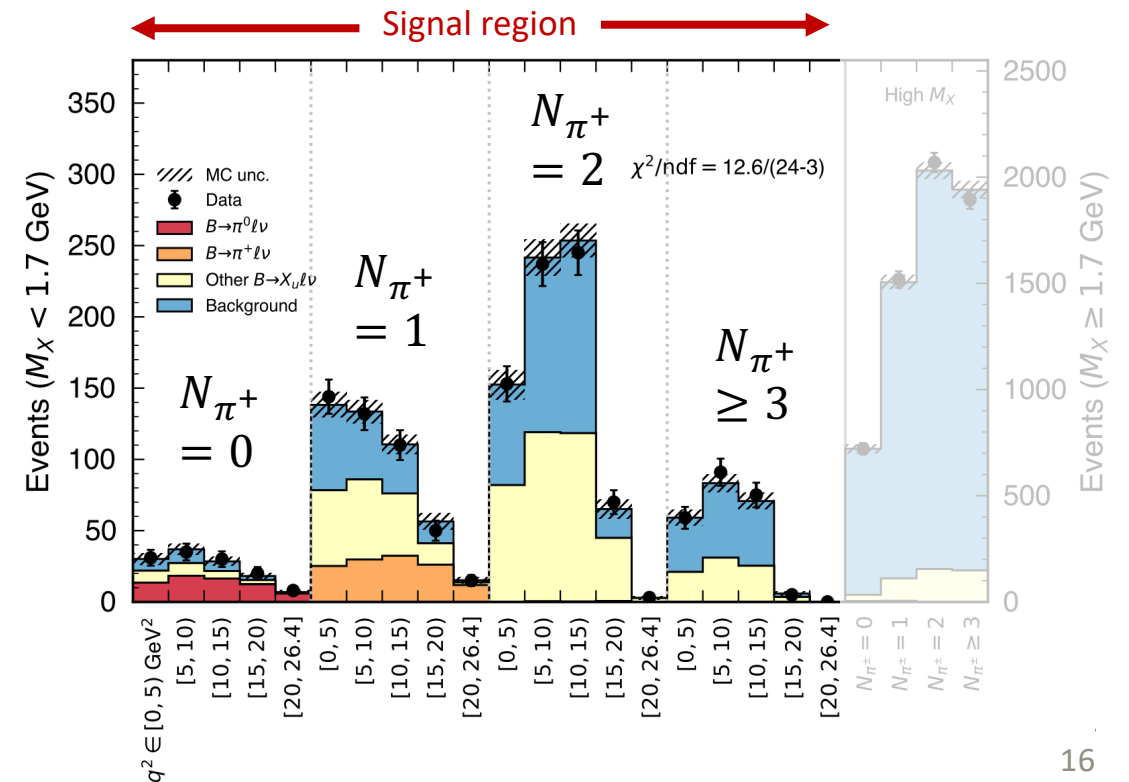
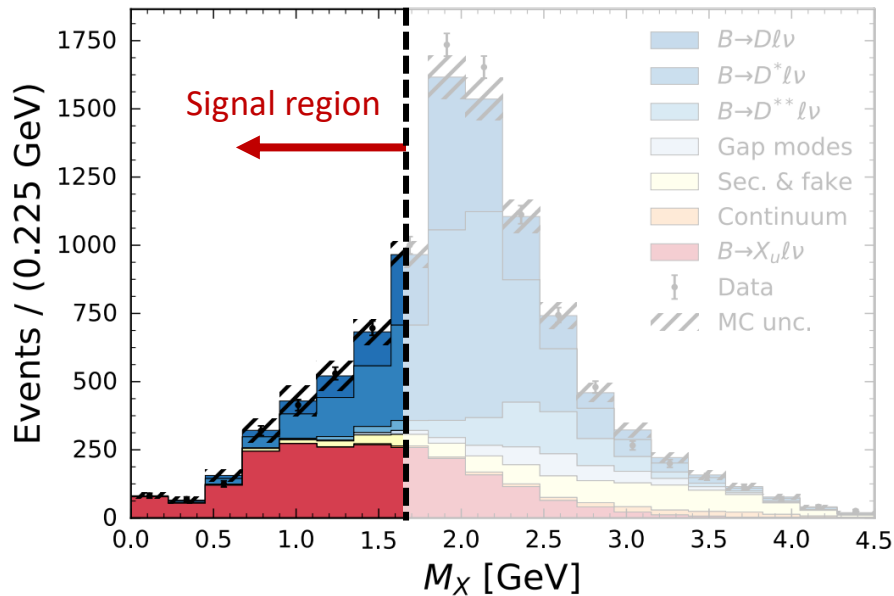
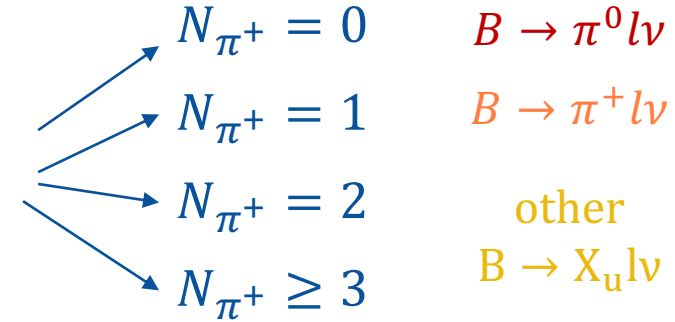
TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLE

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- Signal region selected in hadronic mass: M_X



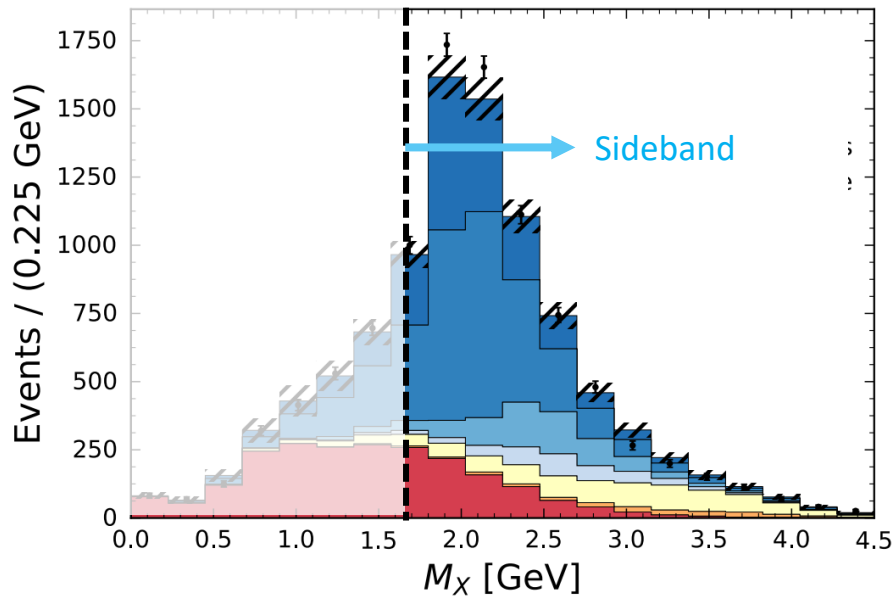
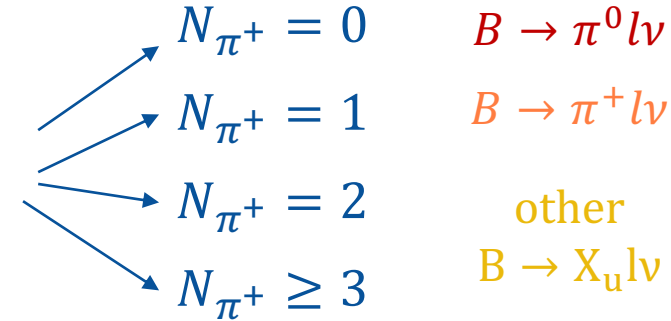
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- Extract signal yields in 2D fit of q^2 and N_{π^+}

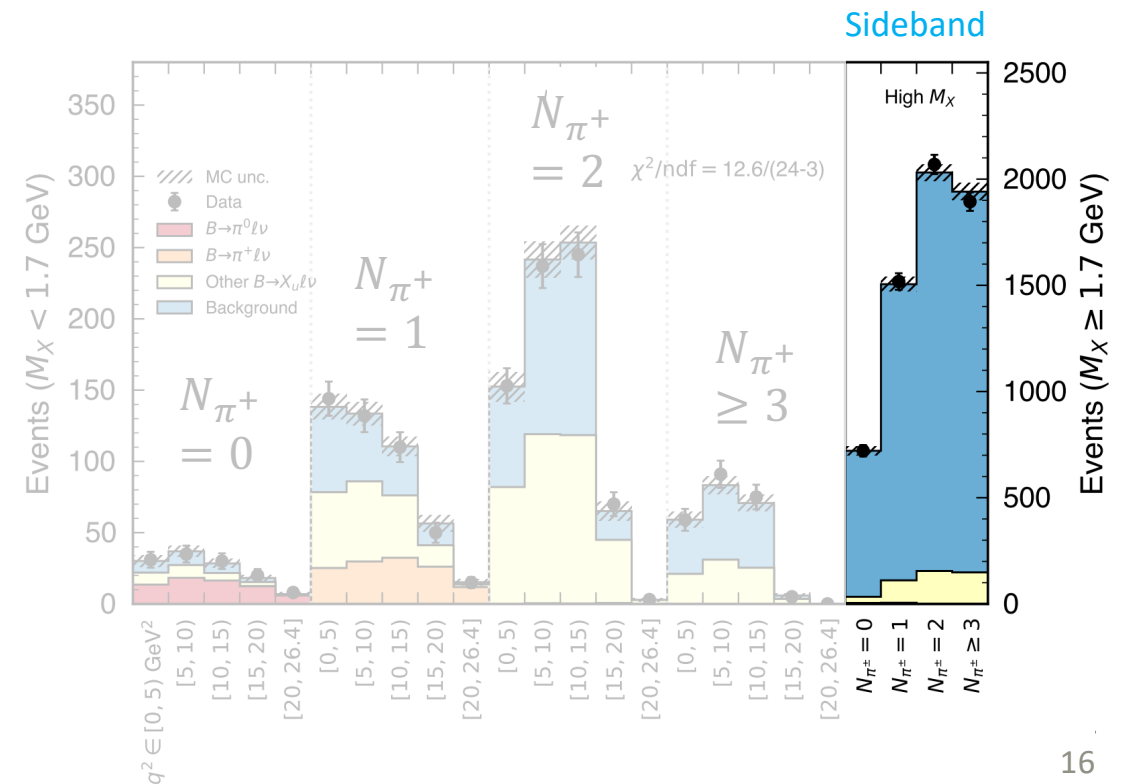


TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLE

- Tagged inclusive reconstruction of $B \rightarrow X_u l \nu$
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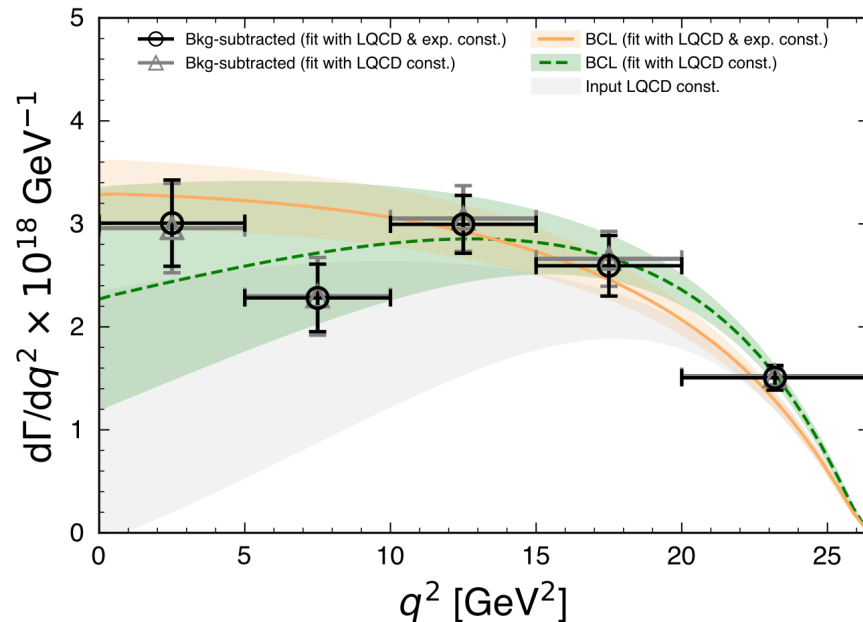


Use high M_X sideband to constrain background



TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLEExclusive $|V_{ub}|$:

- Float BCL $B \rightarrow \pi l \nu$ FF parameters in fit with two constraining options:
 - FLAG lattice QCD [Eur. Phys. J. C 82 \(2022\) 869](#)
 - FLAG + experimental information

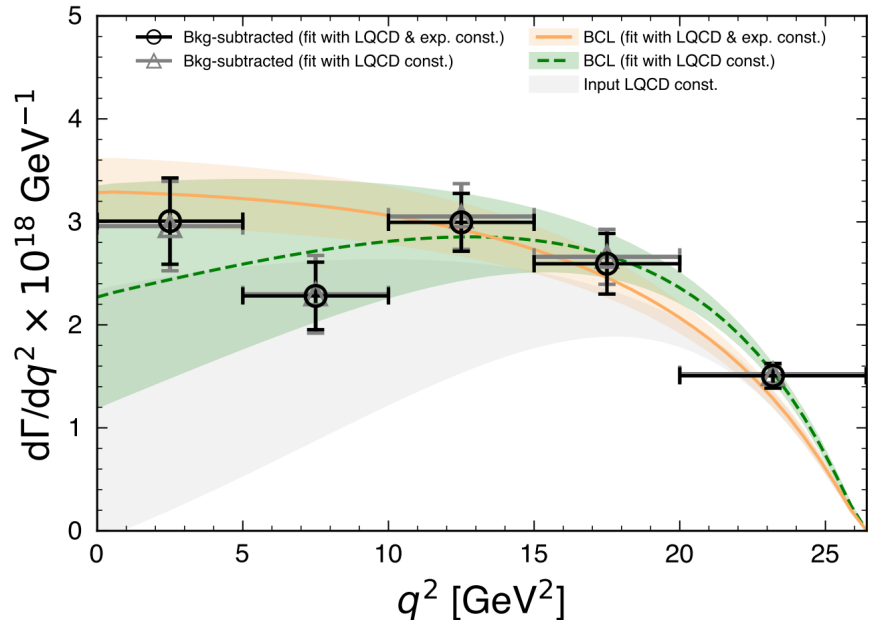


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Inclusive $|V_{ub}|$:

- Use theoretical prediction of inclusive partial rate from GGOU [JHEP 10 \(2007\) 58](#)



TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLEExclusive $|V_{ub}|$:

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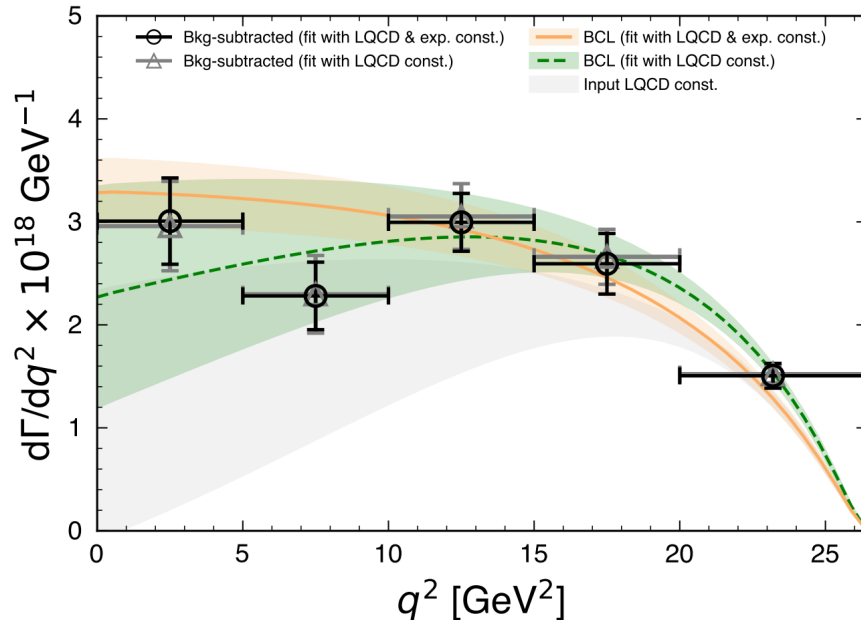
- FLAG lattice QCD [Eur. Phys. J. C 82 \(2022\) 869](#)
- FLAG + experimental information 

Inclusive $|V_{ub}|$:

– Use theoretical prediction of inclusive partial rate from GGOU [JHEP 10 \(2007\) 58](#)

$$|V_{ub}^{\text{excl}}| = (3.78 \pm 0.23_{\text{stat}} \pm 0.16_{\text{syst}} \pm 0.14_{\text{theo}}) \times 10^{-3}$$

$$|V_{ub}^{\text{incl}}| = (3.90 \pm 0.20_{\text{stat}} \pm 0.32_{\text{syst}} \pm 0.09_{\text{theo}}) \times 10^{-3}$$



TAGGED SIMULTANEOUS EXCL. AND INCL. $|V_{ub}|$ AT BELLE

Exclusive $|V_{ub}|$:

– Float BCL $B \rightarrow \pi l \nu$ FF parameters in fit with two constraining options:

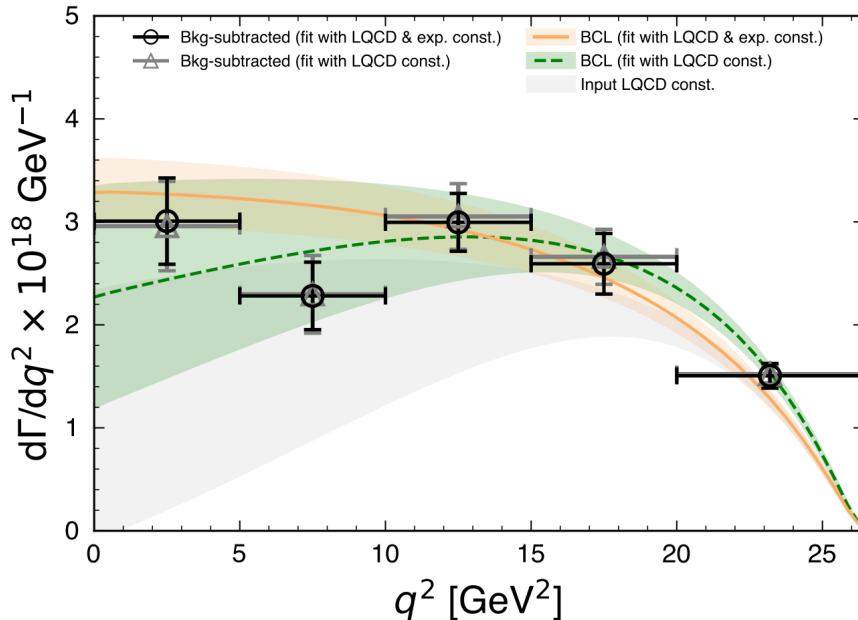
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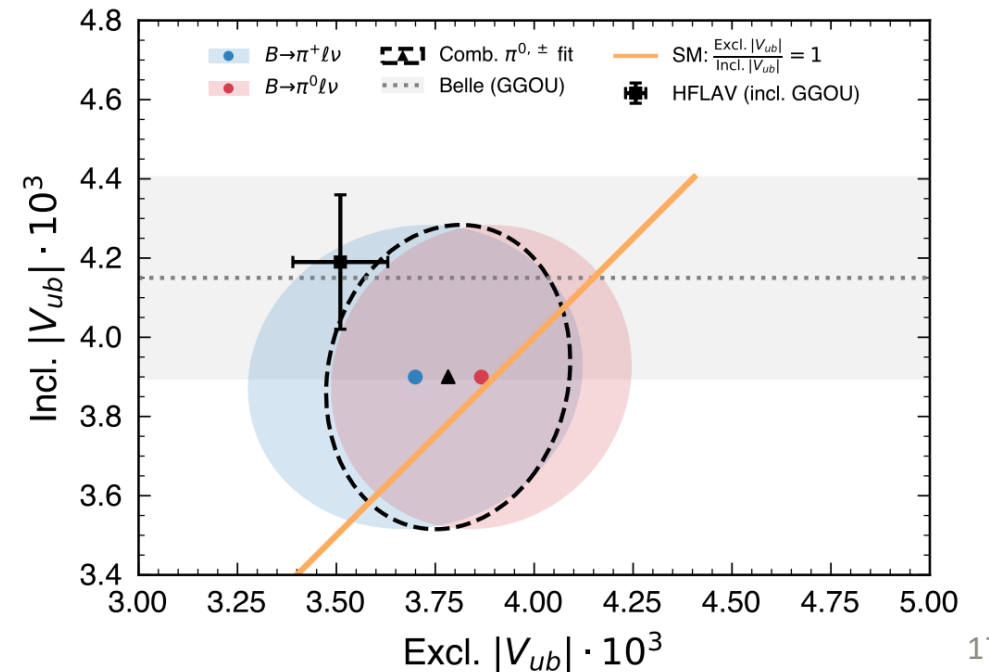
$$|V_{ub}^{\text{excl}}| = (3.78 \pm 0.23_{\text{stat}} \pm 0.16_{\text{syst}} \pm 0.14_{\text{theo}}) \times 10^{-3}$$

$$|V_{ub}^{\text{incl}}| = (3.90 \pm 0.20_{\text{stat}} \pm 0.32_{\text{syst}} \pm 0.09_{\text{theo}}) \times 10^{-3}$$



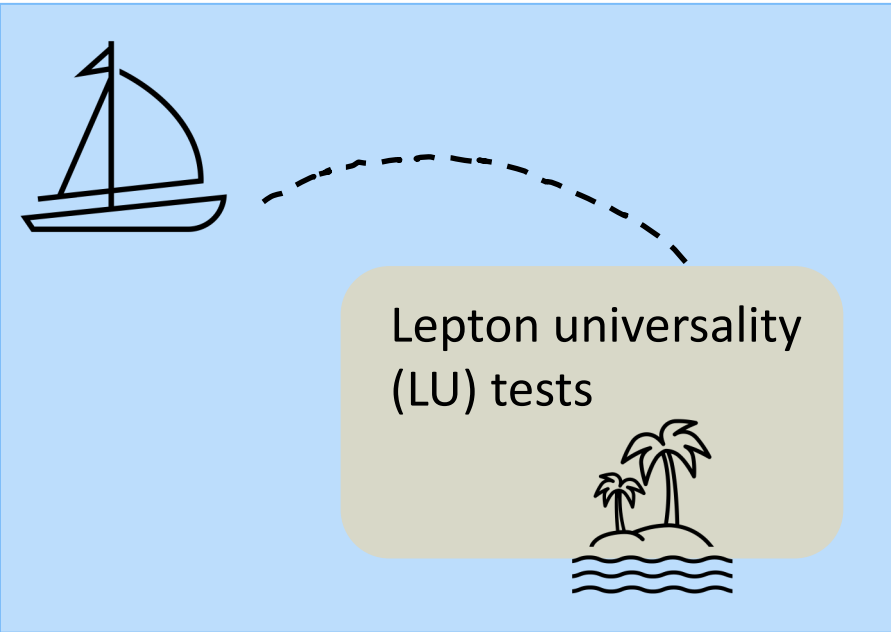
$$\frac{|V_{ub}^{\text{excl}}|}{|V_{ub}^{\text{incl}}|} = 0.97 \pm 0.12_{\text{tot}}$$

Agrees with expectation of 1 and within 1.1σ with the world-average



$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}l\nu)}$$

Angular observables



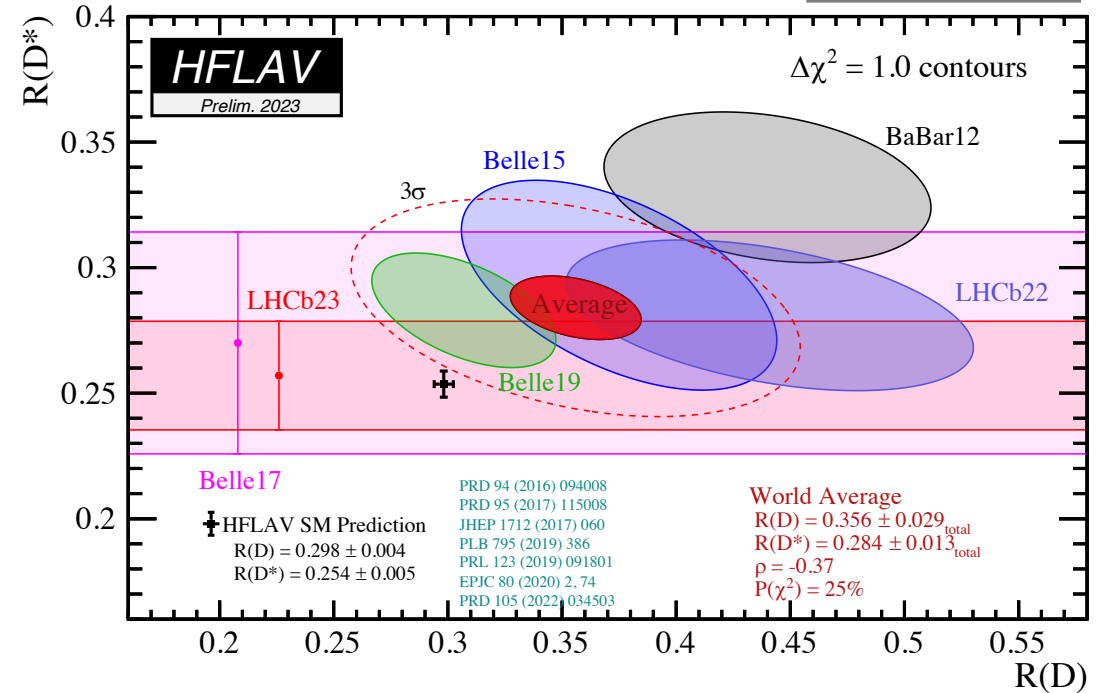
LEPTON UNIVERSALITY (LU)

arXiv:2206.07501

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}l\nu)}$$

Angular observables

Tension with SM at $\approx 3\sigma$



Lepton universality (LU) tests



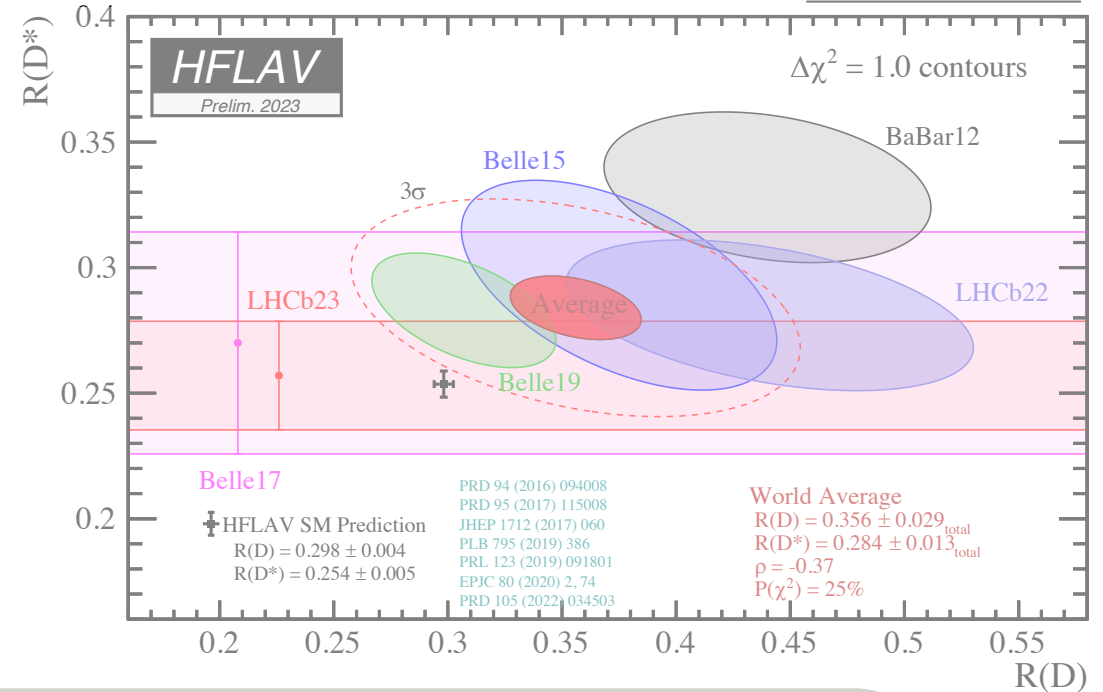
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Lepton universality (LU) tests



LU test in tagged $B \rightarrow Xl\nu$ at Belle II

Tagged $B \rightarrow D^{(*)}\pi(\pi)l\nu$ at Belle

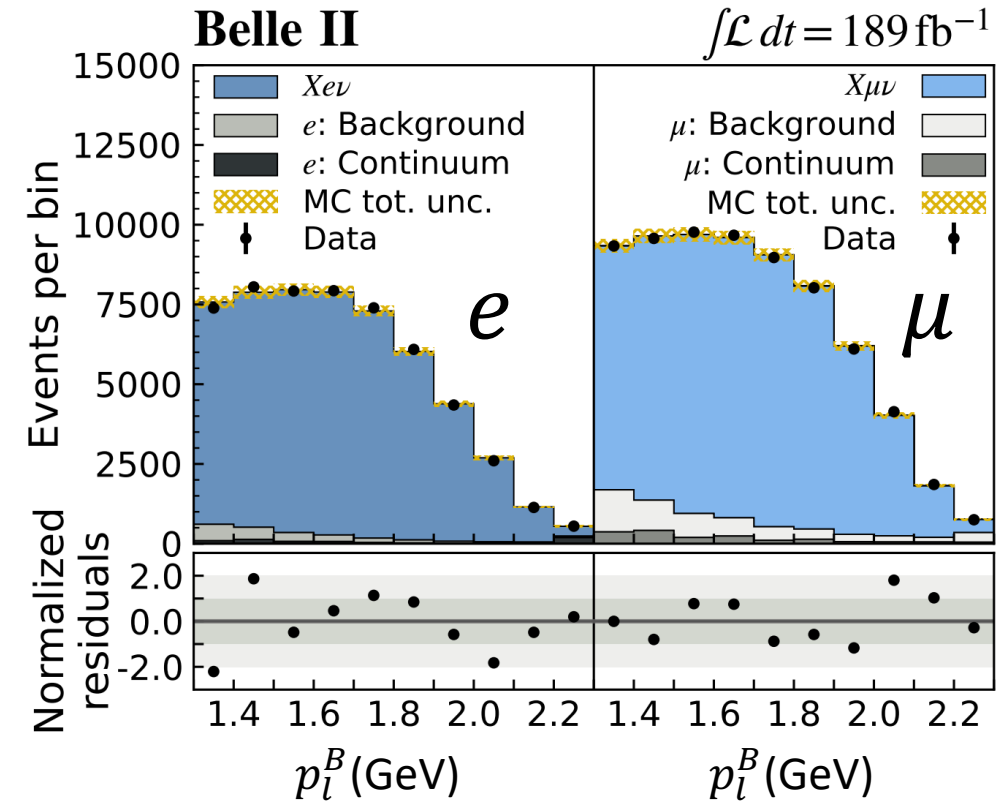
Angular observables in tagged $B \rightarrow D^*l\nu$ at Belle II

LU TEST IN $B \rightarrow Xl\nu$ AT BELLE II

- Inclusive test of LFU in tagged semileptonic B decays

$$R(X_{e/\mu}) = \frac{\mathcal{B}(B \rightarrow Xe\nu)}{\mathcal{B}(B \rightarrow X\mu\nu)}$$

- Fit lepton momentum in B frame ($p_l^B > 1.3$ GeV)
- Constrain continuum + background from sideband



LFU TEST IN $B \rightarrow Xl\nu$ AT BELLE II

- Inclusive test of LFU in tagged semileptonic B decays

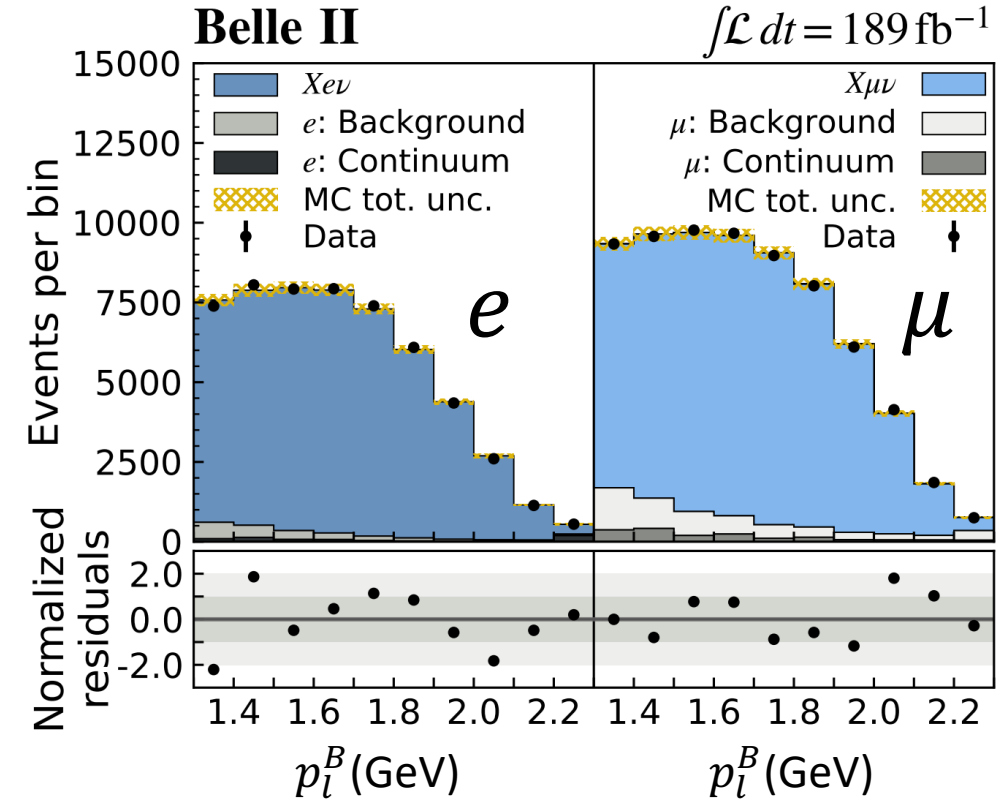
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- Fit lepton momentum in B frame ($p_l^B > 1.3$ GeV)

- Constrain continuum + background from sideband

$$R(X_{e/\mu}) = 1.007 \pm 0.009_{\text{stat}} \pm 0.019_{\text{syst}}$$

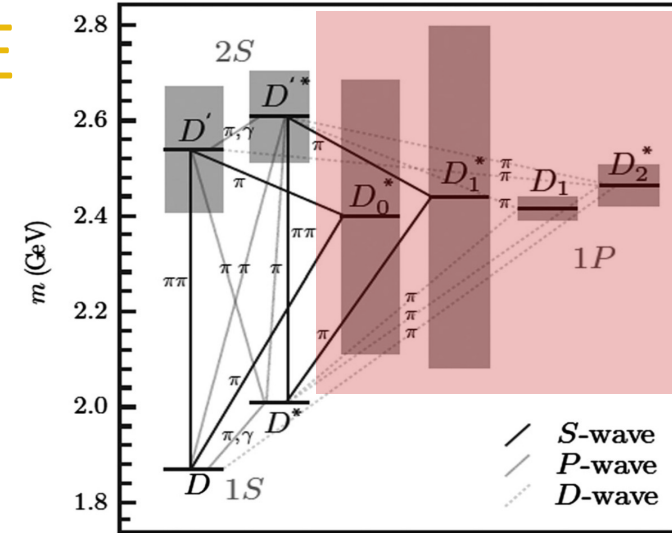
- Compatible with SM prediction [arXiv:2207.03432](https://arxiv.org/abs/2207.03432)
- Most precise BF-based LFU test with semileptonic decays



Source	Uncertainty [%]
Sample size	0.9
Lepton identification	1.9
$Xl\nu$ branching fractions	0.2
$X_c l\nu$ form factors	0.1
Total	2.1

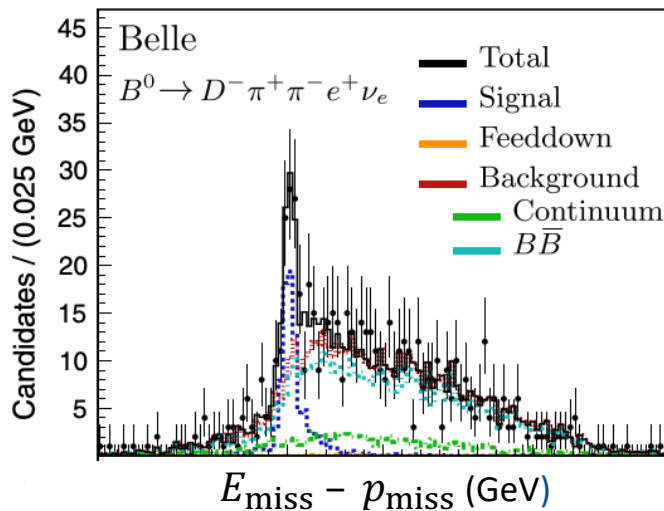
TAGGED $B \rightarrow D^{(*)}\pi(\pi)l\nu$ AT BELLE

- Large uncertainties in $R(D^{(*)})$ measurements from $B \rightarrow D^{**}l\nu$
- 4 orbitally excited charm states that decay into $D^{(*)}\pi$ or $D^{(*)}\pi\pi$
- Determine $\frac{B(B \rightarrow D^{(*)}\pi(\pi)l\nu)}{B(B \rightarrow D^{(*)}l\nu)}$ from unbinned fits to $E_{\text{miss}} - p_{\text{miss}}$



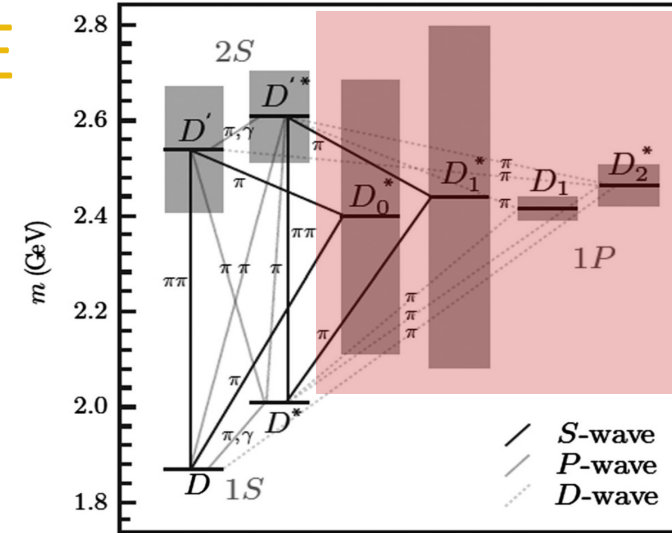
Phys. Rev. D 85 (2012), 094033

One of 16 modes
fit simultaneously:



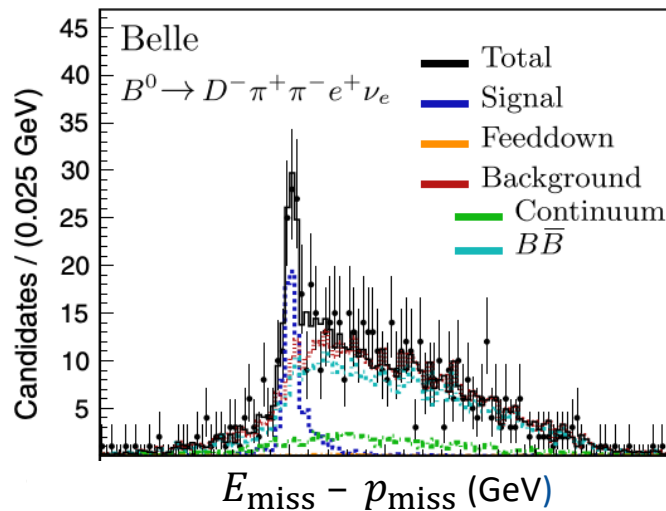
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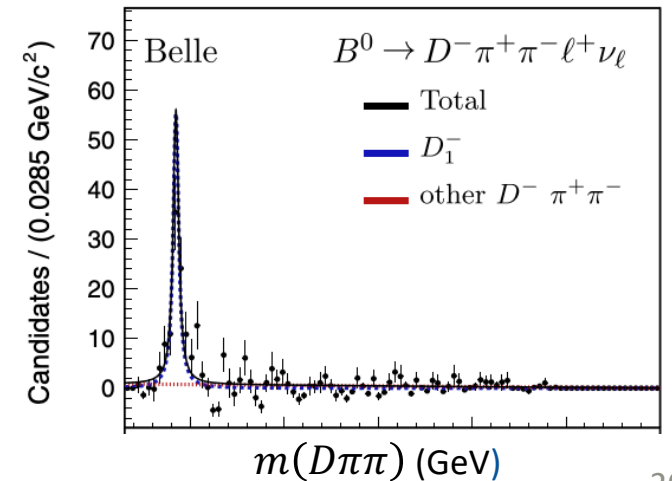
Phys. Rev. D 85 (2012), 094033

One of 16 modes fit simultaneously:



- Subtract background and extract D^{**} contributions from unbinned fit to invariant mass: $m(D^{(*)}\pi(\pi))$

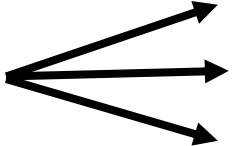
- First observation of $B \rightarrow D_1 l\nu$ with $D_1 \rightarrow D\pi\pi$
- Highest precision $\mathcal{B}(B \rightarrow D^{(*)}\pi(\pi)l\nu)$ to date



ANGULAR ASYMMETRIES IN TAGGED $B \rightarrow D^* l \nu$ AT BELLE II

- Test light LU by measuring angular observables:

$$A_x(w) = \left(\frac{d\Gamma}{dw}\right)^{-1} \left[\int_0^1 - \int_{-1}^0 \right] dx \frac{d^2\Gamma}{dw dx} \longrightarrow \Delta A_x = A_x^e - A_x^\mu$$



 high w
 low w
 inclusive w

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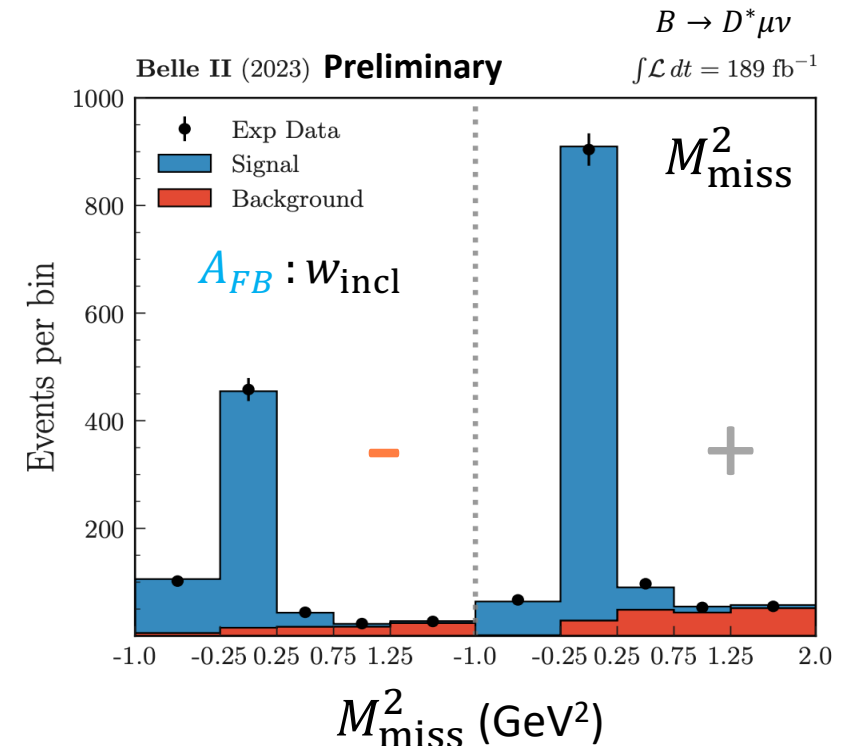
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\downarrow \downarrow \rightarrow \rightarrow \rightarrow

$+$ $-$ $A_{FB}(w): dx \rightarrow d(\cos \theta_l)$ $S_3(w): dx \rightarrow d(\cos 2\chi)$ \dots

\rightarrow high w
 \rightarrow low w
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\downarrow + \downarrow - \rightarrow

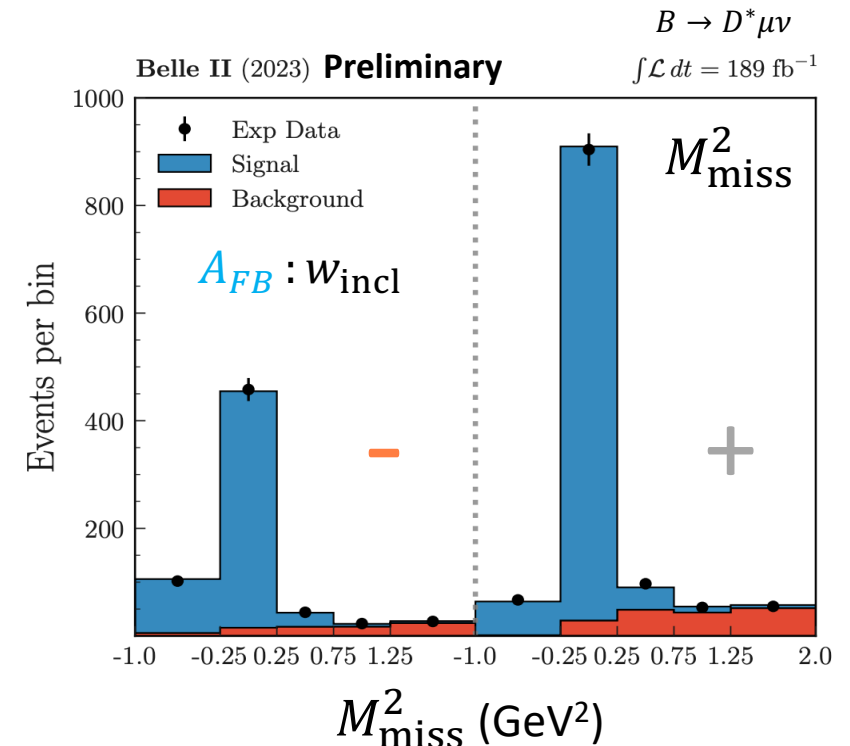
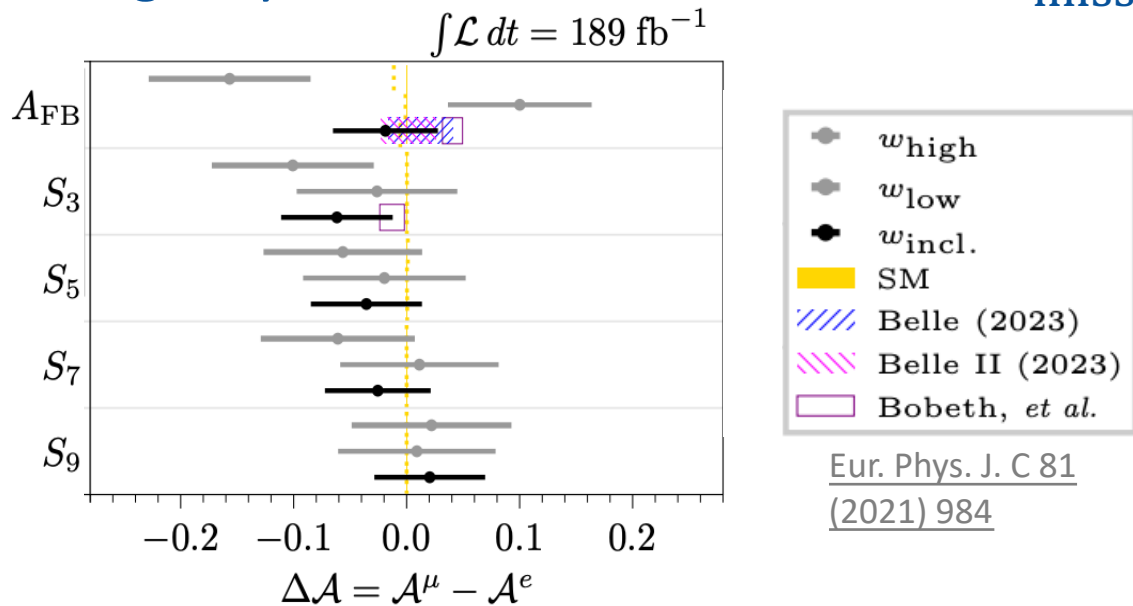
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 ...

\swarrow
high w

\rightarrow
low w

\searrow
inclusive w

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SUMMARY

Precision measurements:

- Most recent $|V_{cb}|$ results from $B \rightarrow D^* l \nu$ shift exclusive closer to inclusive average
- Very active field, with innovation such as simultaneous exclusive and inclusive determination of $|V_{ub}|$



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SUMMARY

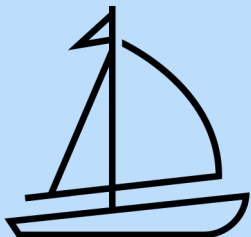
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LU measurements:

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Interested in continuing the journey tomorrow?



Recent Belle II results on the CKM parameters $|V_{cb}|$ and $|V_{ub}|$



- Philipp Horak

Recent Belle II results on semitauonic decays and tests of lepton-flavor universality



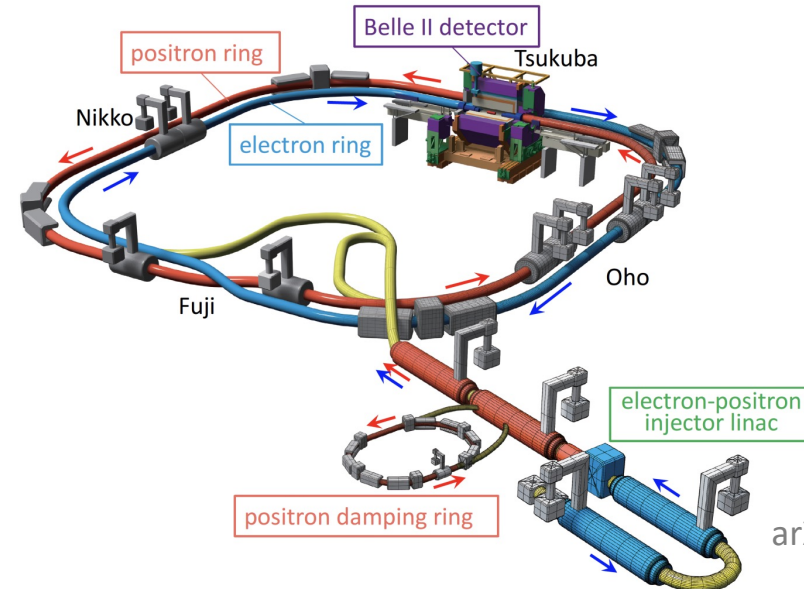
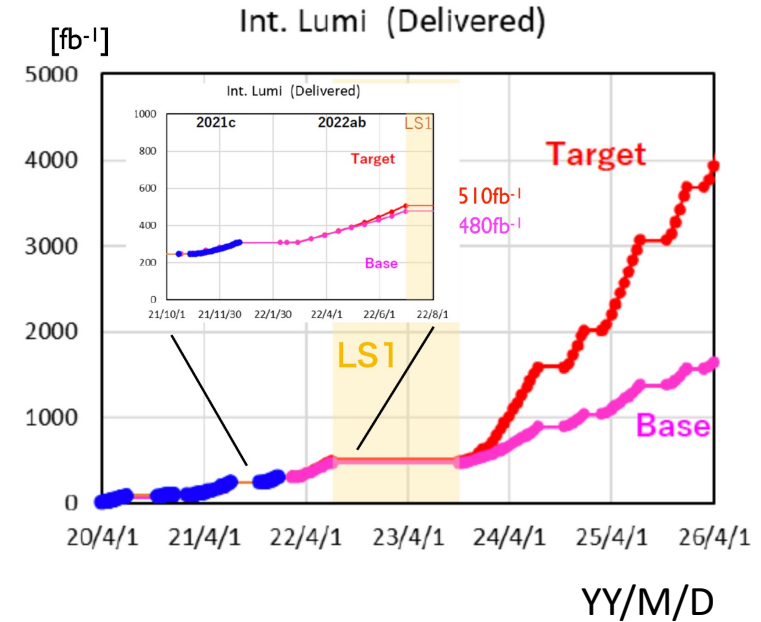
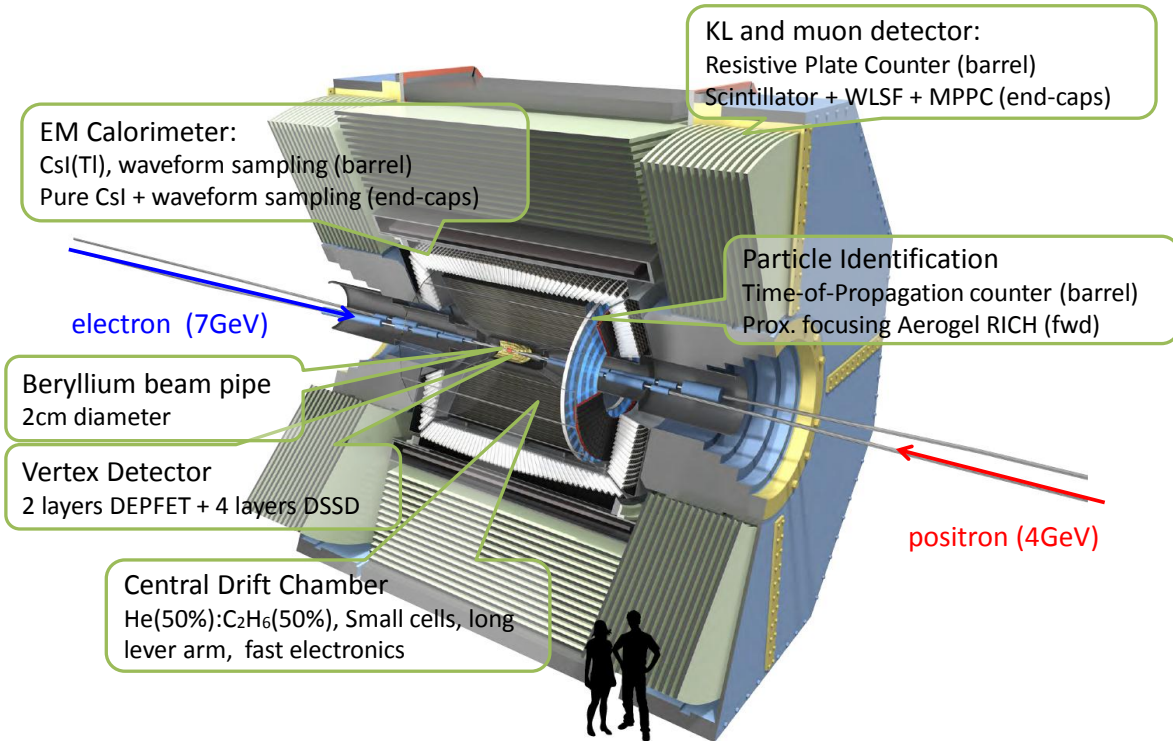
- Peter Lewis

**Thank you for
your attention!**

Backup

SUPERKEKB, BELLE II DETECTOR

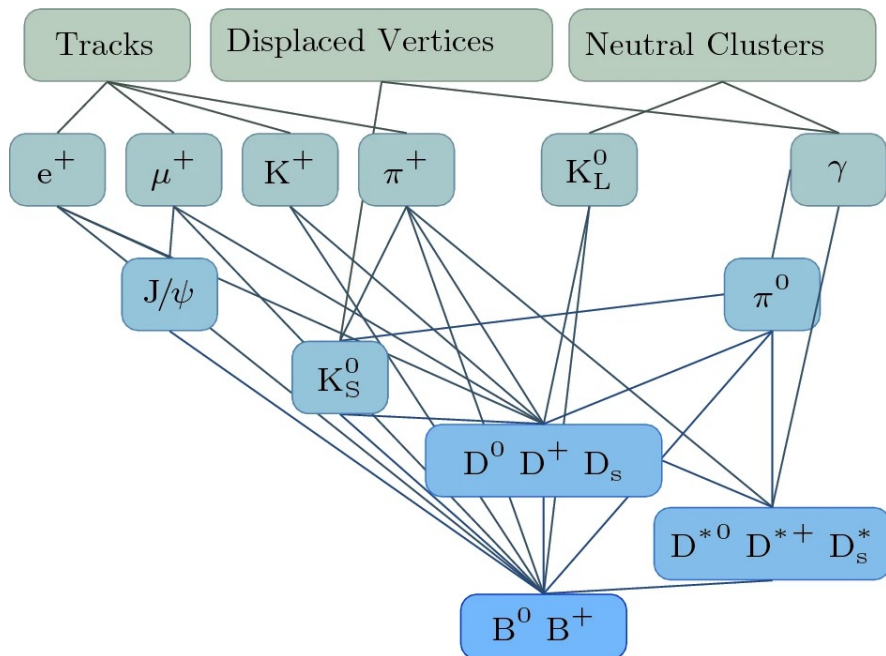
- Now in Long Shutdown 1 (15 months)
- Detector upgrades and beam-pipe improvement



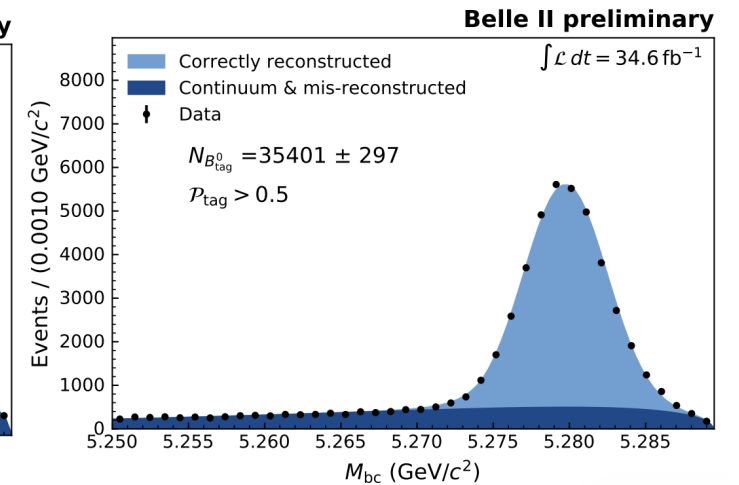
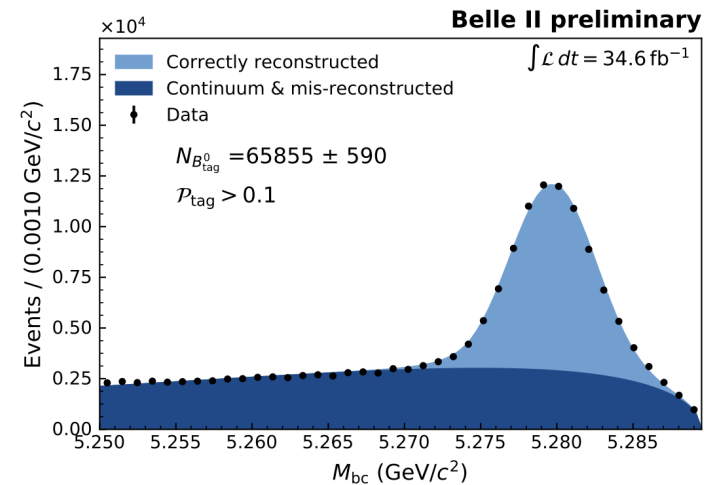
arXiv:1809.01958

- FEI algorithm used to reconstruct B_{tag}
- Uses ≈ 200 BDTs to reconstruct $O(10000)$ different B decay chains
- Assigns signal probability of being correct B_{tag}

Comput Softw Big Sci 3, 6 (2019)

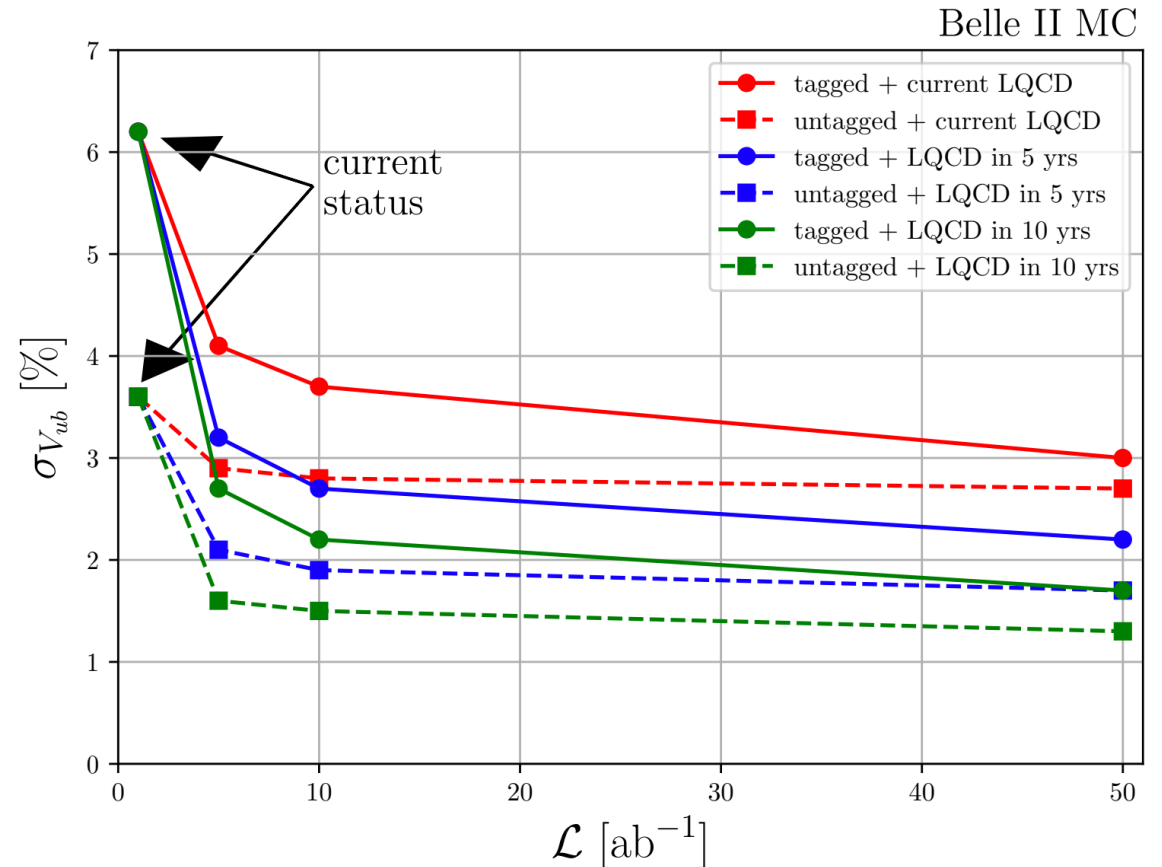


arXiv:2008.060965



Tension:

- Most indications point to inconsistent experimental/theoretical inputs
- Cannot exclude non-SM physics
- Improvements:
 - Theoretical understanding
 - $B \rightarrow X l \nu$ background modeling
 - Calibration of B_{tag} efficiency



arXiv:2207.11275

PROJECTION AT BELLE II: $R(X)$

arXiv:2207.11275

$R(D^{(*)})$:

- Understand $B \rightarrow D^{**} l \nu$ downfeed

$R(X_{\tau/l})$

- Control inclusive background composition

