

Prospects of charm mixing and indirect CPV measurements at Belle II

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On behalf of Belle II collaboration

- **Introduction**
- **Mixing and Indirect CPV in Charm Sector**
 - Brief overview
 - Status so far
 - Prospects with Belle II
- **Summary**

- Mixing in neutral meson

- Their mass eigenstates do not a priori coincide with flavor eigenstates
- ..these states are produced, oscillate and then decay

$$|M_{1,2}\rangle = p|M^0\rangle \pm q|\bar{M}^0\rangle$$

$$|M^0(t)\rangle = f_+(t)|M^0\rangle + \frac{q}{p}f_-(t)|\bar{M}^0\rangle$$

$$|\bar{M}^0(t)\rangle = f_+(t)|\bar{M}^0\rangle + \frac{p}{q}f_-(t)|M^0\rangle$$

$$f_{\pm}(t) = \frac{1}{2}e^{-im_1 t}e^{-\Gamma_1 t/2} \left(1 \pm e^{-i\Delta m t} e^{\Delta\Gamma t/2} \right)$$

$$\begin{aligned} P(M^0(t) \rightarrow M^0) &= P(\bar{M}^0(t) \rightarrow \bar{M}^0) = |f_+(t)|^2 = \frac{1}{2}e^{-\Gamma t} (\cosh(y\Gamma t) + \cos(x\Gamma t)), \\ P(M^0(t) \rightarrow \bar{M}^0) &= \left| \frac{q}{p} \right|^2 |f_-(t)|^2 = \frac{1}{2} \left| \frac{q}{p} \right|^2 e^{-\Gamma t} (\cosh(y\Gamma t) - \cos(x\Gamma t)) \\ P(\bar{M}^0(t) \rightarrow M^0) &= \left| \frac{p}{q} \right|^2 |f_-(t)|^2 = \frac{1}{2} \left| \frac{p}{q} \right|^2 e^{-\Gamma t} (\cosh(y\Gamma t) - \cos(x\Gamma t)) \end{aligned}$$

- Mixing parameters x , and y ; characteristic of neutral meson mixing

$$x = \frac{\Delta m}{\Gamma}, \quad y = \frac{\Delta\Gamma}{2\Gamma},$$

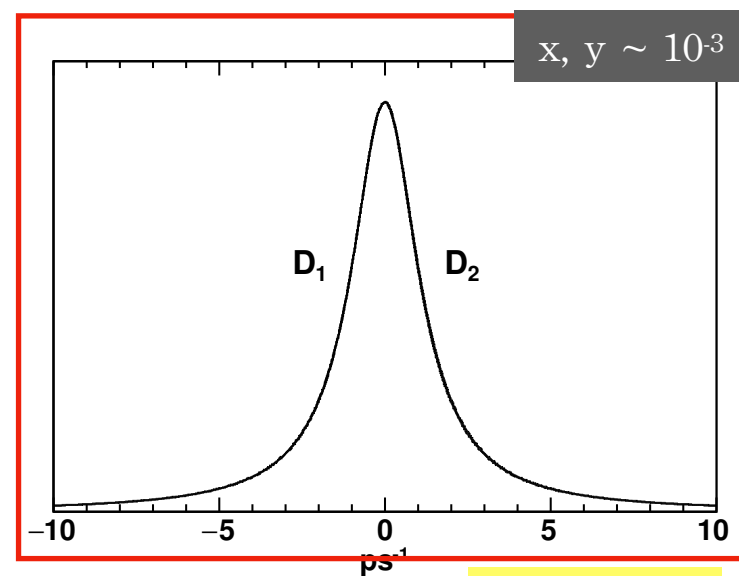
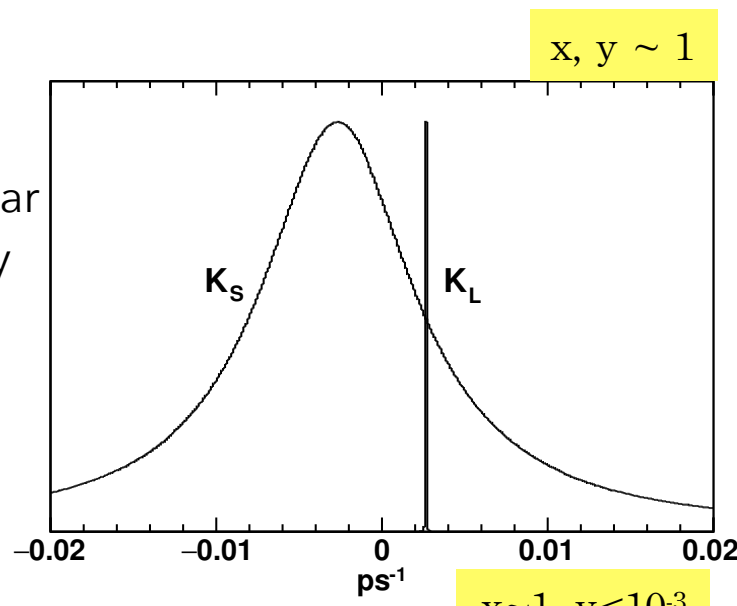
where Δm = mass differences
and $\Delta\Gamma$ = lifetimes differences

$$|M_{1,2}\rangle = p|M^0\rangle \pm q|\bar{M}^0\rangle$$

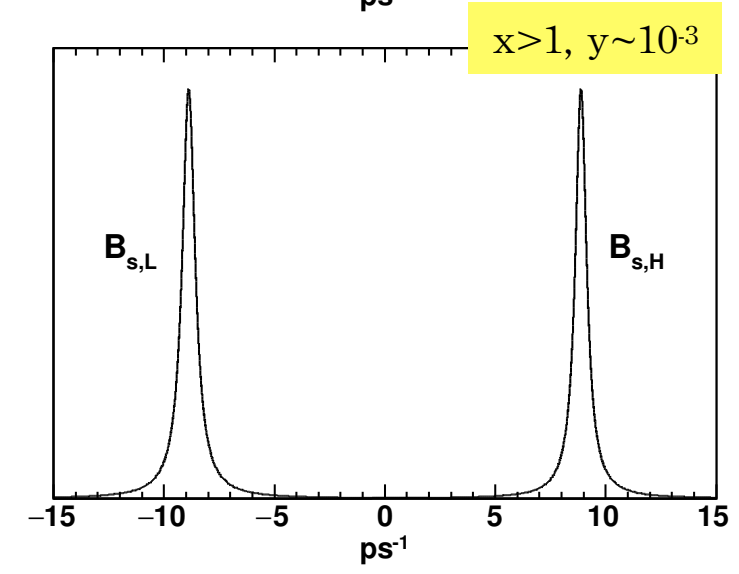
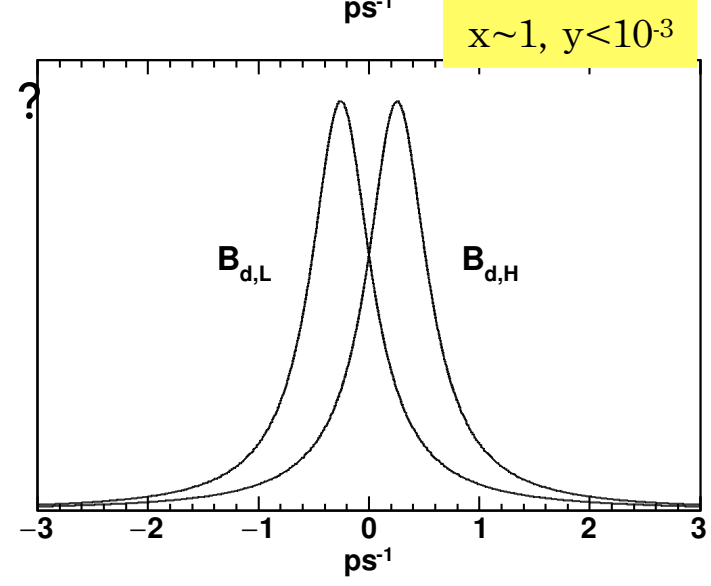
$$x \equiv \Delta m/\Gamma \text{ and } y \equiv \Delta\Gamma/(2\Gamma)$$

4 Mixing in neutral mesons

- Mixing parameters x , and y ;
 - " x " → Rate of oscillation between M and $M\bar{}$
 - " y " → Non-oscillating changes in expo-decay



- What variables we can measure for mixing ?
 - Mixing in CP eigenstates y_{CP}
 - Direct measurement of x and y
 - Mixing rate R
 - Through interference: x'^2 and y'

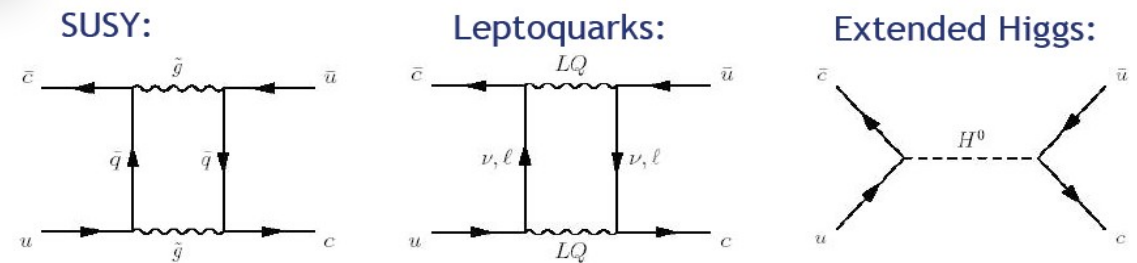


source: Chin.Phys. C38 (2014) 090001.

$$|D_{1,2}\rangle = p|D^0\rangle \mp q|\bar{D}^0\rangle$$

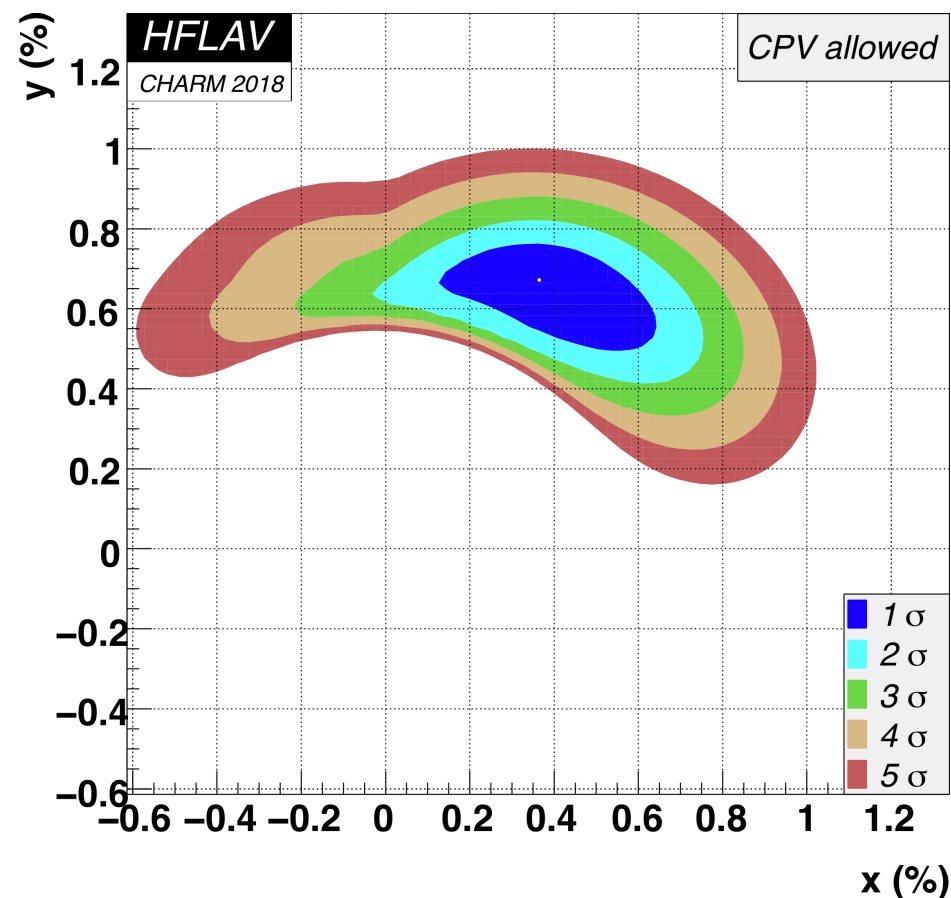
Mixing in charm mesons

- Heavily suppressed (both CKM, and GIM suppressed)
- Small x, y parameters $\sim 10^{-3}$ - 10^{-2}
- Non-SM particles contributing to the box diagram could significantly affect the measured values : **Towards NP**



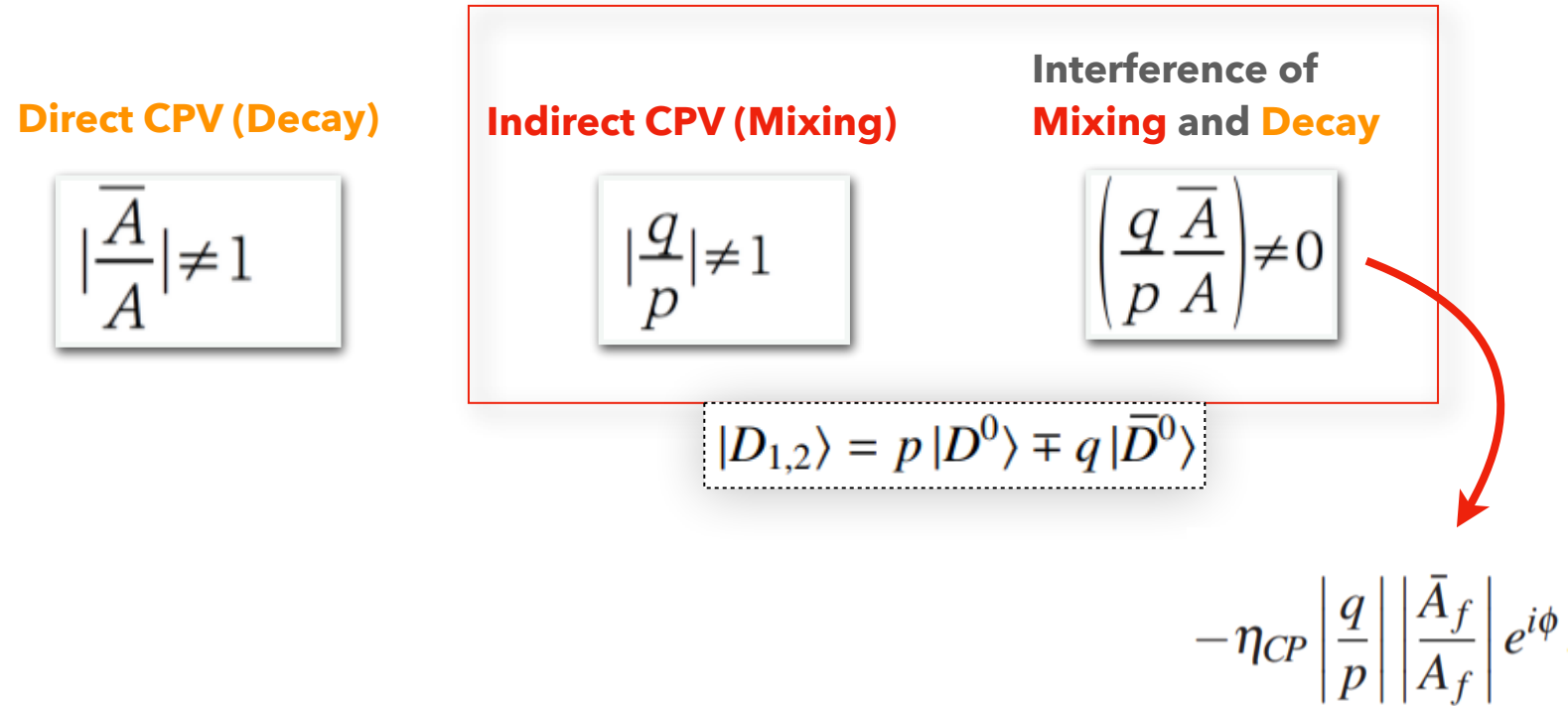
Why mixing measurement need to be improved

- For non-CPV mixing, the theory is limited by "long-distance effects" \rightarrow low-energy QCD.
- For fits allowing for CPV (hope to see more than expected \rightarrow **towards NP**)



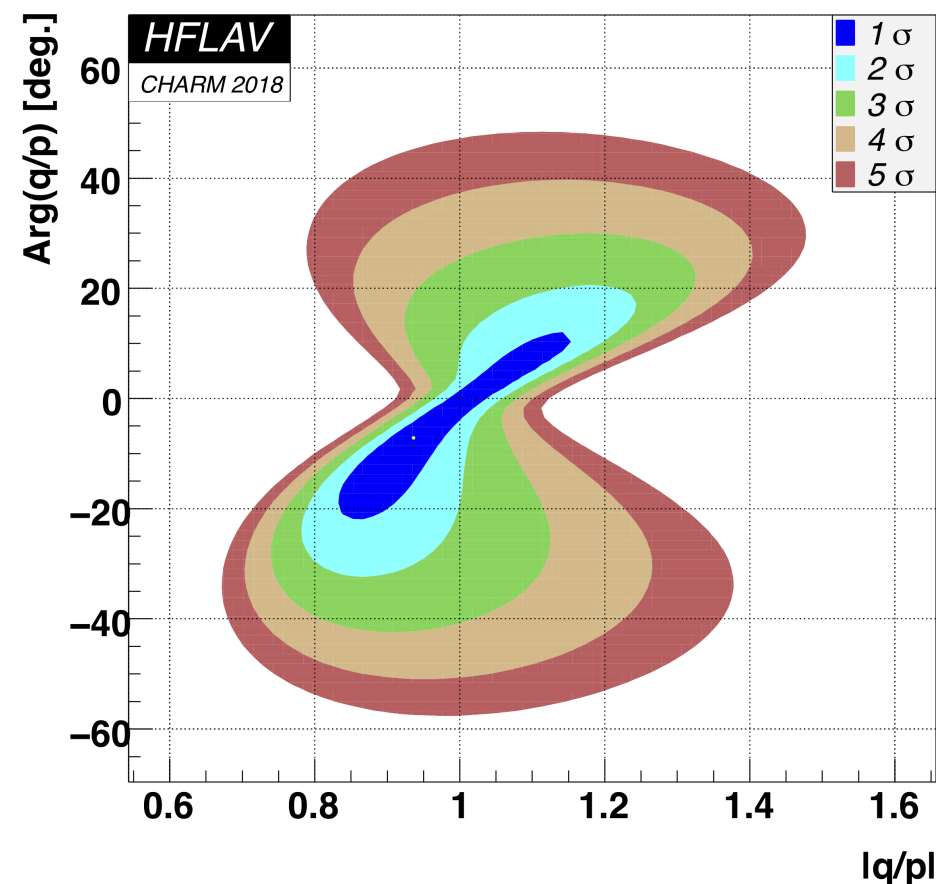
Experiment	Year	\sqrt{s}	$\sigma_{acc}(D^0)$	L	$n(D^0)$
CLEO-c	2003-2008	3.77 GeV	8 nb	0.5 fb^{-1}	4.0×10^6
BESIII	2010-2011	3.77 GeV	8 nb	3 fb^{-1}	2.4×10^7
BaBar	1999-2008	10.6 GeV	1.45 nb	500 fb^{-1}	7.3×10^8
Belle	1999-2010	10.6 – 10.9 GeV	1.45 nb	1000 fb^{-1}	1.5×10^9
CDF	2001-2011	2 TeV	$13 \mu\text{b}$	10 fb^{-1}	1.3×10^{11}
LHCb	2011	7 TeV	1.4 mb	1 fb^{-1}	1.4×10^{12}
LHCb	2012	8 TeV	1.6 mb*	2 fb^{-1}	3.2×10^{12}

Belle II 2017-2022, $L=50 \text{ ab}^{-1}$, and more charm will arrive



- What variables we can measure for indirect CPV ?
 - Direct measurement of $|q/p|$ or ϕ
 - ACP for interference between mixing and decay

- CP violation in charm sector is special !
 - Charm, after strange and beauty (in B^0), where CP violation *remains to be discovered !*
 - Only up-type quark family, where mixing and CPV (may) occur
 - Mixing is heavily suppressed (both CKM, and GIM suppressed)
 - Small x, y parameters $\sim 10^{-3}$ - 10^{-2}
 - Non-SM particles contributing to the box diagram could significantly affect x, y (*NP?*)
 - Study of their oscillations in time can provide insights into CPV in mixing



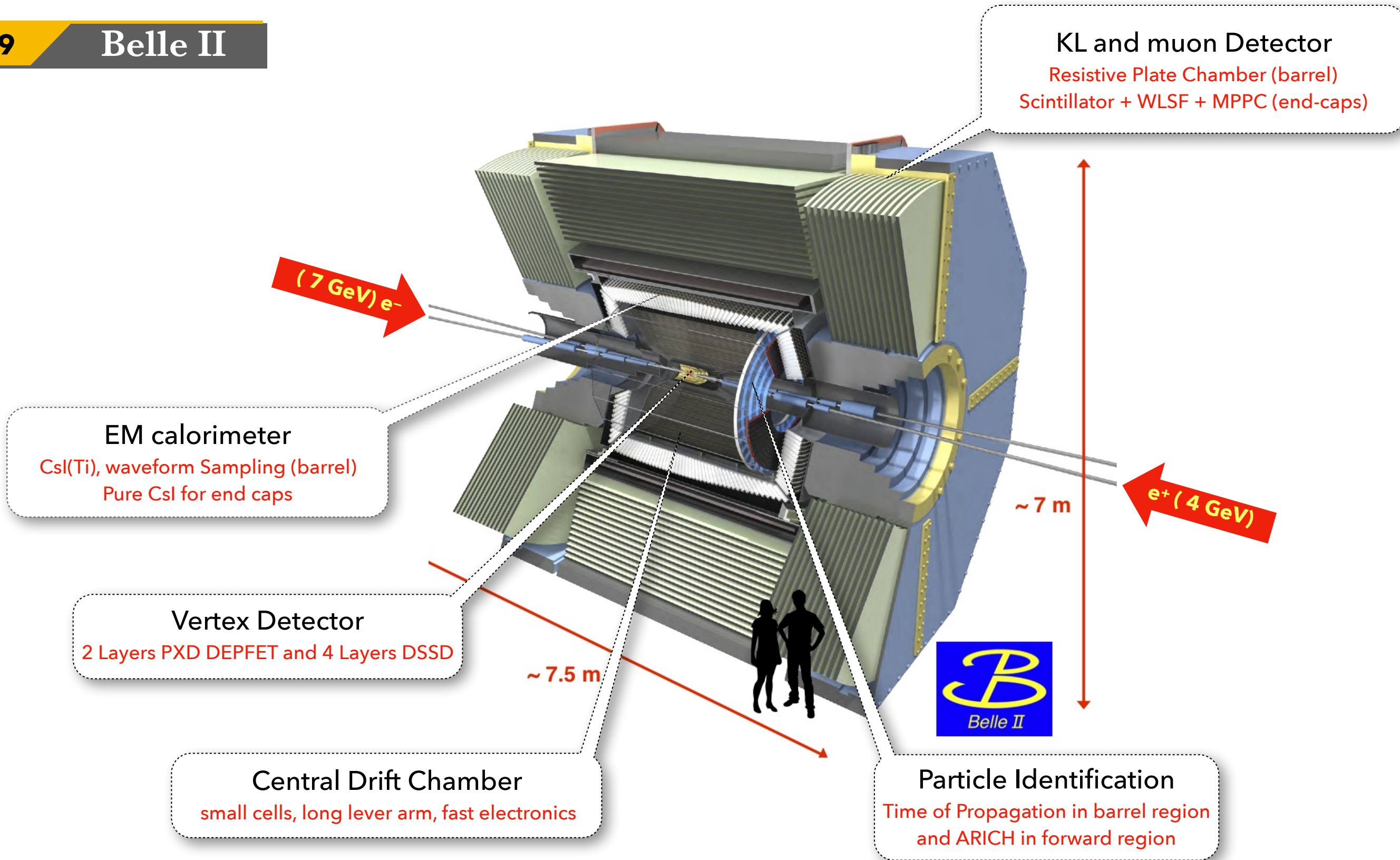
Powerful SuperKEKB

- Provide clean signal of BB pairs; low background with respect to hadron colliders
- Large samples of B and D decays (5×10^{10} pairs of b and c over planned operation)
- Lorentz boost (asymmetric energy) allows precision measurement mixing parameters, and CP violations.
 - Better reconstruction of final states containing photons from particle decays such as π^0 , η etc
 - Straight forward Dalitz plot analyses with low background
 - Many control samples to study systematics

Belle II improvements in view of charm measurement

- **New VXD** of Belle II provides better vertex resolution (for D^0 its around $40 \mu\text{m}$ → next slide)
- IP resolution is improved by **PXD** being at radius of 1.4 cm (better D^0 proper time resolution: next slide)
- Better particle identification w/ upgraded **SVD, CDC, TOP and ARICH**; better K/ π separation (**$D^0 \rightarrow K-\pi^+$**)
- Better reconstruction efficiency with improved tracking efficiency: eg: **$D^* \rightarrow D^0\pi^+$** etc
- More tracking volume from **upgraded CDC and SVD** provides higher K_s efficiency ~ 30%

see more at Belle II TDR: [arXiv: 1011.0352](https://arxiv.org/abs/1011.0352)

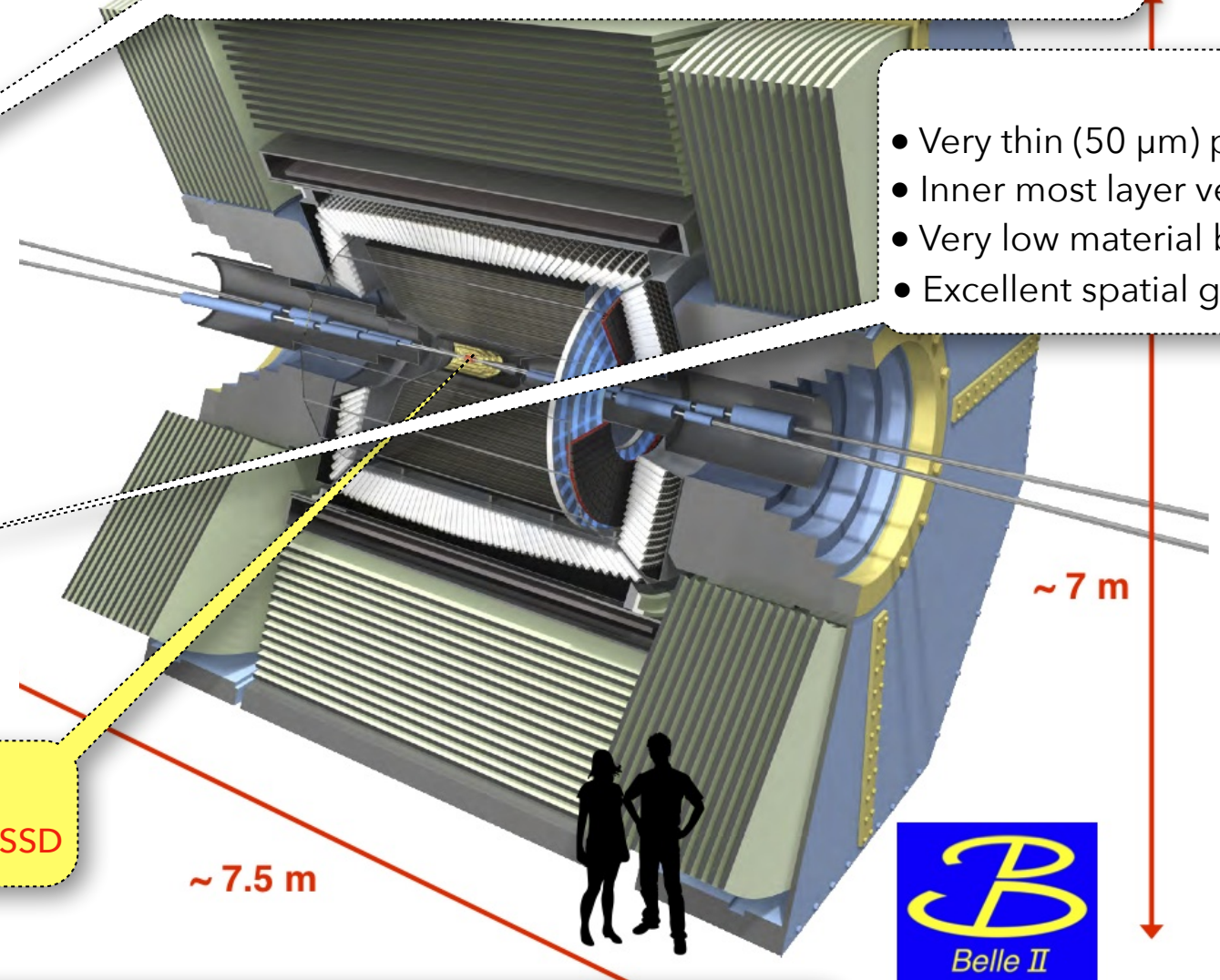
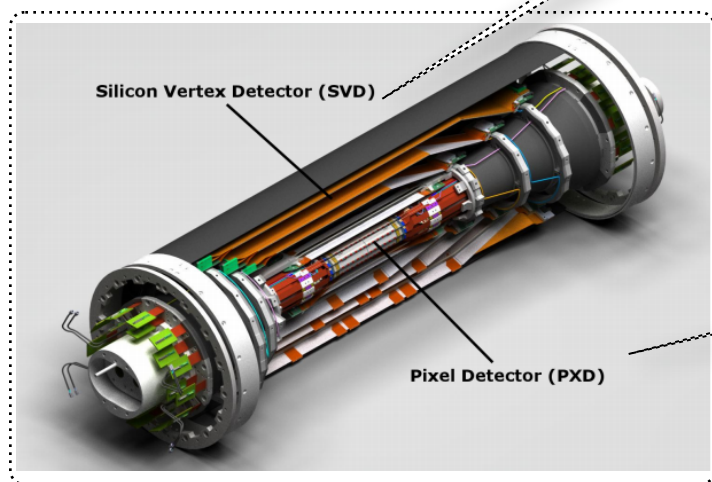


see more at Belle II TDR: [arXiv: 1011.0352](https://arxiv.org/abs/1011.0352)



- SVD**
- Excellent timing resolution ($\sigma \sim 2-3$ ns)
 - Low material budget
 - Larger outer radius (6.05 cm \rightarrow 14 cm)
 - Inner radius: 3.8 cm
 - covers the full Belle II angular acceptance of 17-150 degree

- PXD**
- Very thin (50 μ m) pixel sensor
 - Inner most layer very close to IP ($r = 1.4$ cm)
 - Very low material budget
 - Excellent spatial granularity ($\sigma \leq 15$ μ m)



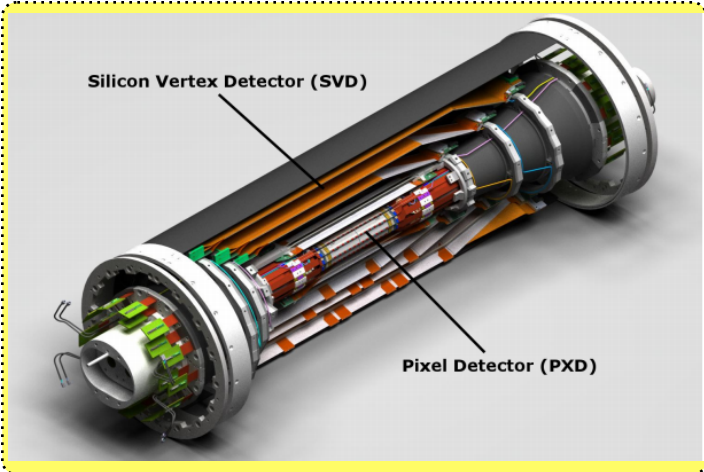
Vertex Detector
2 Layers PXD DEPFET and 4 Layers DSSD



- First run with full vertex detector in early 2019 (Phase 3 of Belle II)
- **Key player for D-mixing sensitivity measurements !**
 - Highly granular pixel sensors provide most accurate 2D position information
 - Reconstruction of primary and secondary vertices of short-lived particles (< 100 μ m from IP)

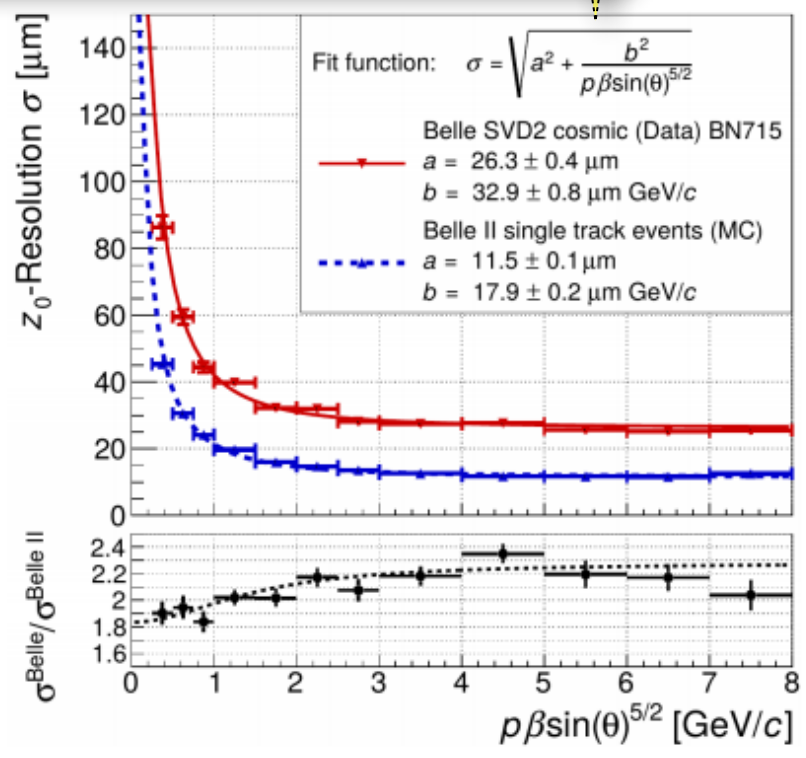
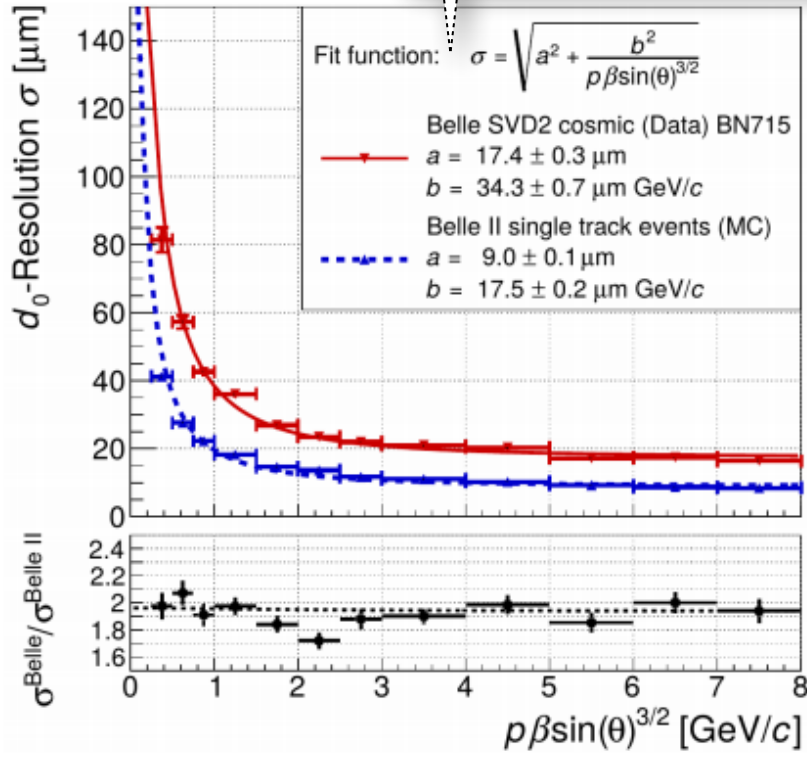
see more at Belle II TDR: arXiv: 1011.0352

11 Vertex performance

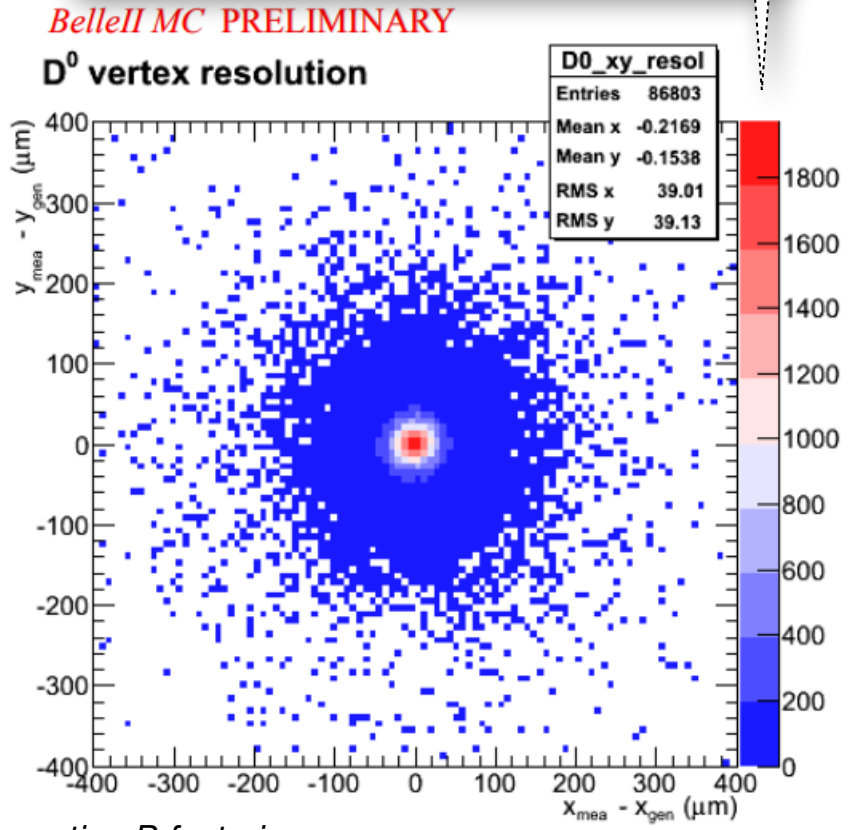


Vertex Detector
2 Layers PXD DEPFET and 4 Layers DSSD

A factor of 2 improvement in "track impact parameter" with respect to Belle



Better vertex resolution ~ 40 micrometers



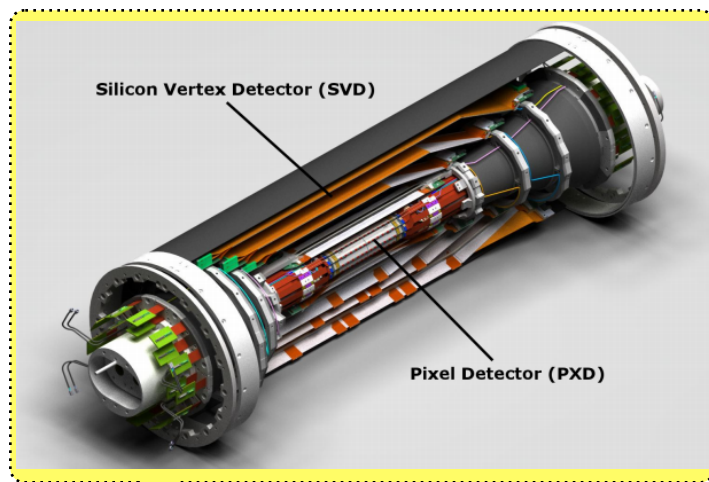
*with respect to previous generation B factories.

see more at Belle II TDR: arXiv: 1011.0352

12 Time resolution

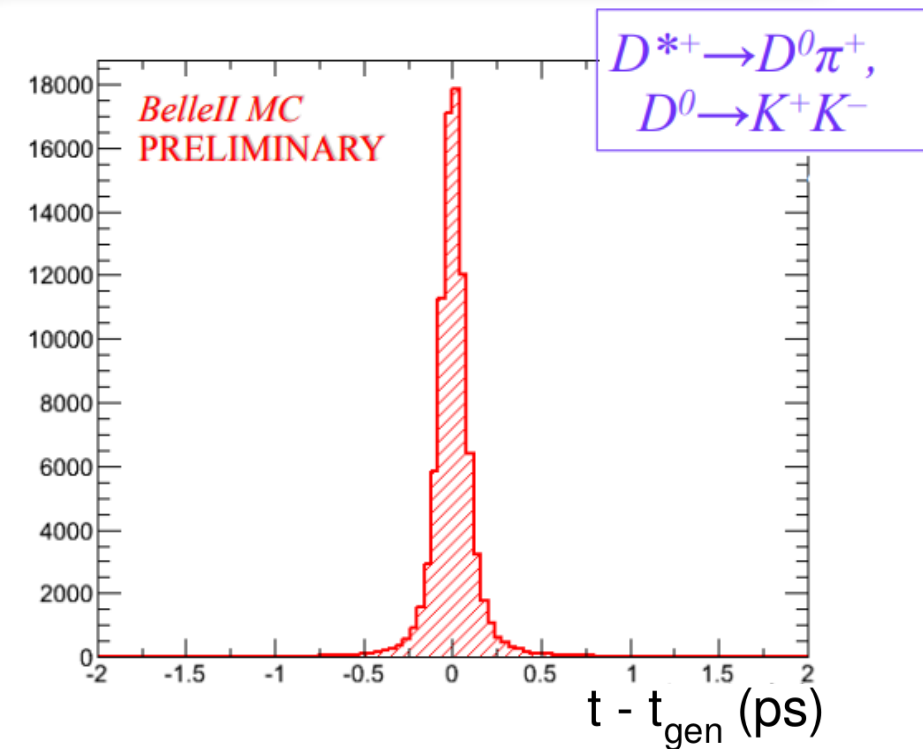
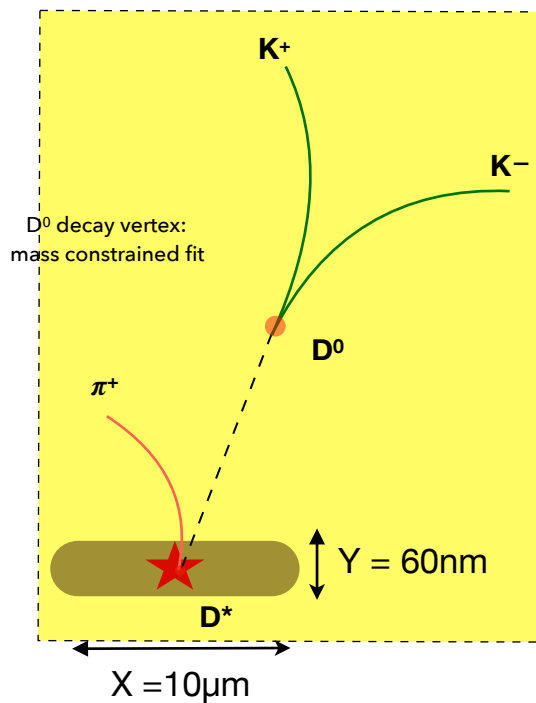


$$t = \frac{l}{\beta\gamma c} = \frac{l m_D}{c |\vec{p}|}$$

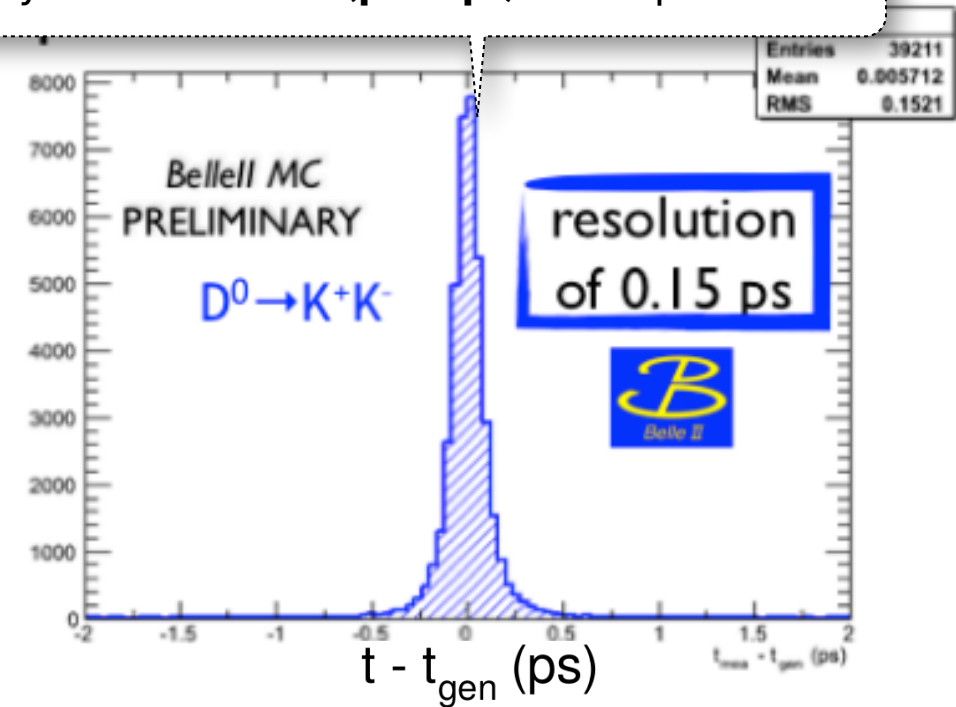
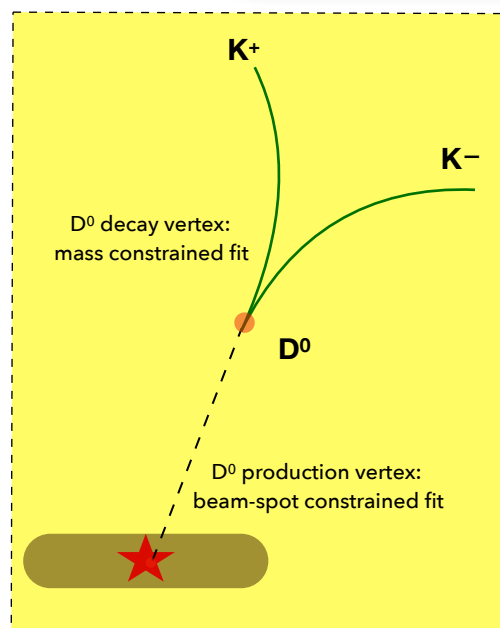


Vertex Detector
2 Layers PXD DEPFET and 4 Layers DSSD

$D \rightarrow hh$ decay time resolution (**D^* tag**) ~ 0.14 ps
-- 2x better than Belle and BaBar



$D \rightarrow hh$ decay time resolution (**prompt**) ~ 0.15 ps



Charm Mixing and Indirect CPV prospects at Belle II

The experimental status of $D^0\bar{D}^0$ mixing and CP violation in different decays.

Decay Type	Final State	LHCb	Belle	BaBar	CDF	CLEO	BES III
DCS 2-body(WS)	$K^+\pi^-$	★	★	●	★	✓	
DCS 3-body(WS)	$K^+\pi^-\pi^0$		✓ _{ACP}	●		✓ _{ACP}	
CP-eigenstate	$K^+K^-, \pi^+\pi^-$	● ^(a) _{ACP}	●	●	✓ _{ACP}	✓	
Self-conjugated 3-body decay	$K_S^0\pi^+\pi^-$	✓	✓	✓ _{ACP}	✓		
	$K_S^0K^+K^-$		✓ ^(b)	✓			
Self-conjugated SCS 3-body decay	$\pi^+\pi^-\pi^0$	✓ _{ACP}	✓ _{ACP}	✓ ^{mixing} _{ACP}			
	$K^+K^-\pi^0$			✓ _{ACP}			
SCS 3-body	$K_S^0K^\pm\pi^\mp$	✓ _{$\delta^{K_S^0K\pi}$}				✓ _{$\delta^{K_S^0K\pi}$}	
Semileptonic decay	$K^+\ell^-\nu_\ell$		✓	✓		✓	
Multi-body($n\geq 4$)	$\pi^+\pi^-\pi^+\pi^-$	✓ _{ACP}					
	$K^+\pi^-\pi^+\pi^-$	★	✓ _{ACP}	✓			
	$K^+K^-\pi^+\pi^-$	✓ ^(c) _{ACP}		✓ _{AT}		✓ _{ACP}	
$\psi(3770) \rightarrow D^0\bar{D}^0$ via correlations						✓ _{$\delta^{K\pi}$}	✓ _{y_{CP}}

★ for observation ($> 5\sigma$); ● for evidence ($> 3\sigma$); ✓ for measurement.

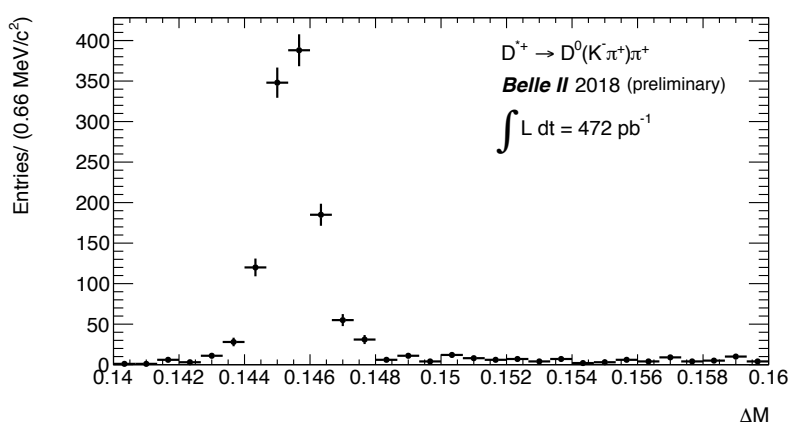
(a) LHCb measured the indirect CP asymmetry in Phys. Rev. Lett. **112**, 041801 (2014).

(b) Belle measured y_{CP} in $D^0 \rightarrow K_S^0\phi$ in Phys. Rev. D **80**, 052006 (2009).

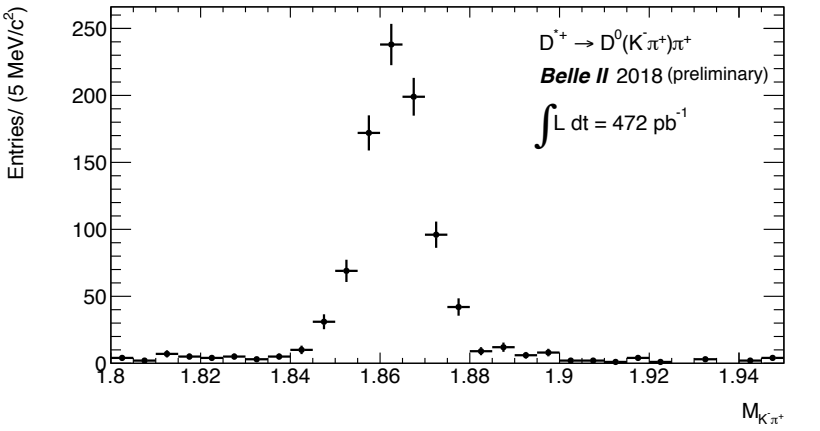
(c) LHCb searched for CP violation using T-odd correlations in JHEP **10** (2014) 005.

Challenging: higher event rate and radiation damage to detectors from machine background processes

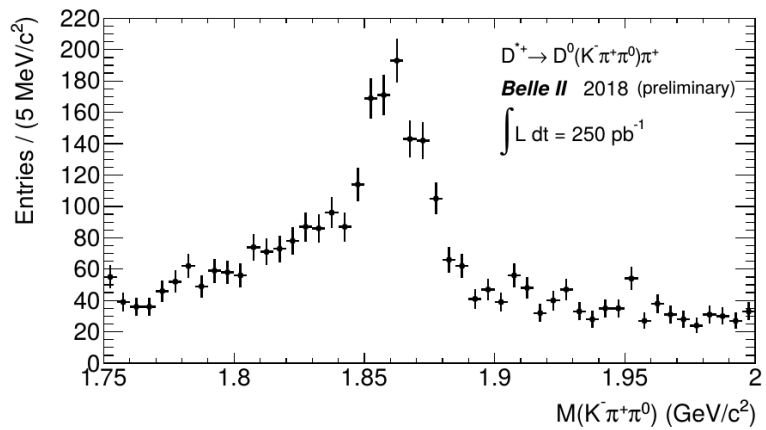
source: Belle II Physics Book: arXiv: 1808.10567



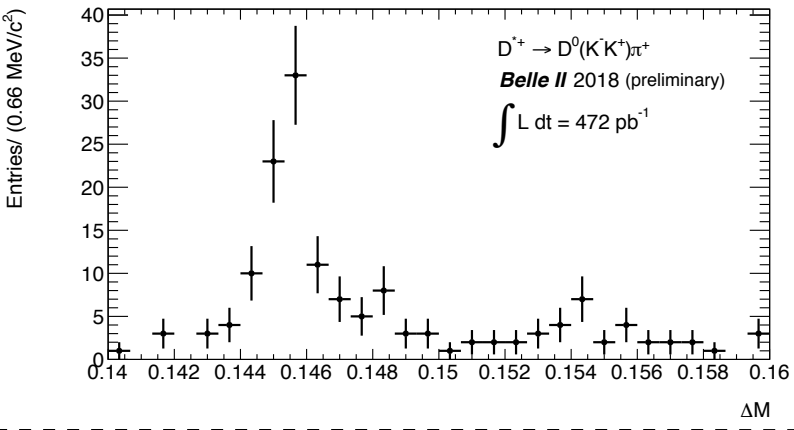
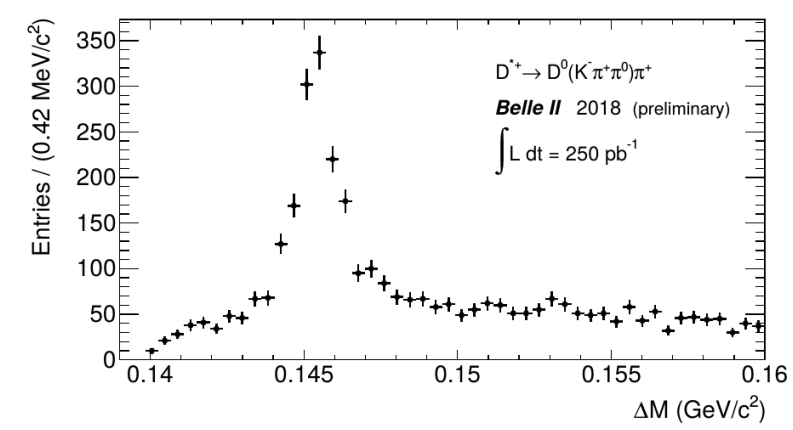
$D^0 \rightarrow K^- \pi^+$



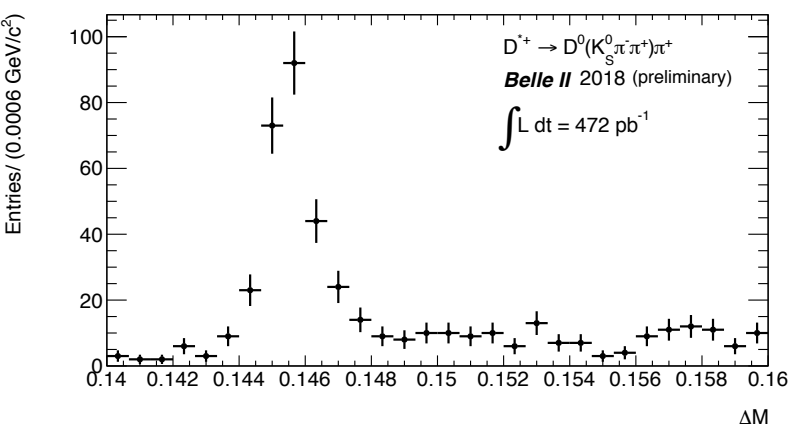
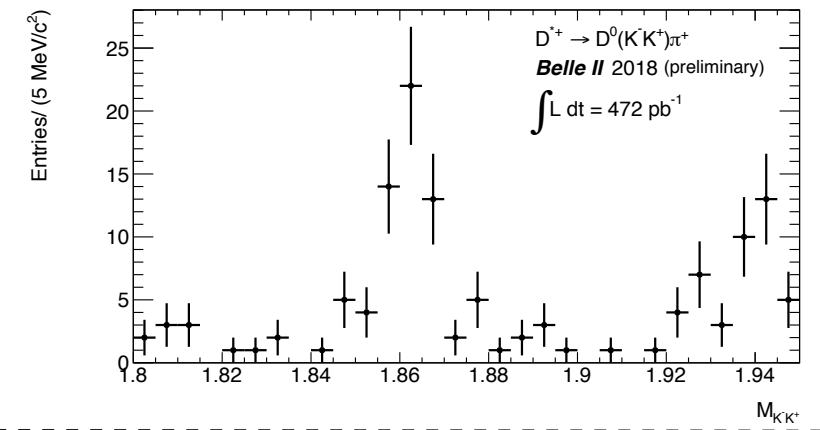
Re-discoveries of D meson decays



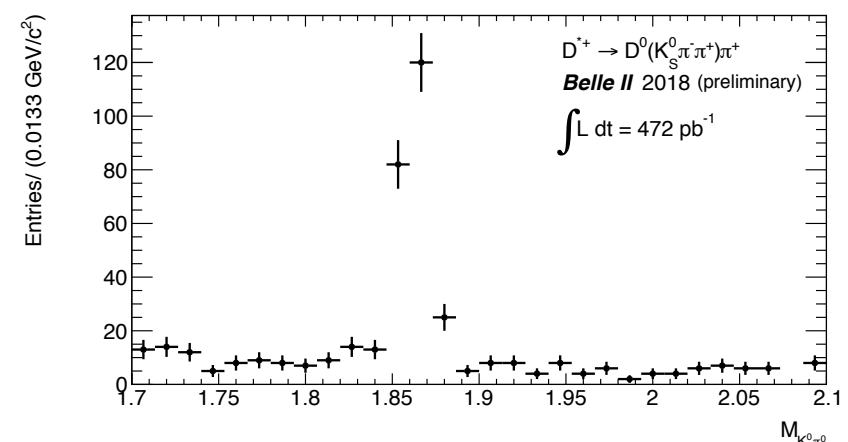
$D^0 \rightarrow K^- \pi^+ \pi^0$



$D^0 \rightarrow K^+ K^-$



$D^0 \rightarrow K_S^0 \pi^- \pi^+$



Category 1. Mixing in CP eigenstates

- Compare effective lifetime of CP eigenstates with flavor ones
- y_{CP} is most powerful parameter that can constraint "y"

So far...

$$y_{CP} \equiv \frac{\Gamma_{CP\pm}}{\Gamma} - 1$$

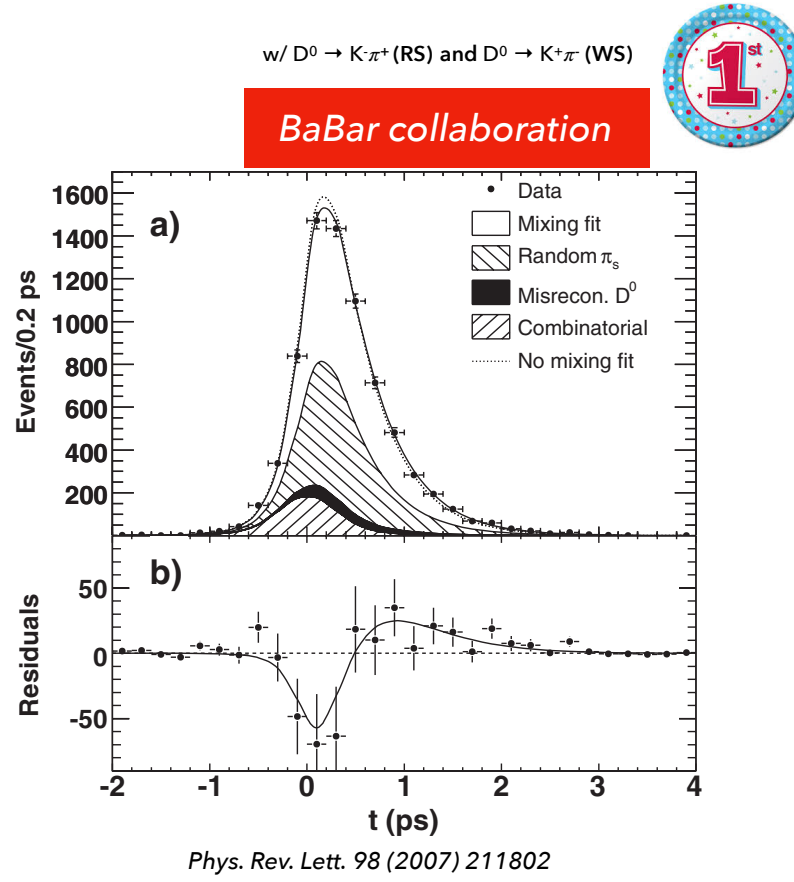
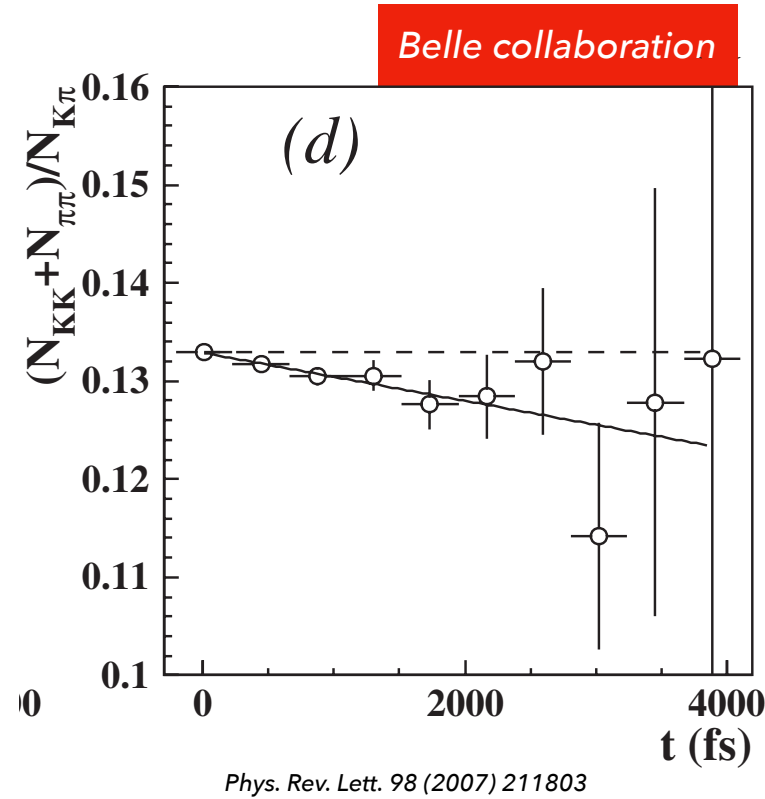
1 CP eigenstates, $D^0 \rightarrow K^+K^-/\pi^+\pi^-$ and decays to CP mixed state, $D^0 \rightarrow K^-\pi^+$

	y_{CP} in 10^{-3}
LHCb	$5.5 \pm 6.3 \pm 4.1$
BaBar	$7.2 \pm 1.8 \pm 1.2$
Belle	$11.1 \pm 2.2 \pm 1.1$

BaBar: Phys.Rev. D87 (2013) 012004
 LHCb: JHEP 1204 (2012) 129
 Belle: arXiv:1212.3478

2 CP eigenstates, $D^0 \rightarrow K_s K^+ K^-$ via Dalitz model

	y_{CP} in 10^{-3}
Belle	$1.1 \pm 6.1 \pm 5.2$



Belle II predictions

Observable	Statistical	Systematic		Total
		red.	irred.	
$y_{CP} [10^{-2}]$				
976 fb^{-1}	0.22	0.07	0.07	0.24
5 ab^{-1}	0.10	0.03-0.04	0.07-0.04	0.11-0.12
50 ab^{-1}	0.03	0.01	0.07-0.04	0.05-0.08

$D^0 \rightarrow \pi^-\pi^+\pi^-\pi^+$?
 $D^0 \rightarrow K_s\pi^+\pi^-\pi^0$?

Source	$\Delta y_{CP} [10^{-2}]$
acceptance	0.050
SVD misalignments	0.060
mass window position	0.007
background	0.059
resolution function	0.030
binning	0.021
total syst. error	0.105
stat. error	0.220

Source Belle II Physics Book: arXiv: 1808.10567

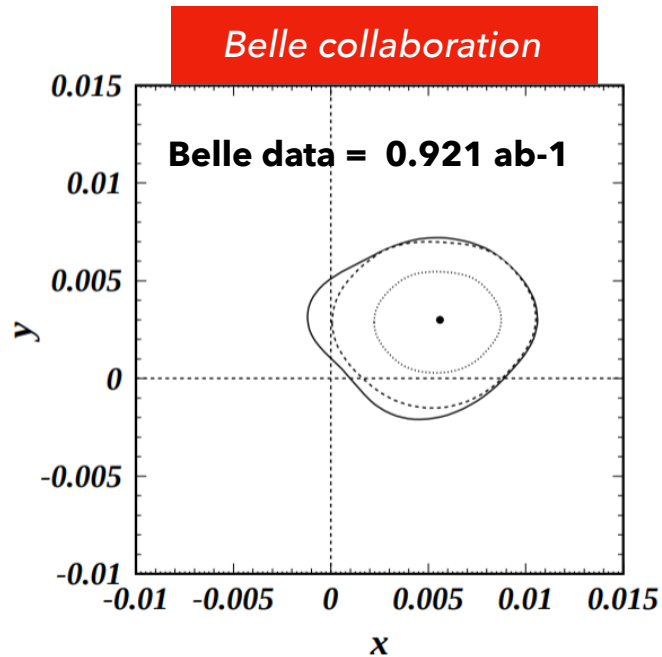
Category 2. Measurement of x and y variables

- Simultaneous measurement of decay-time evolution and resonance amplitudes
- $D^0 \rightarrow K_s K^- K^+$ for study which also allow to probe indirect CPV

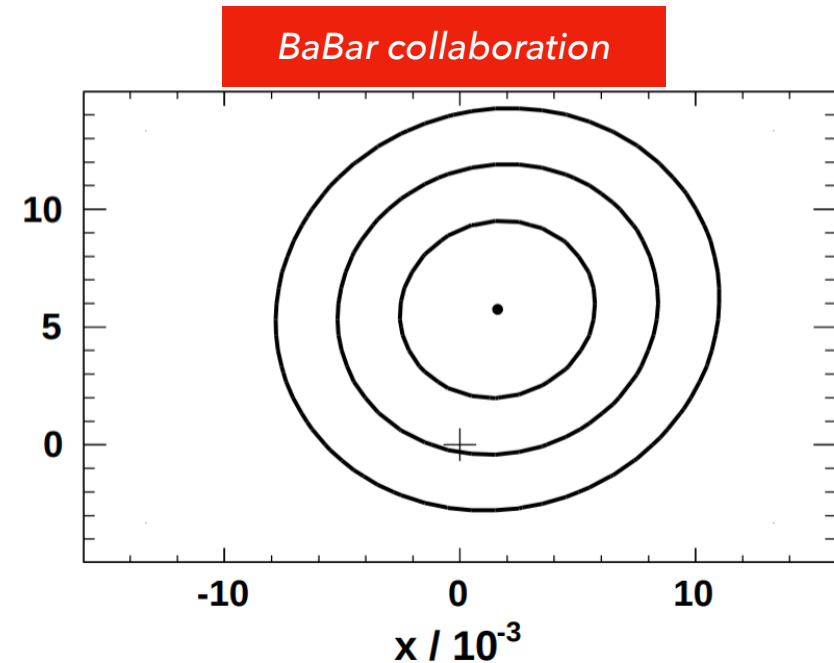
So far...

	x in 10^{-3}	y in 10^{-3}
BaBar	$1.6 \pm 2.3 \pm 1.2 \pm 0.8$	$5.7 \pm 2.0 \pm 1.3 \pm 0.7$
Belle	$5.6 \pm 1.9^{+0.3+0.6}_{-0.9-0.9}$	$3.0 \pm 1.5^{+0.4+0.3}_{-0.5-0.6}$

*Under no CPV



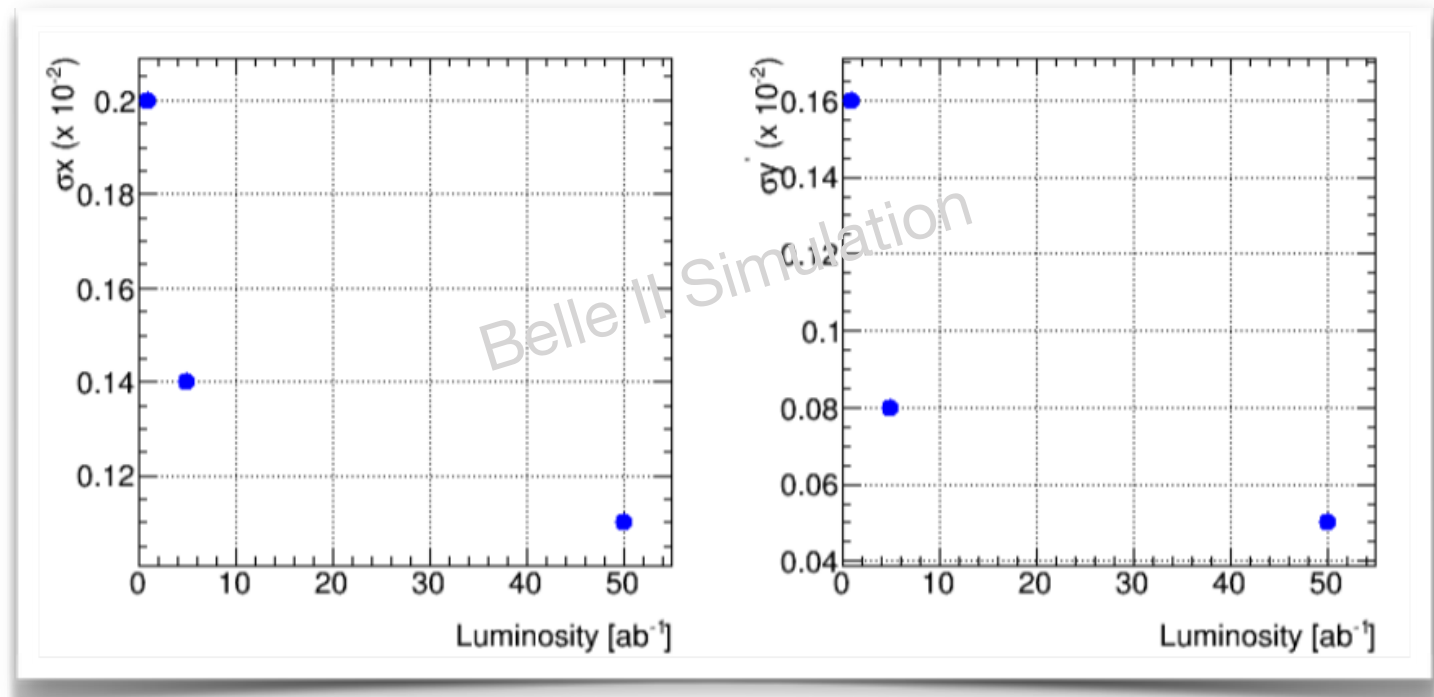
Phys.Rev. D89, (2014) 091103



Phys. Rev. Lett. 105 (2010) 081803,

Belle II predictions

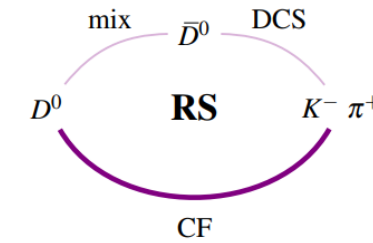
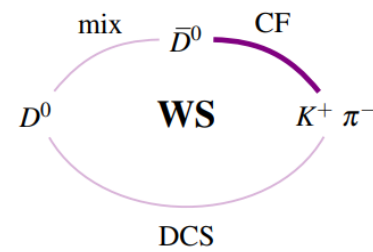
- better precision is expected
 - by factor of 3 for x, y resolutions
- even more..
 - w/ improved decay time resolution



17 Mixing measurements

Category 3. Mixing via interference

- Golden channel is $D^0 \rightarrow K^+ \pi^-$ (many syst auto-cancelled)

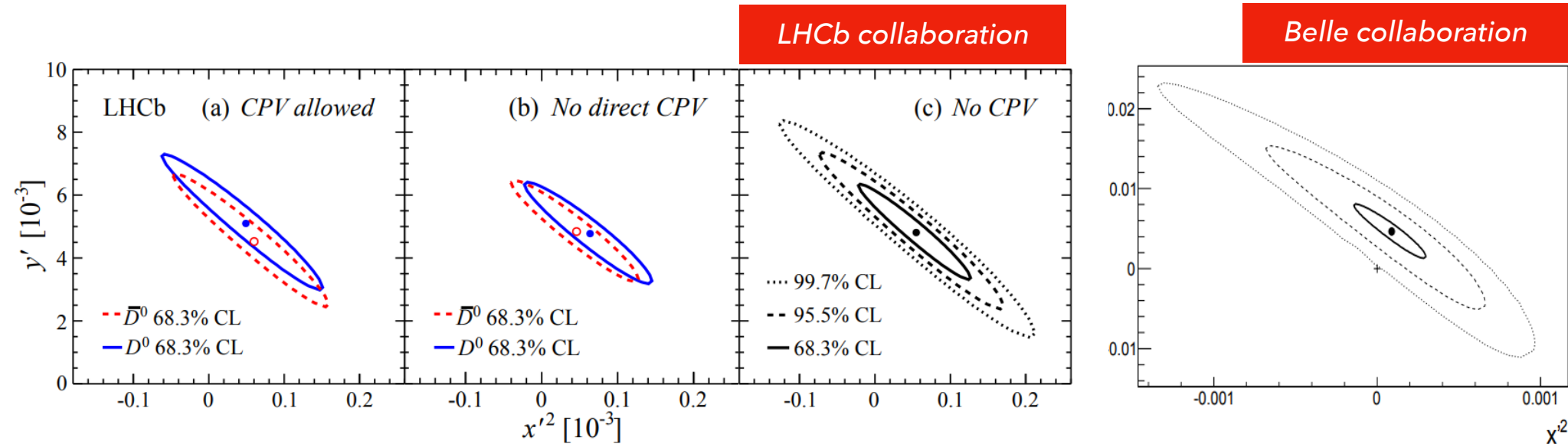


So far...

	x'^2 in 10^{-3}	y' in 10^{-3}
CDF	0.08 ± 0.18	4.3 ± 4.3
LHCb	0.06 ± 0.05	4.8 ± 1.0
Belle	0.09 ± 0.22	4.6 ± 3.4

$$x'' = x \cos \delta_{K^+ \pi^- \pi^0} + y \sin \delta_{K^+ \pi^- \pi^0}$$

$$y'' = y \cos \delta_{K^+ \pi^- \pi^0} - x \sin \delta_{K^+ \pi^- \pi^0}$$



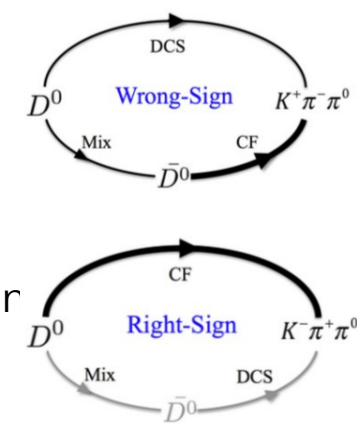
LHCb: Phys. Rev. Lett. 110 (2013) 101802,
 CDF: Phys. Rev. Lett. 100 (2008) 121802
 CDF: Phys. Rev. Lett. 111, (2013) 231802
 LHCb: Phys. Rev. Lett. 111 (2013) 251801
 Belle: Phys. Rev. Lett. 112, (2014) 111801

Belle II predictions

Parameter	5 ab^{-1}	20 ab^{-1}	50 ab^{-1}
$\delta x'^2$ (10^{-5})	7.5	3.7	2.3
$\delta y'$ (%)	0.11	0.056	0.035

Luminosity (ab^{-1})	Belle	Belle II
0.400	4 024	
0.976	11 478	
5.0		58 800
20		235 200
50		588 010

Category 3. Mixing via interference



- CF and DCS can also lead to excited states of same quark content
- Channel is $D^0 \rightarrow K^+\pi^-\pi^0$ (resonance $K^+\rho^-$ and $K^{*+}\pi^-$)

$$x'' = x \cos \delta_{K^+\pi^-\pi^0} + y \sin \delta_{K^+\pi^-\pi^0}$$

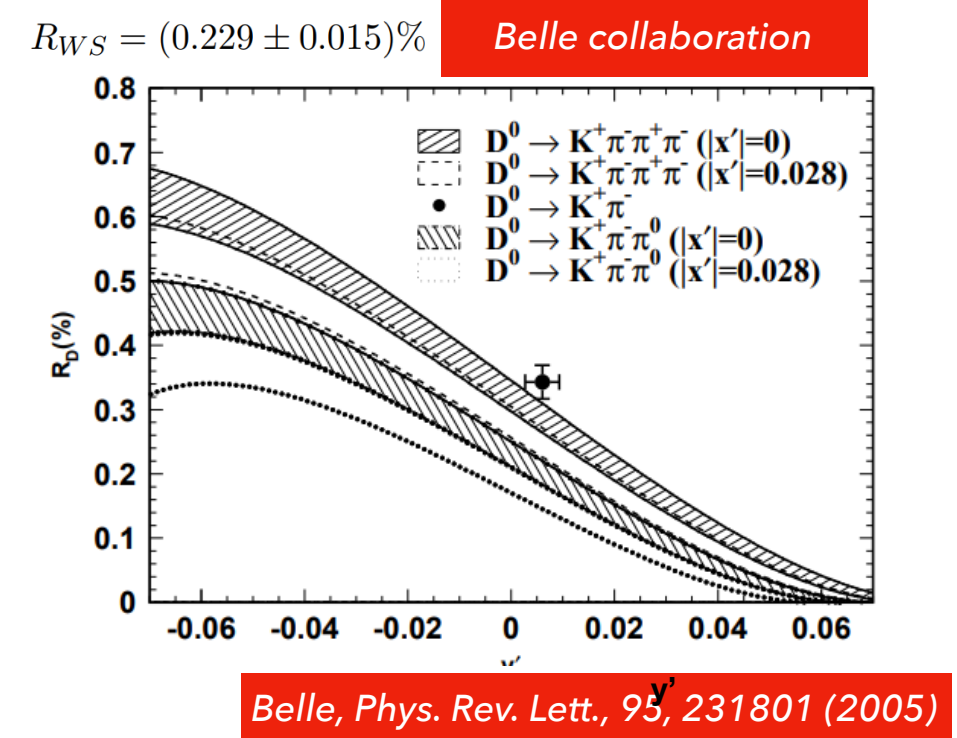
$$y'' = y \cos \delta_{K^+\pi^-\pi^0} - x \sin \delta_{K^+\pi^-\pi^0}$$

So far...

$$x'' = (2.61_{-0.68}^{+0.57} \pm 0.39)\%$$

$$y'' = (-0.06_{-0.64}^{+0.55} \pm 0.34)\%$$

BaBar, Phys. Rev. Lett., 103, 211801 (2009)

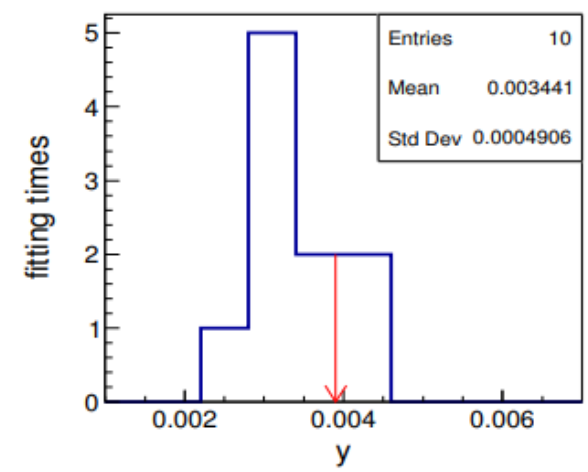
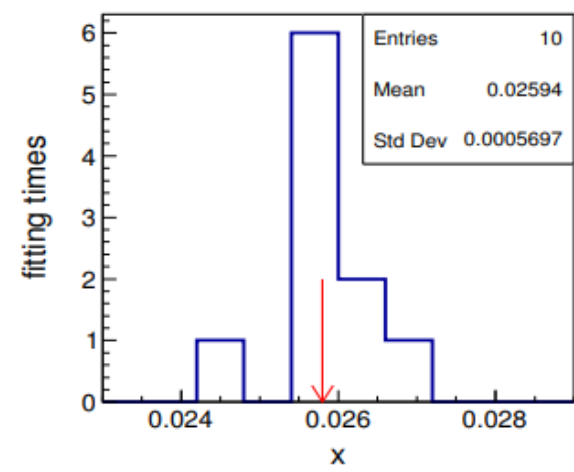
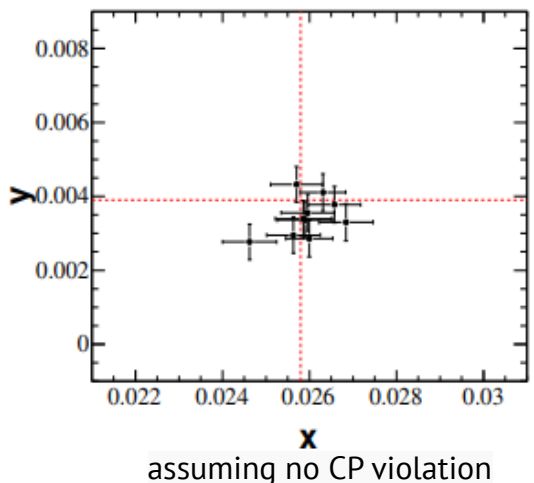


Belle II predictions

*assuming Belle II reconstruction efficiency is same as Belle
 * one order of magnitude precise than BaBar

$$\sigma_{x''} = 0.057\%$$

$$\sigma_{y''} = 0.049\%$$



So far...

Belle II impact on the World Average

- So far no single measurement has been able to measure precisely
- Combined results by Heavy-Flavour Averaging group (HFA) : **World Average**

w/o CPV in mixing and decay

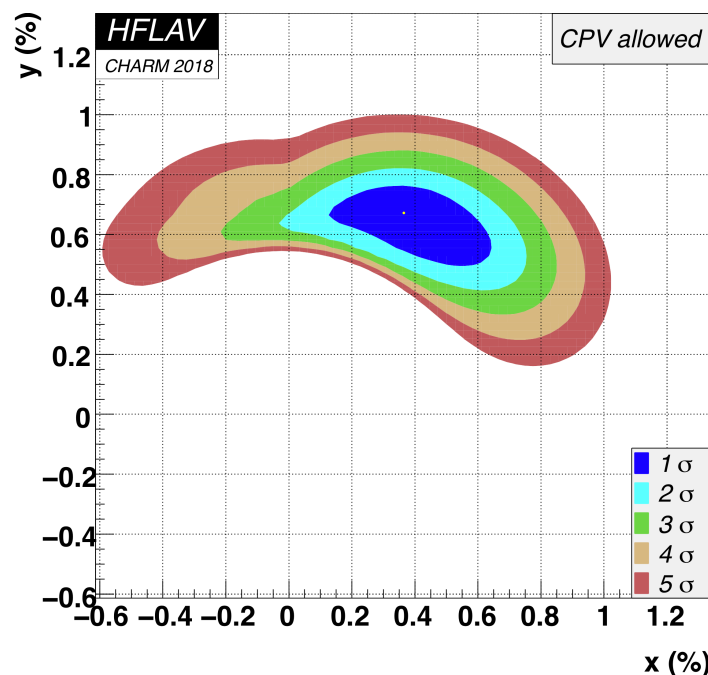
$$x = (4.9^{+1.4}_{-1.5}) \times 10^{-3} \quad y = (6.2 \pm 0.8) \times 10^{-3}$$

- .. but hint of D^0 and \bar{D}^0 mixing by many measurements

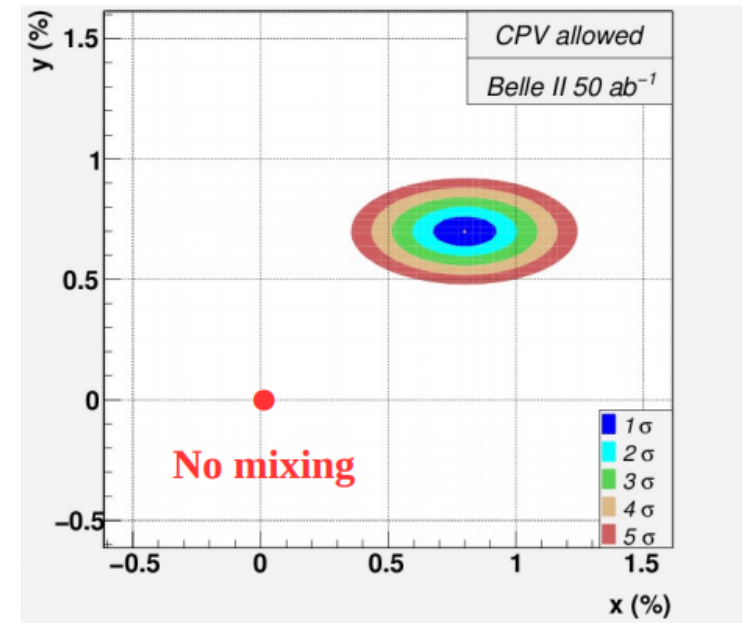
w/ CPV in mixing and decay

World Average	Belle II (50 ab^{-1})
$x = 3.2 \pm 1.4 \times 10^{-3}, y = 6.9 \pm 0.6 \times 10^{-3}$	$x = 8.0 \pm 0.9 \times 10^{-3}, y = 7.0 \pm 0.4 \times 10^{-3}$

Belle II predictions



mixing parameters
 $x = \frac{\Delta m}{\Gamma}, \quad y = \frac{\Delta \Gamma}{2\Gamma},$
 where Δm = mass differences
 and $\Delta \Gamma$ = lifetimes differences



20 Measuring indirect CPV

So far... 1. Direct measurement of $|p/q|$ and ϕ

- Golden channel are : $D^0 \rightarrow K_S K^- K^+$ or $D^0 \rightarrow K_S \pi^+ \pi^-$
- Provide most precise mixing parameters
- To avoid systematic limitation > reduce model limitation OR improve model independent strong phase difference (at BESIII)

Belle collaboration

Fit type	Parameter	Fit result
No CPV	$x(\%)$	$0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$
CPV	$x(\%)$	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
	$y(\%)$	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
	$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
	$\arg(q/p)(^\circ)$	$-6 \pm 11 \pm 3^{+3}_{-4}$

Phys. Rev. D 89, 091103 (2014)

2. CP asymmetries in WS decay: $D^0 \rightarrow K^+ \pi^-$

- Measurement of R_D , x'^2 and y'^2
- Small phase (ϕ) gives direct access to $|q/p|$

$$x'^{\pm} = \left| \frac{q}{p} \right|^{\pm 1} (x' \cos \phi \pm y' \sin \phi)$$

$$y'^{\pm} = \left| \frac{q}{p} \right|^{\pm 1} (y' \cos \phi \mp x' \sin \phi)$$

Belle: Phys.Rev.Lett. 96 151801,2006
BaBar: Phys. Rev. Lett. 98 (2007) 211802

Belle II predictions

Assuming no CPV	Data	stat.			Total	stat.			Total
		red.	syst.			red.	syst.		
			irred.		irred.				
			$\sigma_x (10^{-2})$			$\sigma_y (10^{-2})$			
	976 fb ⁻¹	0.19	0.06	0.11	0.20	0.15	0.06	0.04	0.16
	5 ab ⁻¹	0.08	0.03	0.11	0.14	0.06	0.03	0.04	0.08
	50 ab ⁻¹	0.03	0.01	0.11	0.11	0.02	0.01	0.04	0.05
			$ q/p (10^{-2})$			$\phi (^\circ)$			
	976 fb ⁻¹	15.5	5.2-5.6	7.0-6.7	17.8	10.7	4.4-4.5	3.8-3.7	12.2
	5 ab ⁻¹	6.9	2.3-2.5	7.0-6.7	9.9-10.1	4.7	1.9-2.0	3.8-3.7	6.3-6.4
	50 ab ⁻¹	2.2	0.7-0.8	7.0-6.7	7.0-7.4	1.5	0.6	3.8-3.7	4.0-4.2

Parameter	5 ab ⁻¹	20 ab ⁻¹	50 ab ⁻¹
$\delta x'^2 (10^{-5})$	7.5	3.7	2.3
$\delta y' (\%)$	0.11	0.056	0.035
$\delta x' (\%)$	0.37	0.23	0.15
$\delta y' (\%)$	0.26	0.17	0.10
$\delta q/p $	0.197	0.089	0.051
$\delta \phi (^\circ)$	15.5	9.2	5.7

- SuperKEKB and Belle II will be an excellent platform for charm measurements
 - SuperKEKB Will record 50 x larger data sample than KEKB / Belle (by 2025).
 - Upgraded VXD will provide factor two better D0 decay time resolution than Belle/BaBar.
 - First collision data successfully recorded this year.
 - First data with full vertex detector early 2019.
- Better precision on x and y variables $\leq 0.1\%$ is expected.
- Error extrapolations from Belle measurements is predicted as;

$$\sigma_{\text{Belle II}} = \sqrt{(\sigma_{\text{stat}}^2 + \sigma_{\text{syst}}^2) \cdot (\mathcal{L}_{\text{Belle}}/50 \text{ ab}^{-1}) + \sigma_{\text{irred}}^2}$$

σ_{stat} : Scaling Belle statistical error by the ratio of integrated luminosities

σ_{syst} : Only those who scale with luminosity such as background shapes measured with control samples

σ_{irred} : Those who do not scale with luminosity such as decay time resolution due to detector misalignment

Source Belle II Physics Book: [arXiv: 1808.10567](https://arxiv.org/abs/1808.10567)

Stay tuned.. for new and precise measurements..