

# Prospects of Dalitz Analysis on Charm Physics at Belle II

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# Outline

- 1 Belle experiment to Belle II experiment
  - Accelerator and Nano-beam
  - Detector and its highlights
  - Data set and Collaboration
- 2 Prospects of TDDA on charm at Belle II
  - $D^0$ - $\bar{D}^0$  mixing and  $CP$  violation
  - Time-dependent Dalitz analysis
  - Prospect of TDDA in  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$
  - Prospect of TDDA in  $D^0 \rightarrow K^+ \pi^- \pi^0$
  - A new  $D^0$ -tag method: ROE method
- 3 Re-discoveries of Phase2 at Belle II
- 4 Summary



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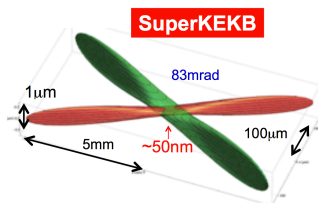
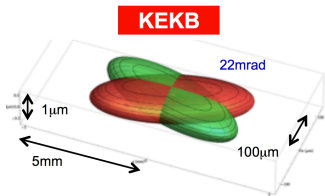
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# Nano-Beam Scheme

- The SuperKEKB upgrade is based on 'Nano-beam' scheme (first proposed for SuperB in Italy)
- Its basic idea is to squeeze the vertical beta function at the IP  $\beta_y^*$  by minimizing the longitudinal size of the overlap region of the two beams at the IP.



luminosity

$$\mathcal{L} = \frac{\gamma_{\pm}}{2e r_e} \left( 1 + \frac{\sigma_y^*}{\sigma_x^*} \right) \frac{I_{\pm} \xi_{y\pm}}{\beta_{y\pm}^*} \left( \frac{R_L}{R_{\xi_y}} \right)$$

beam size:  $\sigma^*$ , beam-beam par.:  $\xi_{\pm}$ ,

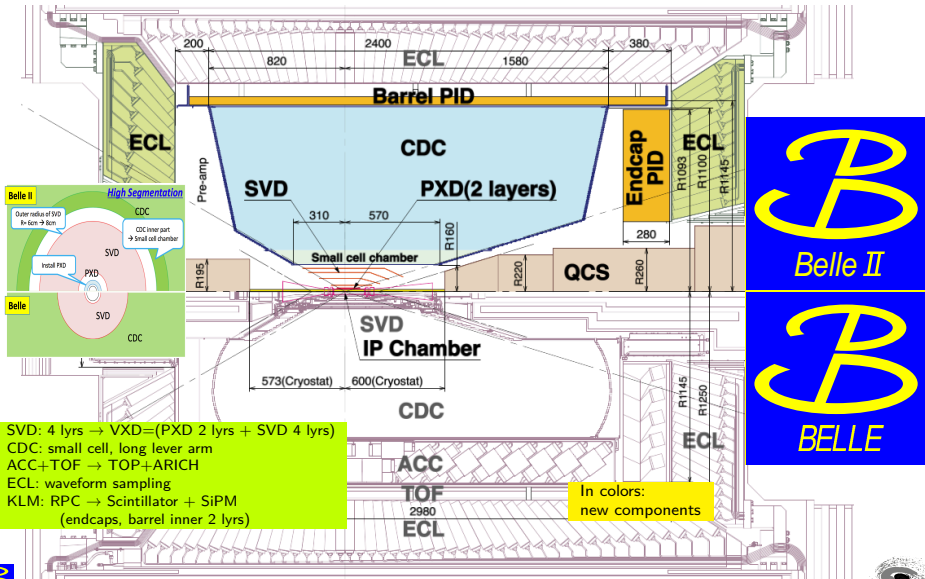
beam current:  $I_{\pm}$ , beta function:  $\beta^*$

|           | $E_{\pm}$ (GeV)        | Cross Angle (mrad) | $I_{\pm}$ (A) | $\beta_y^*$ (mm) | $\mathcal{L}$ ( $\text{cm}^{-2}\text{s}^{-1}$ ) |
|-----------|------------------------|--------------------|---------------|------------------|---|
|           | LER/HER                |                    | LER/HER       | LER/HER          |   |
| KEKB      | 3.5/8.0                | 22                 | 1.64/1.19     | 5.9/5.9          | $2.1 \times 10^{34}$                            |
| SuperKEKB | 4.0/7.0                | 83                 | 3.60/2.60     | 0.27/0.31        | $80 \times 10^{34}$                             |
|           | $\beta\gamma \sim 2/3$ |                    | $\times 2$    | $\times 20$      | $\times 40$                                     |



Detector and its highlights

# Detector: Belle Vs. Belle II



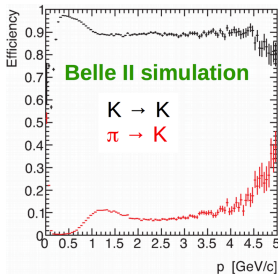
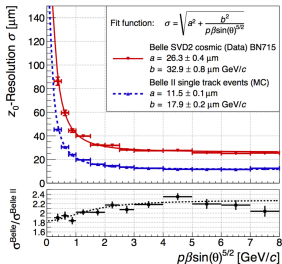
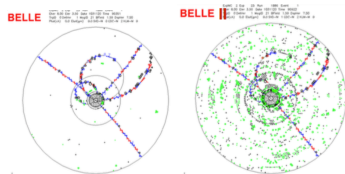
# Detector highlights at Belle II

## ► Under higher luminosity ( $\times 50$ ), Belle II is fighting with

- (1) higher machine backgrounds ( $\times 20$ );
- (2) higher event rate ( $\times 10$ )
- (3) reduced energy asymmetry ( $\beta\gamma$ : 0.45  $\rightarrow$  0.28)

## ► A lot of improved performances, such as

- improved L1 trigger: 500Hz (Belle) Vs. 30kHz (Belle II).
- vertex detector (VXD): better spatial resolution (**Belle II**:  $\sim 2$  better than **Belle**)
- VXD:  $\sim 30\%$  larger acceptance for  $K_S^0$  reconstruction
- higher tracking reconstruction efficiency
- better particle identification:  $K(\pi)$  eff.  $> 90\%$  with fake rate  $< 10\%$  for  $p < 4$  GeV/c.



# larger Data set at Belle II

▶ Each  $1 \text{ ab}^{-1}$  dataset at B-factory provides:

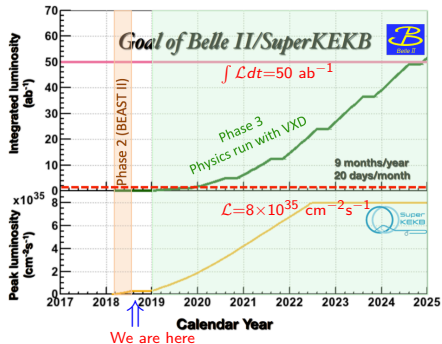
- $\sim 1.1 \times 10^9 \text{ } B\bar{B} \Rightarrow$  a **B-factory**;
- $\sim 1.3 \times 10^9 \text{ } c\bar{c} \Rightarrow$  a **charm-factory**;
- $\sim 0.9 \times 10^9 \text{ } \tau^+\tau^- \Rightarrow$  a  **$\tau$ -factory**;
- wide region  $E_{c,m}^{\text{eff}}=[0.5\text{-}10] \text{ GeV}$  via ISR process.

▶ Available charm dataset at some experiments:

| Experiment | Machine                 | C.M $\sqrt{s}$ | Luminosity           | charm sample                    | efficiency            |
|------------|-------------------------|----------------|----------------------|---------------------------------|-----------------------|
| CLEOC      | CESR<br>( $e^+e^-$ )    | 3.77 GeV       | 0.8 $\text{fb}^{-1}$ | $2.9 \times 10^6 (D^0)$         | $\sim 10\text{-}30\%$ |
|            |                         |                |                      | $2.3 \times 10^6 (D^+)$         |                       |
|            |                         | 4.17 GeV       | 0.6 $\text{fb}^{-1}$ | $0.6 \times 10^6 (D_s^+)$       |                       |
| BES III    | BEPC-II<br>( $e^+e^-$ ) | 3.77 GeV       | 2.9 $\text{fb}^{-1}$ | $10.5 \times 10^6 (D^0)$        | $\sim 10\text{-}30\%$ |
|            |                         |                |                      | $8.4 \times 10^6 (D^+)$         |                       |
|            |                         | 4.18 GeV       | 3.0 $\text{fb}^{-1}$ | $3 \times 10^6 (D_s^+)$         |                       |
|            |                         | 4.6 GeV        | 0.6 $\text{fb}^{-1}$ | $1 \times 10^5 (\Lambda_c^+)$   |                       |
| Belle II   | KEKB<br>( $e^+e^-$ )    | 10.58 GeV      | 1 $\text{ab}^{-1}$   | $1.3 \times 10^9 (D^0)$         | $\sim 5\text{-}10\%$  |
|            |                         |                |                      | $7.7 \times 10^8 (D^+)$         |                       |
|            |                         |                |                      | $2.5 \times 10^8 (D_s^+)$       |                       |
| PEP-II     | PEP-II<br>( $e^+e^-$ )  | 10.58 GeV      | 0.5 $\text{ab}^{-1}$ | $1.5 \times 10^8 (\Lambda_c^+)$ | $\sim 5\text{-}10\%$  |
|            |                         |                |                      | $6.5 \times 10^8 (D^0)$         |                       |
|            |                         |                |                      | $3.8 \times 10^8 (D^+)$         |                       |
| Tevatron   | Tevatron<br>( $pp$ )    | 1.96 TeV       | 9.6 $\text{fb}^{-1}$ | $1.3 \times 10^{11}$            | $\sim 5\text{-}10\%$  |
|            |                         |                |                      | $0.7 \times 10^8 (\Lambda_c^+)$ |                       |
| LHC        | LHC<br>( $pp$ )         | 7 TeV          | 1.0 $\text{fb}^{-1}$ | $5.0 \times 10^{12}$            | $< 0.5\%$             |
|            |                         | 8 TeV          | 2.0 $\text{fb}^{-1}$ |                                 |                       |

▶ Belle II is back to the game.

- Phase 2 has finished (Apr 26 - Jul 17)
- Phase 3 (physics run) will start next spring.
- $\mathcal{L}(\text{Belle+BaBar})$  will be reached in next year.
- collect  $\sim 5 \text{ ab}^{-1}$  by mid 2020.
- collect  $50 \text{ ab}^{-1}$  before 2025.

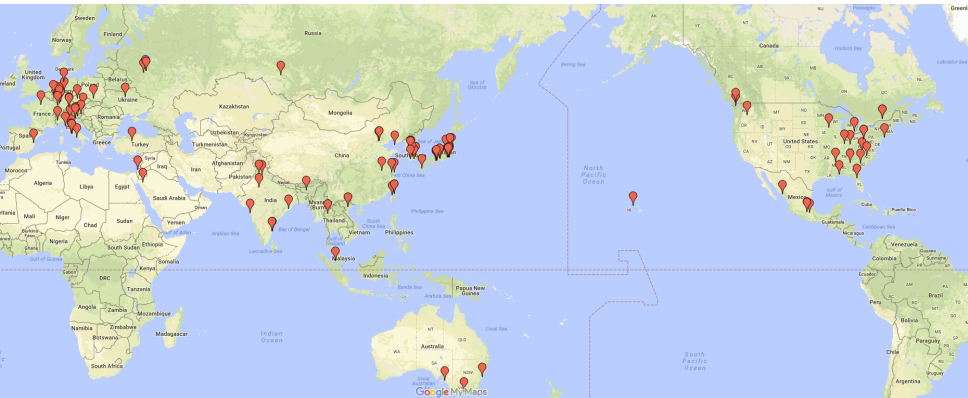


- Belle II awards us a huge B/charm/ $\tau$  sample.





# A big family in Belle II Collaboration



- ▶ Belle Collaboration : 536 colleagues, 91 institutions, 20 countries/regions
- ▶ Belle II Collaboration: 822 colleagues, 110 institutions, 25 countries/regions
- ▶ Belle II has 7 inst. from China mainland (including two **new inst.** this Jun):
  - IHEP(14), USTC(6), Peking(3), BUAA(9), Fudan(7) + LNNU + Soochow.



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# Formalism of $D^0-\bar{D}^0$ mixing and CP violation

- Open-flavor neutral meson transforms to anti-meson:

$$K^0 \Leftrightarrow \bar{K}^0, B_d^0 \Leftrightarrow \bar{B}_d^0, B_s^0 \Leftrightarrow \bar{B}_s^0, D^0 \Leftrightarrow \bar{D}^0$$

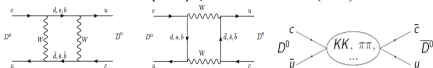
- Flavor eigenstate ( $|D^0\rangle, |\bar{D}^0\rangle$ )  $\neq$  mass eigenstate  $|D_{1,2}\rangle$  with  $M_{1,2}$  and  $\Gamma_{1,2}$

$$|D_{1,2}\rangle \equiv p|D^0\rangle \pm q|\bar{D}^0\rangle \quad (\text{CPT: } p^2+q^2=1)$$

- Mixing parameters:  $\mathbf{x} \equiv 2 \frac{M_1 - M_2}{\Gamma_1 + \Gamma_2}, \quad \mathbf{y} \equiv \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$

- Unique system: only up-type meson for mixing

- Standard Model(SM) predicts:  $\sim \mathcal{O}(1\%)$



(1) short distance ( $< 0.1\%$ )

(2) long distance ( $\sim 1\%$ )

- Precise measurement of  $x, y$ : effectively limit the New Physics(NP) modes; and search for NP, eg:  $|x| \gg |y|$

- Three types of **C**harged-**C**onjugated-**P**arity combined symmetry **V**iolation (CPV):

$$A_{CP}^f = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} = a_d^f + a_m^f + a_i^f$$

- $a_d^f$ : (direct CPV) CPV in decay  $|\bar{A}_f/A_f| \neq 1$

$$\left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2 \neq \left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \text{---} \text{---} \left. \begin{array}{c} \bar{f} \\ \text{---} \\ \text{---} \end{array} \right|^2$$

- $a_m^f$ : CPV in mixing with  $r_m = |q/p| \neq 1$

$$\left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} \bar{f} \\ \text{---} \\ \text{---} \end{array} \right|^2 \neq \left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2$$

- $a_i^f$ : CPV in interference with  $\arg(q/p) \neq 0$

$$\left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2 + \left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2 \neq \left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2 + \left| \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \right. \begin{array}{c} p^0 \\ \text{---} \\ \text{---} \end{array} \left. \begin{array}{c} f \\ \text{---} \\ \text{---} \end{array} \right|^2$$

- SM with only a source: the phase in CKM
- in charm sector, it's predicted at  $\sim \mathcal{O}(10^{-3})$
- $\sim 1\%$  exp. sensitivity to observe CPV $\rightarrow$ NP



# Time evolution of $D^0-\bar{D}^0$ system

- Time evolution of  $D^0-\bar{D}^0$  system:

$$i \frac{\partial}{\partial t} \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix} = (M - \frac{i}{2}\Gamma) \begin{pmatrix} D^0(t) \\ \bar{D}^0(t) \end{pmatrix}$$

diagonal:  $D \rightarrow D$ , non-diagonal:  $D \rightarrow \bar{D}$ .

- Measure  $D^0-\bar{D}^0$  mixing ( $x, y$ ) and CPV ( $q/p$ )

$$|D^0(t)\rangle = g_+(t)|D^0\rangle + \frac{q}{p}g_-(t)|\bar{D}^0\rangle$$

$$|\bar{D}^0(t)\rangle = \frac{p}{q}g_-(t)|D^0\rangle + g_+(t)|\bar{D}^0\rangle$$

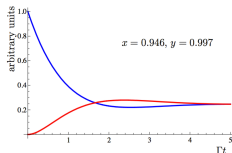
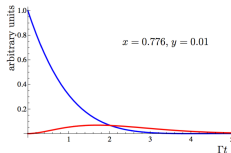
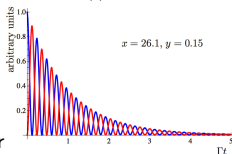
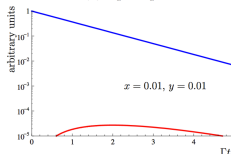
$$g_+(t) = \exp(-iMt - \frac{1}{2}\Gamma t) \cosh\left(-\frac{ix+y}{2}\Gamma t\right)$$

$$g_-(t) = \exp(-iMt - \frac{1}{2}\Gamma t) \sinh\left(-\frac{ix+y}{2}\Gamma t\right)$$

- Probabilities of changed or unchanged D flavor at time  $t$  for an initial pure flavor state  $|D^0\rangle$

$$| \langle D^0 | D^0(t) \rangle |^2 = \frac{1}{2} e^{-\Gamma t} [\cosh(y\Gamma t) + \cos(x\Gamma t)]$$

$$| \langle D^0 | \bar{D}^0(t) \rangle |^2 = \frac{1}{2} \left| \frac{q}{p} \right|^2 e^{-\Gamma t} [\cosh(y\Gamma t) - \cos(x\Gamma t)]$$

(a)  $K^0 - \bar{K}^0$ (b)  $B_d^0 - \bar{B}_d^0$ (c)  $B_s^0 - \bar{B}_s^0$ (d)  $D^0 - \bar{D}^0$ 

$y$  effects lifetime in amplitude;  $x$ : brings a sine oscillating.

- $D^0-\bar{D}^0$  mixing measurement is most difficult.








# Time-dependent Dalitz analyses in $D^0$ three-body decays

- ▶ Time-dependent Dalitz analysis(TDDA) provides an essential tool in studying  $D^0$ - $\bar{D}^0$  mixing.

$$\Gamma(D^0(t) \rightarrow f) \propto |\mathcal{A}_f|^2 e^{-t} \left( \frac{1+|\lambda_f|^2}{2} \cosh(yt) - \text{Re}(\lambda_f) \sinh(yt) + \frac{1-|\lambda_f|^2}{2} \cos(xt) + \text{Im}(\lambda_f) \sin(xt) \right)$$

- ▶ An unique method: **sensitive to linear order** for both mixing parameters.
- ▶ Status of  $D^0$ - $\bar{D}^0$  mixing and  $CP$  violation measurement in  $D^0$  three-body decays:

| Decay Type                | Final State         |  |  |  |  |  |
|---------------------------|---------------------|---|---|---|---|--|
| DCS decay (WS)            | $K^+ \pi^- \pi^0$   | ✓ <sup>(a)</sup>  | ☆   |   |   | ✓ <sub>ACP</sub> ○ <sub>δ</sub>  |
| Self-conjugated CF decay  | $K_S^0 \pi^+ \pi^-$ | ✓   | ✓   | ✓   | ✓ <sub>ACP</sub>  | ✓ <sub>ACP</sub> ○ <sub>δ</sub>  |
|                           | $K_S^0 K^+ K^-$     | ✓ <sup>(b)</sup>  | ✓   | ○   |   | ○ <sub>δ</sub>   |
| Self-conjugated SCS decay | $\pi^+ \pi^- \pi^0$ | ✓ <sub>ACP</sub>  | ✓ <sup>mixing</sup> <sub>ACP</sub>  | ✓ <sub>ACP</sub>  |   | ○ <sub>δ</sub>   |
|                           | $K^+ K^- \pi^0$     |   | ✓ <sub>ACP</sub>  |   |   | ○ <sub>δ</sub>   |
| SCS decay                 | $K_S^0 K^+ \pi^-$   |   |   | ✓ <sub>ACP</sub>  |   | ✓ <sub>δ</sub> ○ <sub>δ</sub>  |
|                           | $K_S^0 K^- \pi^+$   |   |   | ✓ <sub>ACP</sub>  |   | ✓ <sub>δ</sub> ○ <sub>δ</sub>  |

★ for observation ( $> 5\sigma$ ); ☆ for evidence ( $> 3\sigma$ ); ✓ for measurement published; ○ for analysis on going.

The related publications are linked under their corresponding signs.

(a) Belle measured WS-to-RS ratio  $R_{WS}$  and  $A_{CP}$  in  $D^0 \rightarrow K^\mp \pi^\pm \pi^0$  in PRL **95**, 231801 (2005).

(b) Belle measured  $y_{CP}$  in  $D^0 \rightarrow K_S^0 \phi$  in PRD **80**, 052006 (2009), the amplitude analysis for mixing parameters is on going.

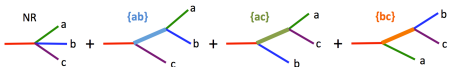
- ▶ A neutral particle exists in the FSPs of all above channels, this possibly makes them more promising at Belle II than LHCb.

⇒ **TDDA will be one of favourites of Belle II Charm WG** to measure  $D^0$ - $\bar{D}^0$  mixing and CPV in such  $D^0$  three-body decays.



# Dalitz analysis with Isobar model

- $P \rightarrow P_a P_b P_c$  decay: d.o.f=2 (i.e.  $m_{ab}^2, m_{bc}^2$ )
- Isobar describes  $\mathcal{M}$ : Phys. Rev. 123, 333 (1961)



$$\mathcal{M}(m_{ab}^2, m_{bc}^2) = a_{NR} e^{i\phi_{NR}} + \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_{ab}^2, m_{bc}^2)$$

here  $a_r(\phi_r)$  is magnitude (phase) of resonance  $r$

- $T_r$ : dynamic function
  - 1) using relativistic Breit-Wigner ( $\Gamma$  depends on  $M$ )
  - 2) Special resonances description:
    - ✓ Flatté model, for mass threshold  
i.e.  $f_0(980)(KK)/a_0(980)(KK/\eta'\pi)$  [PRD 95, 032002 (2017)]
    - ✓ K-matrix model, for overlap resonances,  
i.e.  $\pi\pi$  S-wave [EPJ A16 (2003) 229-258]
    - ✓ Gounaris-Sakurai model:  
i.e.  $\pi\pi$  P-wave  $\rho$  family [PRL 24,244(1968)]
    - ✓ LASS model:  
i.e.  $K\pi$  S-wave with  $K_0^*(1430)$  [EPJ C74 (2014): 3026]
    - ✓ non-resonance:  
i.e. const. ( $D$  decay) or exponential ( $B$  decay)

Also see Daniel's report on 16 July

- Matrix element  $\mathcal{A}_r$  describes the dynamics of  $D \rightarrow (r \rightarrow ab)c$  PRD 63, 092001 (2001)



$$\mathcal{A}_r(m_{ab}^2, m_{bc}^2) = F_D \times F_r \times T_r \times W_r$$

- $F_r, F_D$  form factor: [PR D 63, 092001 (2001)]
  - ▶ using Blatt-Weisskopf Barrier parameterization, depends on angular quantum  $\ell$  (here equals  $J$ ):
 
$$F_{J=0} = 1$$

$$F_{J=1} = \frac{\sqrt{1+z_r}}{\sqrt{1+z_{ab}}}$$

$$F_{J=2} = \frac{\sqrt{(z_r-3)^2+9z_r}}{\sqrt{(z_{ab}-3)^2+9z_{ab}}}$$

$$F_{J=3} = \frac{\sqrt{z_r(z_r-15)^2+9(2z_r-5)}}{\sqrt{z_{ab}(z_{ab}-15)^2+9(2z_{ab}-5)}}$$
 here  $z = (R \cdot q)^2$ ,  $R$  is radius of  $D$  or resonance  $r$
- $W_r$  angular function:
  - (1) Helicity form;
  - (2) Zemach covariant tensor form

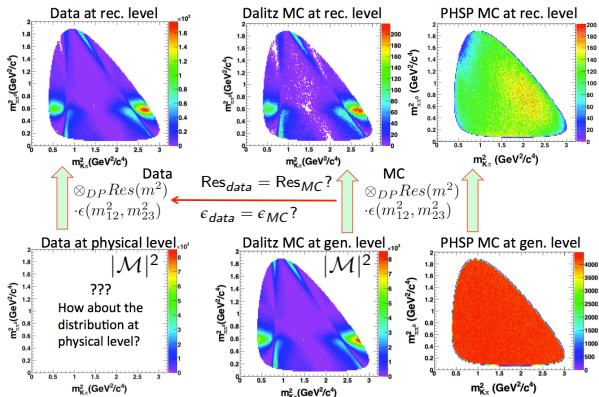


## (time-integrated) Dalitz analysis method

## ► probability density function of (time-integrated) Dalitz analysis:

- (1) efficiency plane  $\epsilon(m_{12,i}^2, m_{23,i}^2)$  to correct: obtained by a large signal MC produced at free PHSP.
- (2) mass resolution  $Res(m)$  effect: needed to check if need? how to consider the resolution?
- (3) normalization: numerical integration on full DP region

$$P_{\text{sig}}(m_{12,i}^2, m_{23,i}^2) = \frac{|\mathcal{M}(m_{12,i}^2, m_{23,i}^2)|^2 \otimes_m Res(m) \cdot \epsilon(m_{12,i}^2, m_{23,i}^2)}{\iint_{DP} dm_{12}^2 dm_{23}^2 |\mathcal{M}(m_{12}^2, m_{23}^2)|^2 \otimes_m Res(m) \cdot \epsilon(m_{12}^2, m_{23}^2)}$$

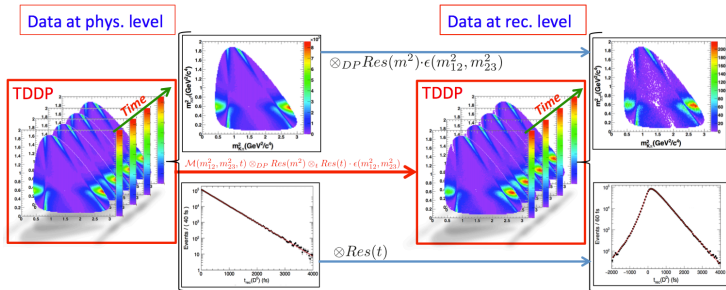


# Time-dependent Dalitz analysis

## ► p.d.f of signal for TDDA:

- (1) efficiency plane  $\epsilon(m_{12,i}^2, m_{23,i}^2)$  and mass resolution  $Res(m)$ , similar with TIDA.
- (2) time resolution  $Res(t)$  effect: usually based on data.
- (3) normalization: numerical integration on full t-dept DP region.

$$p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2, t_i) = \frac{1}{N} \int dt' R_{\text{sig}}(t_i - t', k\sigma_t^i) |\mathcal{M}(m_{12,i}^2, m_{23,i}^2, t')|^2 \otimes_m Res(m) \cdot \epsilon(m_{12,i}^2, m_{23,i}^2)$$



## ► Method: Unbinned Maximum Likelihood (UML) and consideration of Punzi bias

$$2 \ln \mathcal{L} = 2 \sum_i^n \{ \ln(f_{\text{sig}}^i p_{\text{sig}}(m_{12,i}^2, m_{23,i}^2, t_i, k\sigma_t^i; \mathbf{x}, \mathbf{y}, \mathbf{q}/p) p_{\text{sig}}^{\text{nc}}(\sigma_t^i) + \sum_{x=bg} f_x^i p_x(m_{12,i}^2, m_{23,i}^2, t_i) p_x^{\text{nc}}(\sigma_t^i) \}$$

here  $p_x^{\text{nc}}(\sigma_t^i)$  is a function of global time error function, independent on other variables





# Self-conjugated decay $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

- TDDA in  $D^0$  self-conjugated decays:

(1) direct measurement for  $x$  and  $y$ ; (2) search for CPV:  $q/p \neq 1$

$$|\mathcal{M}(f, t)|^2 = \frac{e^{-\Gamma t}}{2} [ (|A_f|^2 + |\bar{q}/p|^2 |A_{\bar{f}}|^2) \cosh(y\Gamma t) + (|A_f|^2 - |\bar{q}/p|^2 |A_{\bar{f}}|^2) \cos(x\Gamma t) + 2 \operatorname{Re}[\frac{\bar{q}}{p} A_f A_{\bar{f}}^*] \sinh(y\Gamma t) + 2 \operatorname{Im}[\frac{\bar{q}}{p} A_f A_{\bar{f}}^*] \sin(x\Gamma t) ]$$

- $D^0 \rightarrow K_S^0 \pi^+ \pi^-$  with quasis-two-body decays with difference physics process:

Right-Sign:  $A_f = \langle f | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{A_f}{A_{\bar{f}}} = \left| \frac{A_f}{A_{\bar{f}}} \right| \frac{1-\epsilon}{1+\epsilon} e^{i(\delta+\phi)}$ ; eg:  $D^0 \rightarrow K^{*-} \pi^+$  etc.

Wrong-Sign:  $A_{\bar{f}} = \langle \bar{f} | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{A_{\bar{f}}}{A_f} = \left| \frac{A_{\bar{f}}}{A_f} \right| \frac{1-\epsilon}{1+\epsilon} e^{-i(\delta-\phi)}$ ; eg:  $D^0 \rightarrow K^{*+} \pi^-$  etc.

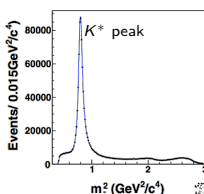
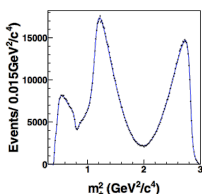
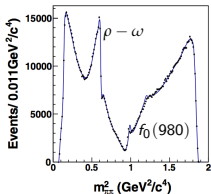
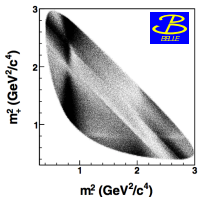
CP-even:  $A_+ = \langle + | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{A_+}{A_+} = + \frac{1-\epsilon}{1+\epsilon} e^{+i\phi}$ ; eg:  $D^0 \rightarrow K_S^0 f_0$  etc.

CP-odd:  $A_- = \langle - | \mathcal{H} | D^0 \rangle$ ;  $\frac{q}{p} \frac{A_-}{A_-} = - \frac{1-\epsilon}{1+\epsilon} e^{-i\phi}$ ; eg:  $D^0 \rightarrow K_S^0 \rho / K_S^0 \omega$  etc.



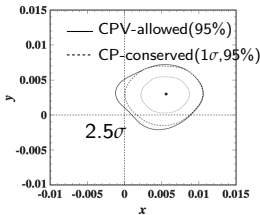
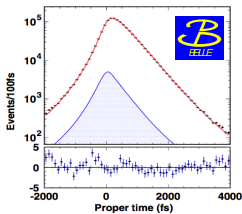
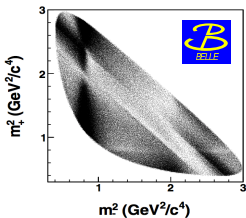
- Review of Belle's result of TDDA in this decay [PRD 89, 091103(R) (2014)]

- $D^0$  flavor is tagged via the charge of slow  $\pi_s$  from  $D^{*+} \rightarrow D^0 \pi_s^+$ .
- Dalitz variables  $m_-^2 = m_{K_S^0 \pi^-}^2$ ,  $m_+^2 = m_{K_S^0 \pi^+}^2$  for  $D^0$ , exchange for  $\bar{D}^0$ .
- Dalitz Model: 12 RBW+K-matrix( $\pi\pi$  S-wave)+LASS( $K\pi$  S-wave).



# Dataset size effect on TDDA in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

- Results of TDDA based on  $921 \text{ fb}^{-1}$  of data at Belle [PRD 89, 091103(R) (2014)]
  - a consistent determination of  $D^0$ - $\bar{D}^0$  mixing with significantly improve sensitivity.
  - the most accurate value of CPV parameters  $|q/p|$  and  $\arg(q/p)$ .



- Prospects at Belle II with larger dataset:  $\sigma_{\text{Belle II}} = \sqrt{(\sigma_{\text{stat}}^2 + \sigma_{\text{sys}}^2) \frac{\mathcal{L}_{\text{Belle}}}{50 \text{ ab}^{-1}} + \sigma_{\text{irreducible}}^2}$
- a significantly improved  $\sigma_{\text{stat}}$ ; Dalitz model uncertainty will dominate the errors.  
 $\Rightarrow$  model-indept. Dalitz analysis will be more promising in this channel.

| Fit type | Para.               | Belle II prospect                          |                       |                       | model-indept.<br>100 M signals | LHCb<br>50 $\text{fb}^{-1}$ |
|----------|---------------------|--|-----------------------|-----------------------|--------------------------------|-----------------------------|
|          |                     | Belle Fit result<br>921 $\text{fb}^{-1}$   | 5 $\text{ab}^{-1}$    | 50 $\text{ab}^{-1}$   |                                |                             |
| No CPV   | x(%)                | $0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$  | $\pm 0.08 \pm 0.11$   | $\pm 0.03 \pm 0.11$   | $\pm 0.017$                    |                             |
|          | y(%)                | $0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$  | $\pm 0.06 \pm 0.05$   | $\pm 0.02 \pm 0.04$   | $\pm 0.019$                    |                             |
| indirect | x(%)                | $0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$  | $\pm 0.08 \pm 0.11$   | $\pm 0.03 \pm 0.11$   |                                | 0.04                        |
|          | y(%)                | $0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$  | $\pm 0.06 \pm 0.05$   | $\pm 0.02 \pm 0.04$   |                                | 0.004                       |
| CPV      | $ q/p $             | $0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$ | $\pm 0.069 \pm 0.073$ | $\pm 0.022 \pm 0.069$ |                                | 0.04                        |
|          | $\arg(q/p)(^\circ)$ | $-6 \pm 11 \pm 3^{+3}_{-4}$                | $\pm 4.7 \pm 4.2$     | $\pm 1.5 \pm 3.8$     |                                | 3                           |



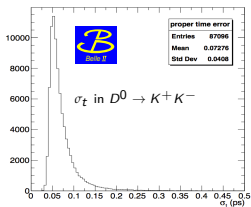
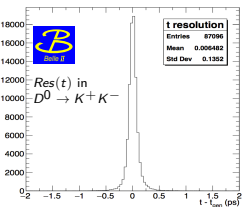
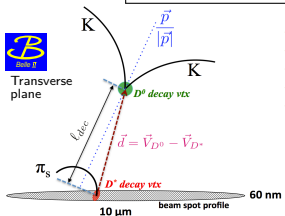
Improved  $D^0$  lifetime resolution at Belle II

- Time resolution is essential in time-dependent measurements of  $D^0$ - $\bar{D}^0$  mixing and CPV.

- such as the time-dependent amplitude of  $D^0 \rightarrow f$  (here  $t[\tau_{D^0}]$  and  $\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f}$ ):

$$\Gamma(D^0(t) \rightarrow f) \propto |\mathcal{A}_f|^2 e^{-t} \left( \frac{1+|\lambda_f|^2}{2} \cosh(yt) - \text{Re}(\lambda_f) \sinh(yt) + \frac{1-|\lambda_f|^2}{2} \cos(xt) + \text{Im}(\lambda_f) \sin(xt) \right) \otimes_t \text{Res}(t)$$

- $D^0$  lifetime:  $t = \frac{\ell_{\text{dec}}}{c\beta\gamma} = \frac{m_D}{cp} \vec{d} \cdot \frac{\vec{p}}{p}$  and  $\sigma_t$  by error matrix of vertex fits and momentum.



- Based on MC study,  $D^0$  lifetime resolution  $\text{Res}(t) \approx 140$  fs: half of BaBar's (270 fs)

- Time error  $\sigma_t$ : 1/3 of BaBar's; and  $\text{RMS}(\sigma_t)$  reduced by half.

- resolution function  $g(t) = \text{Gauss}(\mu, k\sigma_t)$ , reduced  $\text{RMS}(\sigma_t)$  (higher weight in the fit) results in an increased statistics

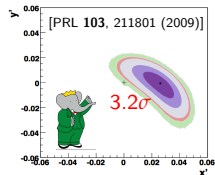
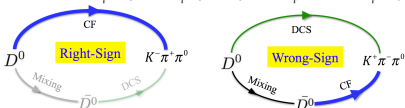


Time resolution effect on TDDA in  $D^0 \rightarrow K^+ \pi^- \pi^0$ 

- TDDP fit on  $D^0 \rightarrow K^+ \pi^- \pi^0$  WS decays to extract mixing par. ( $x''/r_0, y''/r_0$ )

$$|A_{\bar{f}}|^2 = \left[ |A_{\bar{f}}^{DCS}|^2 e^{-\Gamma t} + \frac{(x^2 + y^2)}{4r_0^2} |A_{\bar{f}}^{CF}|^2 (\Gamma t)^2 e^{-\Gamma t} + \left( \frac{y''}{r_0} \text{Re}[A_{\bar{f}}^{DCS} \bar{A}_{\bar{f}}^{CF}] + \frac{x''}{r_0} \text{Im}[A_{\bar{f}}^{DCS} \bar{A}_{\bar{f}}^{CF}] \right) (\Gamma t) e^{-\Gamma t} \right] \otimes_t \text{Res}(t)$$

where  $x'' = x \cos \delta_{K\rho} + y \sin \delta_{K\rho}$ ,  $y'' = y \cos \delta_{K\rho} - x \sin \delta_{K\rho}$ ,  $r_0 = |A^{CF}| / |A^{DCS}|$ .



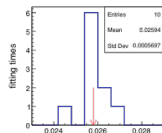
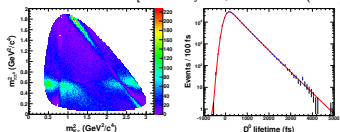
- BaBar performed TDDA with  $384 \text{ fb}^{-1}$ :

$$x'' = (2.61_{-0.68}^{+0.57} \pm 0.39)\%, \quad y'' = (-0.06_{-0.64}^{+0.55} \pm 0.34)\%$$

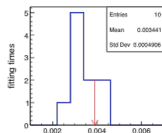
$\Rightarrow$  the first evidence to veto the hypothesis of no  $D^0$ - $\bar{D}^0$  mixing in  $D^0$  multi-body decays.

- ToyMC: smear exponential lifetime with Gauss ( $\sigma=140$  fs) to consider the improved time resolution at Belle II; without considering background effects.
- Sensitivity estimation: **one order of magnitude improvement than BaBar**

detailed info. see [Chin. Phys. C, **41**: 023001 (2017)]



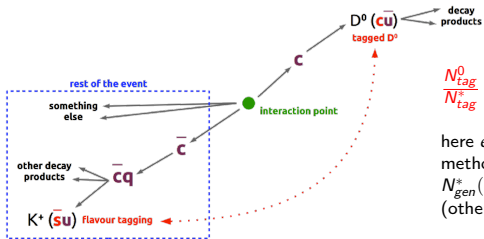
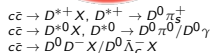
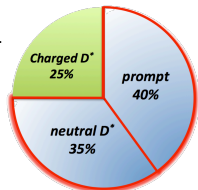
$$\sigma_x = 0.060\%$$



$$\sigma_y = 0.049\%$$

# A new $D^0$ -tag method at Belle II: ROE method

- To measure CPV, the flavor of  $D$  is needed to be determined efficiently.
- At B-factories, the charge of  $\pi_S$  from  $D^{*+} \rightarrow D^0 \pi_S^+$  is used to tag the flavor of  $D^0$  and  $D^0$  mesons from  $B$  decays are excluded.  
 $\Rightarrow$  only  $D^0$  from  $D^{*\pm}$  in  $c\bar{c}$  events (25%) were used.
- To utilize another charm meson decay is the essential idea of ROE.
- ROE method: select events with only one  $K^\pm$  in the Rest Of Event;
- Using the charge of this  $K^\pm$  in ROE to determine the flavor of  $D^0$ .



$$\frac{N_{tag}^0}{N_{tag}^*} = \frac{\epsilon_{tag}^0}{\epsilon_{tag}^*} \cdot \frac{N_{gen}^0 + (1 - \epsilon_{tag}^*) \cdot N_{gen}^*}{N_{gen}^*} \sim 1$$

here  $\epsilon_{tag}^*$  ( $\epsilon_{tag}^0$ ): tagging efficiency of  $D^*$  (ROE) method with 80% ( $\leq 20\%$ ).

$N_{gen}^*$  ( $N_{gen}^0$ ): number of  $D^0$  produced by a  $D^*$  (other  $c\bar{c}$  event) with  $N_{gen}^*$  :  $N_{gen}^0 \simeq 1 : 3$

A reduction of  $\sim 15\%$  of  $\sigma(stat)$  on  $A_{CP}$

an additional  $D^0$  sample via ROE method will be available and optimistic.



# Outline

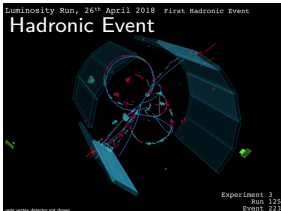
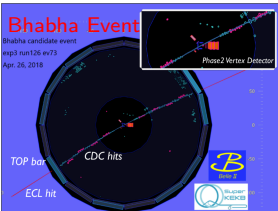
- 1 Belle experiment to Belle II experiment
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  - Prospect of TDDA in  $D^0 \rightarrow K^+ \pi^- \pi^0$
  - A new  $D^0$ -tag method: ROE method
- 3 Re-discoveries of Phase2 at Belle II
- 4 Summary



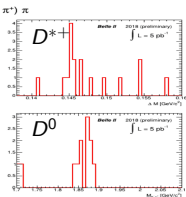
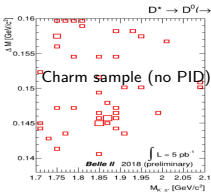
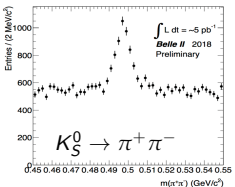
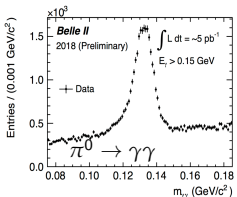
# Some 'first' events and re-dcoveries with first data

- First collision and 'First' events

First collision at April 25, 2018

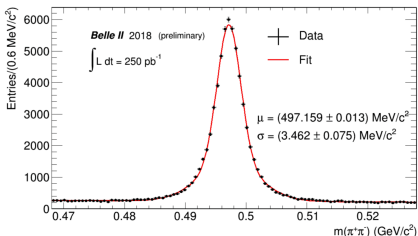
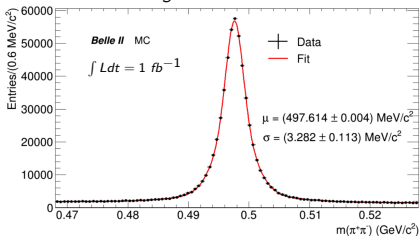


- First data (5 pb<sup>-1</sup>) gave evidences of  $\pi^0/K_S^0$ /charm. Calibrations at a very early stage.



# $K_S^0$ invariant Mass

- Belle II has already finished Phase 2 on Jul 17 with  $\sim xxx \text{ pb}^{-1}$  (wait official statement).
- Some approval plots on up to  $250 \text{ pb}^{-1}$ : with requirement of at least tree tracks from the IP region, while rejecting beam included background, Bhabha events and other low multiplicity background sources.
- for example of  $K_S^0 \rightarrow \pi^+ \pi^-$  with partial Phase2 dataset.



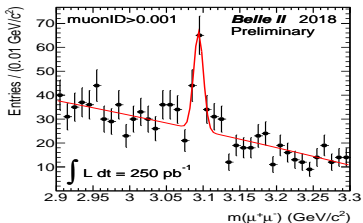
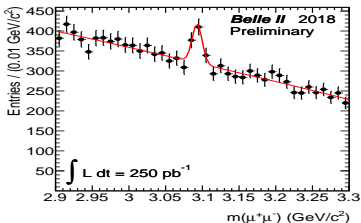
- $K_S^0$  mass resolutions within a few % of what expected by the simulation.
- Tracking efficiency measurements are ongoing.



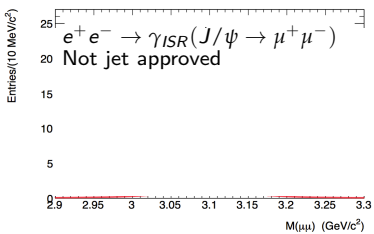
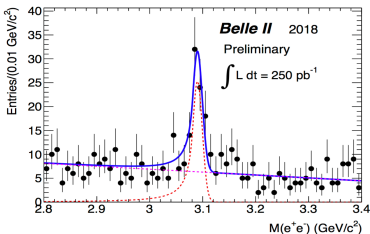


# Re-discovery: November revolution in June

- re-discovery of  $J/\psi \rightarrow \mu^+ \mu^-$  in  $250 \text{ pb}^{-1}$  of Phase 2 data w/o and w/ muonID.

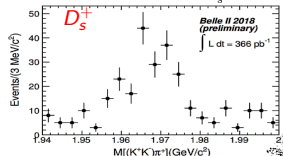
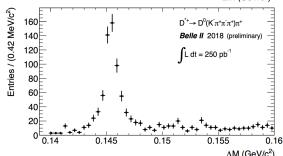
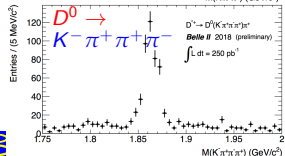
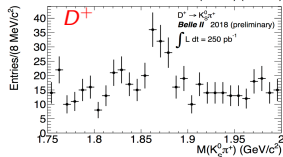
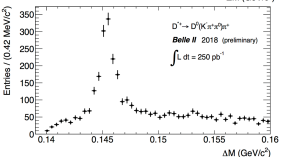
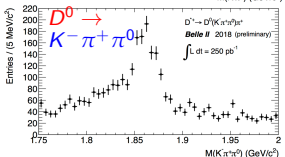
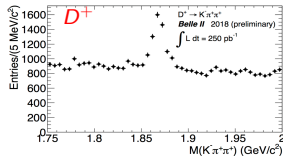
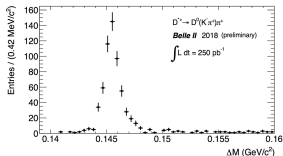
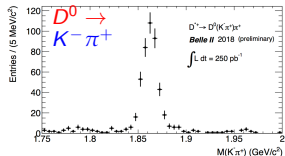


- other processes, like  $J/\psi \rightarrow e^+ e^-$  and  $e^+ e^- \rightarrow \gamma_{ISR}(J/\psi \rightarrow \mu^+ \mu^-)$ .



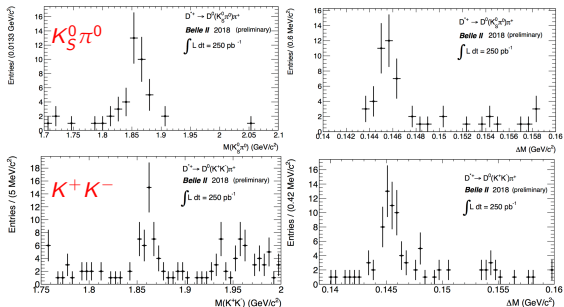
# Re-discovery: charm sample with definite flavor

- Each  $c\bar{c}$  event at B-factories has averaged  $\bar{N}(D^0) = 1.119 \pm 0.007$ ,  $\bar{N}(D^+) = 0.595 \pm 0.005$ ,  $\bar{N}(D_s^+) = 0.195 \pm 0.003$ .
- $D^0$  CF decays  $K\pi$ ,  $K\pi\pi^0$  and  $K\pi\pi\pi$  with flavor tagged, and  $D_s^+$  are observed.

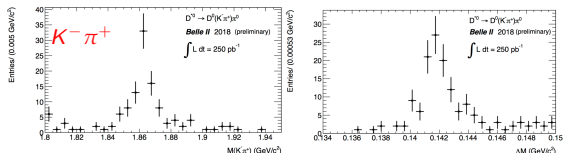


# Re-discovery: $D^0$ sample in other channels

- in  $D^{*+}$  sample: CP eigenstate decays of  $D^0 \rightarrow K_S^0 \pi^0$  (CF) and  $D^0 \rightarrow K^+ K^-$  (SCS) are observed.

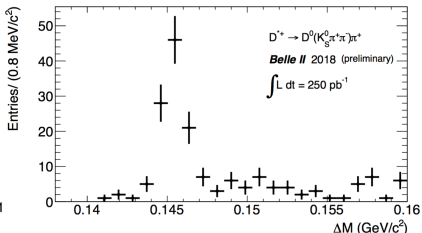
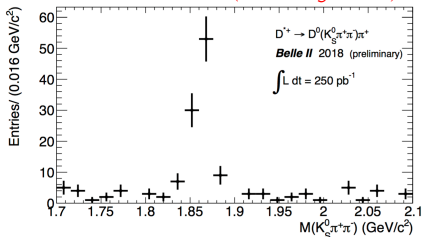


- In  $D^{*0}$  sample:  $D^0 \rightarrow K^- \pi^+$  is observed.



# Re-discovery: charm sample

- Golden channel  $D^{*+} \rightarrow (D^0 \rightarrow K_S^0 \pi^+ \pi^-) \pi^+$  is observed with high purity



- what is the future with full Belle II dataset ( $\times 40,000$ ) for this channel? most precise result on  $D^0-\bar{D}^0$  mixing? observation CPV in charm?



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# Summary

- **Belle II is back to the game** after eight year passed since Belle shut down.
- Belle II will have a rich charm physics program ahead. **TDDA** will become one of favourites of Belle II charm WG to study  $D^0$ - $\bar{D}^0$  mixing and  $CP$  violation in many multi-body decays.
- Considering **50 times dataset** and **half of  $D^0$  lifetime resolution** at Belle II, two sensitivity estimations in **TDDA** are presented:
  - Prospect in  $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ : factor 3 improved, and Dalitz model will dominate the errors.
  - Prospect in  $D^0 \rightarrow K^+ \pi^- \pi^0$ : one order of magnitude improved w/o considering the bkg effects.
  - more decay channels will contribute  $D^0$ - $\bar{D}^0$  mixing and CPV via TDDA benefiting from improved performances and a large data set.
- **ROE  $D^0$  tagging method** is presented: provides an additional tagged  $D^0$  sample.
- **Phase2 has finished**, some re-discoveries with  $250 \text{ pb}^{-1}$  are shown, especially charm sample in many channels.
- **Phase3 operation** (physics run) with full Belle II detector will **start next spring**.
- Looking forward to **charming news on charm physics via TDDA**.



Thank you for your attention.

谢谢!

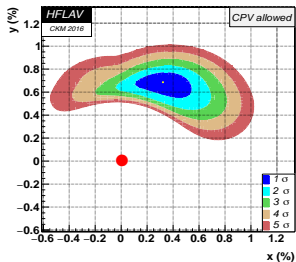


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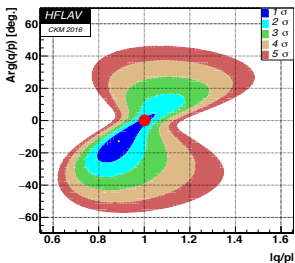


# Status of $D^0-\bar{D}^0$ mixing and $CP$ violation [mainly ref. charm physics at HFLAV]

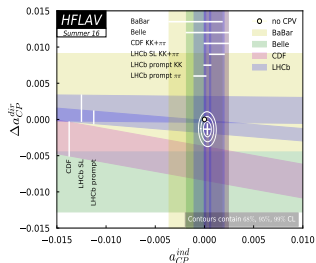
$D^0-\bar{D}^0$  mixing



indirect  $CP$  violation



$CP$  violation in  $D^0 \rightarrow KK/\pi\pi$



- $\gg 11.5\sigma$  to exclude no mixing  $(x,y)=(0,0)$  with CPV-allowed
- No hints for indirect CPV  $\Leftarrow$  no direct CPV  $(|q/p|,\phi)=(1,0)$  at C.L=40%
- No clear evidence of direct CPV  $\Leftarrow$  no CPV at C.L=9.3%

$D^0-\bar{D}^0$  mixing observation in more channels, and  $CPV$  searches are two of most important physical goals for Charm WG at our Belle II experiment.

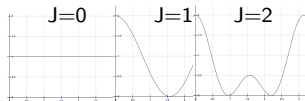


# description of angular function $W_r$

- (1) Helicity form: [Phys. Rev. D **78**, 052001 (2008)]

easily understood, but need many Lorentz transform, take much time on calculation

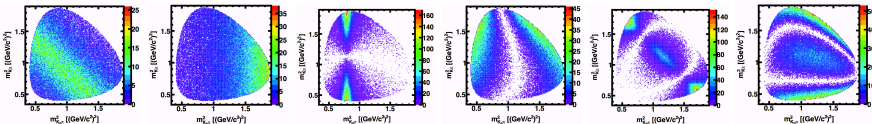
$$\begin{aligned} \mathcal{A}_r &= F_D \times F_r \times T_r \times (|p|^J |q|^J P_J(\cos \theta_H^r)) \\ W_r(J=0) &= 1 && \propto \text{const.} \\ W_r(J=1) &= -2(\vec{p} \cdot \vec{q}) = -2|p||q| \cos \theta_H && \propto \cos \theta_H \\ W_r(J=2) &= \frac{16}{3}|p|^2|q|^2(3 \cos^2 \theta_H - 1) && \propto \cos^2 \theta_H \end{aligned}$$



- (2) Zemach covariant tensor form: [Phys. Rev. **133**, B1201 (1964), Phys. Rev. **140**, B109 (1965)]

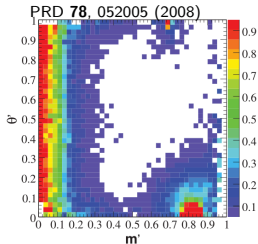
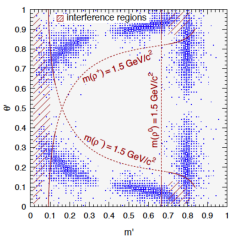
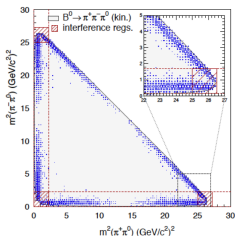
difficult to understand, usually only used in spin-0 final state particles, but take less time in calculation

$$\begin{aligned} W_r(J=0) &= 1 \\ W_r(J=1) &= m_{ac}^2 - m_{bc}^2 + \frac{(M_D^2 - M_C^2)(M_b^2 - M_a^2)}{M^2} \\ W_r(J=2) &= \left[ m_{bc}^2 - m_{ac}^2 + \frac{(M_D^2 - M_C^2)(M_a^2 - M_b^2)}{M^2} \right]^2 - \frac{1}{3} \left[ m_{ab}^2 - 2M_D^2 - 2M_C^2 + \frac{(M_D^2 - M_C^2)^2}{M^2} \right] \times \left[ m_{ab}^2 - 2M_a^2 - 2M_b^2 + \frac{(M_a^2 - M_b^2)^2}{M^2} \right] \end{aligned}$$



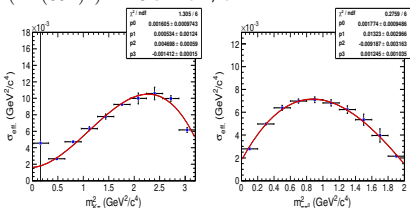
# Square Dalitz Plot Method

- In Dalitz analyses of  $B$  meson decays, the cared interference region is usually concentrate on the marginal area (left figure).
- To avoid the variation of efficiency plane in one bin, a better Dalitz plot region with better resolution is needed.
- It can also efficiently describe efficiency plane or background distribution on Dalitz plot, such as misidentified background in  $B \rightarrow K\pi\pi^0$  (right figure).
- Expanded Dalitz plot plane  $[0, 1] \times [0, 1]$ : square Dalitz Plot (SDP) [PRD 72, 052002 (2005)]
  - $m' = \frac{1}{\pi} \arccos \left( 2 \frac{m_{ab} - m_{ab}^{min}}{m_{ab}^{max} - m_{ab}^{min}} - 1 \right) \in [0, 1]$       $\theta' = \frac{1}{\pi} \theta_{ab} \in [0, 1]$
  - where  $m_{ab}^{max} = M_B - m_c$ ,  $m_{ab}^{min} = m_a + m_b$ , Jacobian determinant  $|J|$  meets:  $dm_{12}^2 dm_{23}^2 = |J| dm' d\theta'$

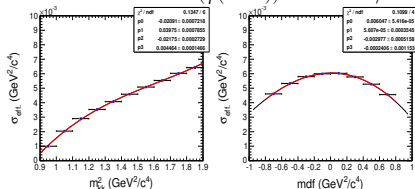


# Mass resolution problem in Dalitz analysis

- In  $D^0 \rightarrow K^+ \pi^- \pi^0$ , Dalitz resolution meets  $\sigma(m^2) \ll 2m_r \cdot \Gamma_r$ , but narrowest width of intermediate states is  $\Gamma(K^*(892)^0) = 48.7 \text{ MeV}/c^2$



- In  $D^0 \rightarrow K_S^0 K^+ K^-$ , Dalitz resolution meets  $\sigma(m^2) \sim 2m_r \cdot \Gamma_r$ , but narrowest width of intermediate states is  $\Gamma(\phi(1020)) = 4.38 \text{ MeV}/c^2$ .



here DP uses  $m_{KK}^2 = C - (m_+^2 + m_-^2)$  and  $mdf = m_+^2 - m_-^2$

- Strictly speaking, a convolution is needed on whole region of DP to consider the resolution effects: a time-consuming challenge for CPU.
- A discretization of convolution via a grid weight method: decide grid size by resolution, and use averaged value of around grid points with weight  $W_{ij} = e^{-(i^2+j^2)/2}$ , the normalized form is as follows:

$$pdf_{resol}(x, y) = \frac{\sum_{l=-3, j=-3}^{3, 3} pdf(x + l\sigma_x, y + j\sigma_y) \cdot W_{lj}}{\sum_{l=-3, j=-3}^{3, 3} W_{lj}}$$



## Efficiency difference between data and MC

- To consider the difference of particle identification(PID) efficiency between data and MC, a data-driven efficiency plane is applied.
- Obtain a 2D table of the ratio of each charged particles' PID efficiency between data and MC, dependent on various particles' momentum and PID requirement.
- re-weight each event in reconstructed DP according its momentum, PID requirement and above ratio value, then obtain the data-driven efficiency plane by the ratio of corrected rec. DP plane to gen. DP plane.

