

Belle II perspectives on charm

(in the light of recent LHCb results)

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- $D^0 - \bar{D}^0$ mixing and t-dependent CPV
- t-integrated CPV (A_{CP})
- Rare decays (FCNC, LFV, LV)

$D^0 - \bar{D}^0$ mixing

- Mass eigenstates differ from flavor eigenstates

$$|D_{1,2}^0\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

- $D_{1,2}^0$ with masses m_1, m_2 and partial widths Γ_1, Γ_2
- CP violation if $q \neq p$
- Mixing parameters:

$$x = \frac{\Delta m}{\Gamma} \qquad y = \frac{\Delta\Gamma}{2\Gamma}$$

- Time dependent decay rates of $D^0 \rightarrow f$ (since mixing is small):

$$\frac{dN_{D^0 \rightarrow f}}{dt} \propto e^{-\Gamma t} \left| \langle f | \mathcal{H} | D^0 \rangle + \frac{q}{p} \left(\frac{y + ix}{2} \Gamma t \right) \langle f | \mathcal{H} | \bar{D}^0 \rangle \right|^2$$

Measurement strategies

$$\frac{dN_{D^0 \rightarrow f}}{dt} \propto e^{-\Gamma t} \left| \langle f | \mathcal{H} | D^0 \rangle + \frac{q}{p} \left(\frac{y+ix}{2} \Gamma t \right) \langle f | \mathcal{H} | \bar{D}^0 \rangle \right|^2$$

- Wrong-sign semileptonic decays ($D^0 \rightarrow K^+ \ell^- \nu$)
 - WS only via mixing: $\langle f | \mathcal{H} | D^0 \rangle = 0$
 - measures time integrated mixing rate $R_M = \frac{x^2 + y^2}{2} = \frac{N_{WS}}{N_{RS}}$
- Wrong-sign hadronic decays ($D^0 \rightarrow K^+ \pi^-$)
 - WS via doubly Cabibbo suppressed (DCS) decays or mixing
 - interference between DCS and mixing (strong phase δ)
 - measures $x' = x \cos \delta + y \sin \delta$, $y' = y \cos \delta - x \sin \delta$
- Decays to CP eigenstates ($D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$)
 - if no direct CPV: $\langle f | \mathcal{H} | \bar{D}^0 \rangle = -\langle f | \mathcal{H} | D^0 \rangle$
 - measures y
- Decays to self-conjugate states ($D^0 \rightarrow K_S^0 \pi^+ \pi^-$)
 - time dependent Dalitz plot analysis
 - measures x and y

CP violation

$$\frac{dN_{D^0 \rightarrow f}}{dt} \propto e^{-\Gamma t} \left| \langle f | \mathcal{H} | D^0 \rangle + \frac{q}{p} \left(\frac{\gamma + i\chi}{2} \Gamma t \right) \langle f | \mathcal{H} | \bar{D}^0 \rangle \right|^2$$

- $q/p \neq 1 \Rightarrow$ indirect CP violation
- $q/p = |q/p| \cdot e^{i\phi}$:
 - $|q/p| \neq 1 \Rightarrow$ CP violation in mixing
 - $\phi \neq 0(\pi) \Rightarrow$ CP violation in interference of decays w/ and w/o mixing
- $|\mathcal{A}(D^0 \rightarrow f)|^2 \neq |\mathcal{A}(\bar{D}^0 \rightarrow \bar{f})|^2 \Rightarrow$ direct CP violation

Experimental techniques

- Time-dependent analysis:
 - difference in proper decay time distributions of $D^0 \rightarrow f$ and $\bar{D}^0 \rightarrow \bar{f}$
 - measure indirect CPV
- Time-integrated analysis:
 - difference in time-integrated decay rates of $D^0 \rightarrow f$ and $\bar{D}^0 \rightarrow \bar{f}$
 - measure direct+indirect CPV

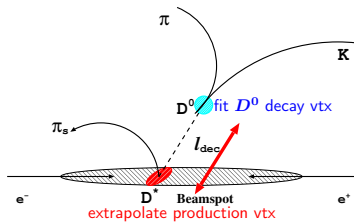
Experimental method at B-factories

- $D^{*+} \rightarrow D^0 \pi_{\text{slow}}^+$
 - flavor tagging by π_{slow} charge
 - background suppression
- D^0 proper decay time measurement:

$$t = \frac{l_{\text{dec}}}{c\beta\gamma}, \quad \beta\gamma = \frac{p_{D^0}}{M_{D^0}}$$

- Measurements performed mainly at $\Upsilon(4S)$
 - D^{*+} from B decays can be completely rejected with

$$p_{D^{*+}}^{\text{CMS}} > 2.5 \text{ GeV}/c$$



t-integrated measurements (A_{CP})

- Asymmetry in time-integrated decay rates of $D^0 \rightarrow f$ and $\bar{D}^0 \rightarrow \bar{f}$

$$A_{CP}^f = \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$$

- Raw asymmetry

$$A_{\text{raw}} = \frac{N - \bar{N}}{N + \bar{N}} = A_D + A_\epsilon^f + A_{CP}^f$$

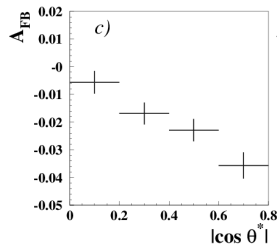
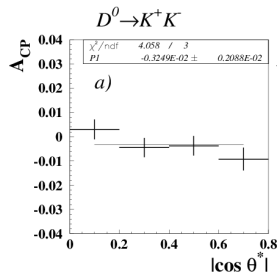
- A_D production asymmetry
- A_ϵ^f asymmetry in efficiencies
- Production at B-factory is symmetric
 - huge benefit vs. LHC
 - however: odd function of CMS polar angle

$$A_D \equiv A_{FB}(\cos\theta^*)$$

- can easily be disentangled

$$A_{CP} = \frac{A_{\text{raw}}^{\text{COR}}(\cos\theta^*) + A_{\text{raw}}^{\text{COR}}(-\cos\theta^*)}{2}$$

$$A_{FB} = \frac{A_{\text{raw}}^{\text{COR}}(\cos\theta^*) - A_{\text{raw}}^{\text{COR}}(-\cos\theta^*)}{2}$$



Detection asymmetries

- Asymmetries in detection efficiencies can be measured with sufficient precision using CF decays (CPV is very unlikely)
 - must be performed in bins of relevant phase-spaces
 - requires production asymmetries to be known
 - at B-factory: $A_D \equiv A_{FB}(\cos\theta^*)$
- Slow pions: from tagged and untagged $D^0 \rightarrow K^- \pi^+$ decays
- Kaons: from decays $D^0 \rightarrow K^- \pi^+$ and $D_s^+ \rightarrow \phi \pi^+$
- Pions: from decays $D^+ \rightarrow K^- \pi^+ \pi^+$ and $D^0 \rightarrow K^- \pi^+ \pi^0$

Recent LHCb results

- A_{Γ} (1 fb^{-1} @ 7 TeV) PRL 112, 041801 (2014)
 - no evidence for CPV
 - $4\times$ better sensitivity compared to Belle result at 1 ab^{-1}
- $D^0 \rightarrow K^+ \pi^-$ (3 fb^{-1} @ 7-8 TeV) PRL 111, 251801 (2013)
 - observation of mixing
 - no evidence for CPV
- $\Delta A_{CP} = A_{CP}^{KK} - A_{CP}^{\pi\pi}$ (1 fb^{-1} @ 7 TeV) LHCb-CONF-2013-003
PLB 723 (2013) 33
 - update of prompt D^* sample
 - $B \rightarrow D^0 \mu X$ sample ($2\times$ less sensitive)
 - no evidence for CPV
- A_{CP} for $D^+ \rightarrow \phi \pi^+$ (1 fb^{-1} @ 7 TeV) JHEP 06 (2013) 112
 - equal systematic and statistic uncertainties
 - no evidence for CPV
- y_{CP} (0.03 fb^{-1}) JHEP 04 (2012) 129
 - on very small (low luminosity) sample - no update available yet

Recent LHCb results compared to Belle

- Uncertainty is statistics and systematics added in quadrature
- Naive average of the two LHCb results in case of A_{Γ} and ΔA_{CP}

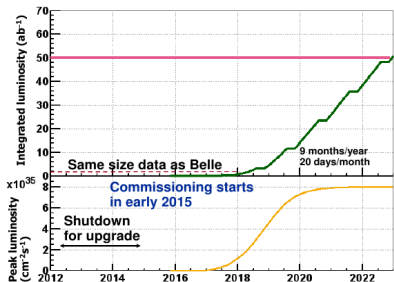
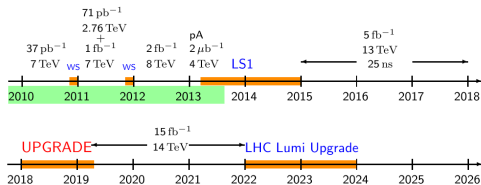
	LHCb	lumin. fb^{-1}	Belle	lumin. ab^{-1}	
A_{Γ}	$(-0.017 \pm 0.054)\%$	1	$(-0.03 \pm 0.22)\%$	1	naive av.
ΔA_{CP}	$(-0.15 \pm 0.16)\%$	1	$(-0.87 \pm 0.41)\%$	1	naive av.
x'^2	$(5.5 \pm 4.9) \times 10^{-5}$	3	$(18 \pm 22) \times 10^{-5}$	0.4	no CPV
y'	$(4.8 \pm 1.0) \times 10^{-3}$	3	$(0.6 \pm 4.0) \times 10^{-3}$	0.4	no CPV
y_{CP}	$(0.55 \pm 0.75)\%$	0.03	$(1.11 \pm 0.25)\%$	1	
$A_{CP}^{\phi\pi^+}$	$(-0.04 \pm 0.20)\%$	1	$(0.51 \pm 0.28)\%$	1	

- Equivalent Belle II luminosity to obtain the sensitivity of LHCb measurements at 1 fb^{-1} can be roughly estimated with

$$\mathcal{L}_{\text{BelleII}}^{\text{equiv}} = \left(\frac{\sigma_{\text{Belle}}}{\sigma_{\text{LHCb}}} \right)^2 \frac{\mathcal{L}_{\text{Belle}}}{\mathcal{L}_{\text{LHCb}}}$$

LHCb/Belle II schedules

- LHCb (A. Contu, Charm 2013)
 - expect $\sim 8 \text{ fb}^{-1}$ by 2018
 - 2018 - mid 2019 upgrade (3 - 4 \times increase in D meson yields)
 - then additional 15 fb^{-1} by 2022
- Belle II
 - 2017: start to increase luminosity
 - collect $\sim 10 \text{ ab}^{-1}$ by mid 2019
 - collect 50 ab^{-1} by 2023



Equivalent Belle II integrated luminosity

A_{Γ}	1 fb^{-1} (LHCb)	\sim	16 ab^{-1} (Belle II)
ΔA_{CP}	1 fb^{-1} (LHCb)	\sim	7 ab^{-1} (Belle II)
x'^2, y'	1 fb^{-1} (LHCb)	\sim	2.5 ab^{-1} (Belle II)
y_{CP}	1 fb^{-1} (LHCb)	\sim	4 ab^{-1} (Belle II)
$A_{CP}^{\phi\pi^+}$	1 fb^{-1} (LHCb)	\sim	2 ab^{-1} (Belle II)

- Will not be competitive in A_{Γ} and ΔA_{CP}
 - but Belle II can measure A_{CP}^{KK} and $A_{CP}^{\pi\pi}$ separately
- Maybe still competitive in x'^2, y' and y_{CP}
 - y_{CP} comparison based on initial low luminosity LHCb data (0.03 fb^{-1})
→ extrapolation to 1 fb^{-1} might be too optimistic
- t-dependent Dalitz ?
- A_{CP} measurements: Belle II in favor because of symmetric production

Prospects at Belle II for mixing and CPV

- Belle measurements extrapolated to 50 ab^{-1}
- Systematics primarily scales with integrated luminosity, with two exceptions:
 - t-dependent Dalitz: model related systematics (resonance parameters - masses, widths, form factors, angular dependence etc.)
 - A_{CP} of modes with K_s^0 : asymmetry of K^0/\bar{K}^0 interactions in material (PRD 84, 111501 (2011)), $\sigma_{\text{ired}} \approx 0.02\%$
- Extrapolation:

$$\sigma_{\text{BelleII}} = \sqrt{(\sigma_{\text{stat}}^2 + \sigma_{\text{sys}}^2) \frac{\mathcal{L}^{\text{Belle}}}{50 \text{ ab}^{-1}} + \sigma_{\text{ired}}^2}$$

Mixing and indirect CPV

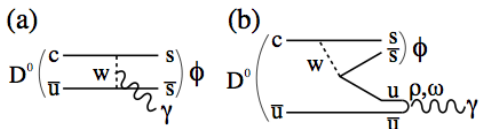
$D^0 \rightarrow K^{(*)-} \ell^+ \nu$	492 fb^{-1}	50 ab^{-1}
R_M	$(1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$	$\pm 0.3 \times 10^{-4}$
$D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$	976 fb^{-1}	50 ab^{-1}
y_{CP}	$(1.11 \pm 0.22 \pm 0.11)\%$	$\pm 0.04\%$
A_Γ	$(-0.03 \pm 0.20 \pm 0.08)\%$	$\pm 0.03\%$
$D^0 \rightarrow K^+ \pi^-$	400 fb^{-1}	50 ab^{-1}
x'^2	$(1.8 \pm 2.2 \pm 1.1) \times 10^{-4}$	$\pm 0.22 \times 10^{-4}$
y'	$(0.06 \pm 0.40 \pm 0.20)\%$	$\pm 0.04\%$
A_M	0.67 ± 1.20	± 0.11
$ \phi $	0.16 ± 0.44	± 0.04
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	921 fb^{-1}	50 ab^{-1}
x	$(0.56 \pm 0.19 \pm 0.06 \pm 0.08)\%$	$\pm 0.08\%$
y	$(0.30 \pm 0.15 \pm 0.06 \pm 0.04)\%$	$\pm 0.05\%$
$ q/p $	$0.90 \pm 0.16 \pm 0.04 \pm 0.06$	± 0.06
ϕ	$-0.10 \pm 0.19 \pm 0.04 \pm 0.07$	± 0.07

$$|q/p| = 1 + \frac{1}{2} A_M \Rightarrow \delta|q/p| = \frac{1}{2} \delta A_M$$

Direct CPV

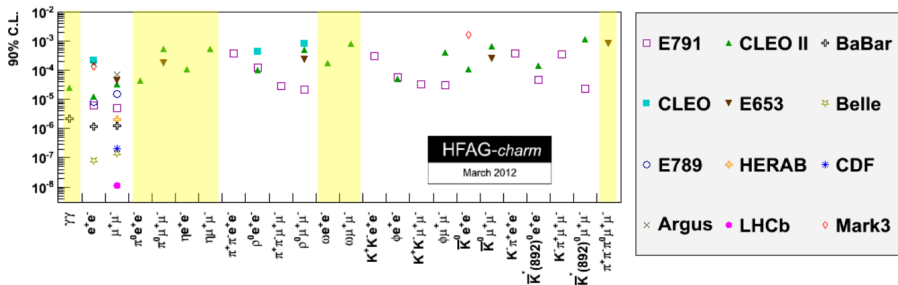
mode	\mathcal{L} (fb $^{-1}$)	A_{CP} (%)	Belle II at 50 ab $^{-1}$
$D^0 \rightarrow K^+ K^-$	976	$-0.32 \pm 0.21 \pm 0.09$	± 0.03
$D^0 \rightarrow \pi^+ \pi^-$	976	$+0.55 \pm 0.36 \pm 0.09$	± 0.05
$D^0 \rightarrow \pi^0 \pi^0$	976	$\sim \pm 0.60$	± 0.08
$D^0 \rightarrow K_s^0 \pi^0$	791	$-0.28 \pm 0.19 \pm 0.10$	± 0.03
$D^0 \rightarrow K_s^0 \eta$	791	$+0.54 \pm 0.51 \pm 0.16$	± 0.07
$D^0 \rightarrow K_s^0 \eta'$	791	$+0.98 \pm 0.67 \pm 0.14$	± 0.09
$D^0 \rightarrow \pi^+ \pi^- \pi^0$	532	$+0.43 \pm 1.30$	± 0.13
$D^0 \rightarrow K^+ \pi^- \pi^0$	281	-0.60 ± 5.30	± 0.40
$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$	281	-1.80 ± 4.40	± 0.33
$D^+ \rightarrow \phi \pi^+$	955	$+0.51 \pm 0.28 \pm 0.05$	± 0.04
$D^+ \rightarrow \eta \pi^+$	791	$+1.74 \pm 1.13 \pm 0.19$	± 0.14
$D^+ \rightarrow \eta' \pi^+$	791	$-0.12 \pm 1.12 \pm 0.17$	± 0.14
$D^+ \rightarrow K_s^0 \pi^+$	977	$-0.36 \pm 0.09 \pm 0.07$	± 0.03
$D^+ \rightarrow K_s^0 K^+$	977	$-0.25 \pm 0.28 \pm 0.14$	± 0.05
$D_s^+ \rightarrow K_s^0 \pi^+$	673	$+5.45 \pm 2.50 \pm 0.33$	± 0.29
$D_s^+ \rightarrow K_s^0 K^+$	673	$+0.12 \pm 0.36 \pm 0.22$	± 0.05

Direct CPV in $D^0 \rightarrow \phi\gamma, \rho^0\gamma$

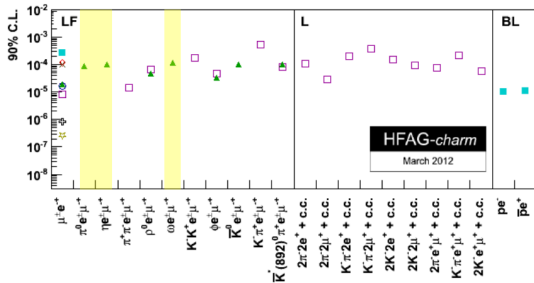


- Direct CPV in radiative decays can be enhanced to exceed 1% (G. Isidori and J. F. Kamenik, PRL 109, 171801 (2012))
 - $D^0 \rightarrow \phi\gamma$: A_{CP} up to 2%
 - $D^0 \rightarrow \rho^0\gamma$: A_{CP} up to 10%
- $D^0 \rightarrow \phi\gamma$: first observation by Belle with 78 fb^{-1} (PRL 92, 101803 (2004))
 - measured yield: $27.6^{+7.4+0.5}_{-6.5-1.0}$
 \Rightarrow relative error on yield 25% (as would be the error on A_{CP})
- A_{CP} sensitivity at 50 ab^{-1} : $\approx 1\%$

Rare and forbidden decays



- Shaded regions indicate the decays with γ or π^0
- Mostly done by CLEO
- Belle II can improve these UL by several orders of magnitude



$$D^0 \rightarrow \gamma\gamma$$

- SM predictions: long distance effects dominate

$$Br \sim \text{few} \times 10^{-8}$$

- BaBar, 470 fb^{-1}

$$Br < 2.2 \times 10^{-6} \text{ @ } 90\% \text{ CL}$$

PRD 85 (2012) 091107

- Belle II at 50 fb^{-1} :

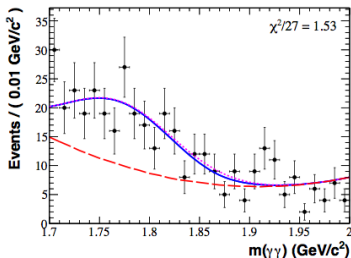
→ depends how background behaves

- if UL would scale with \mathcal{L} :

$$UL \sim 2 \times 10^{-8}$$

- if UL would scale with $\sqrt{\mathcal{L}}$:

$$UL \sim 2 \times 10^{-7}$$

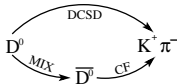


Conclusions

- Perspectives for charm measurements at Belle II have been discussed in the light of recent LHCb results.
- We focused on D-mixing and CPV.
- Using Belle results and a rough extrapolation to 50 ab^{-1} we found:
 - Belle II cannot compete with LHCb in measurements of A_{Γ} and ΔA_{CP} , but might still be competitive in x'^2 , y' and y_{CP} measurements.
 - In t-dependent Dalitz analysis of $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ the model dependent systematics will probably dominate and saturate the sensitivity.
 - Belle II is in favor in A_{CP} measurements because of symmetric D-meson production; the sensitivity would reach in some cases a 0.03% level.
- Belle II can also be competitive in searches of rare and forbidden decays of D-mesons with γ or π^0 in the final state.

t-dependent measurements: $D^0 \rightarrow K^+ \pi^-$

- Wrong sign (WS) final state:
via DCS decays or via mixing



- Proper decay time distribution

$$\frac{dN}{dt} \propto [R_D + y' \sqrt{R_D} (\Gamma t) + \frac{x'^2 + y'^2}{4} (\Gamma t)^2] e^{-\Gamma t}$$

● DCS ● interference ● mixing

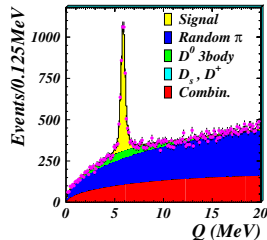
R_D ratio of DCS/CF decay rates

$$x' = x \cos \delta + y \sin \delta$$

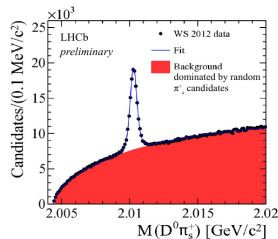
$$y' = y \cos \delta - x \sin \delta$$

δ strong phase between DCS and CF

WS events (Belle)



WS events (LHCb)



t-dependent measurements: $D^0 \rightarrow K^+\pi^-$

CP violation

- D^0 and \bar{D}^0 samples analyzed separately
 $\Rightarrow R_D^\pm, x'^{2\pm}, y'^{\pm}$
- direct CPV in DCS decays:

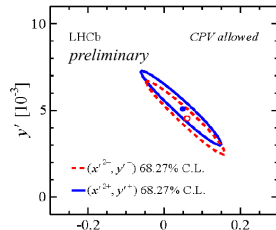
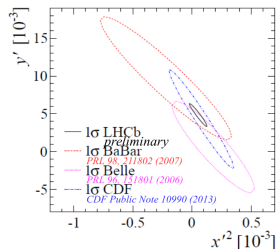
$$A_D = \frac{R_D^+ - R_D^-}{R_D^+ + R_D^-}$$

- CPV in mixing and interference \rightarrow by solving 4 equations for 4 unknowns:

$$x'^{\pm} = (1 \pm \frac{1}{2}A_M) \cdot (x' \cos \phi \pm y' \sin \phi)$$

$$y'^{\pm} = (1 \pm \frac{1}{2}A_M) \cdot (y' \cos \phi \mp x' \sin \phi)$$

$$\rightarrow x', y', \phi, |q/p| = 1 + \frac{1}{2}A_M$$



t-dependent measurements: $D^0 \rightarrow K^+K^-, \pi^+\pi^-$

- Measurement of lifetime difference between flavor specific and decays into CP final states

- choice of flavor specific: kinematically similar $D^0 \rightarrow K^-\pi^+$

- Timing distributions are exponential

- mixing parameter:

$$y_{CP} = \frac{\tau(K^-\pi^+)}{\tau(K^+K^-)} - 1$$

- $y_{CP} = y$, if CP conserved

- If CP violated \rightarrow difference in lifetimes of $D^0/\bar{D}^0 \rightarrow K^+K^-, \pi^+\pi^-$

- asymmetry in lifetimes:

$$A_{\Gamma} = \frac{\tau(\bar{D}^0 \rightarrow K^-K^+) - \tau(D^0 \rightarrow K^+K^-)}{\tau(\bar{D}^0 \rightarrow K^-K^+) + \tau(D^0 \rightarrow K^+K^-)}$$

- If direct CPV negligible:

- $y_{CP} = y \cos \phi - \frac{1}{2} A_{MX} \sin \phi$
- $A_{\Gamma} = \frac{1}{2} A_{MY} \cos \phi - x \sin \phi$

t-dependent measurements: $D^0 \rightarrow K_s^0 \pi^+ \pi^-$

- This three body decay proceeds via many intermediate states, like

$$\text{CF: } D^0 \rightarrow K^{*-} \pi^+$$

$$\text{DCS: } D^0 \rightarrow K^{*+} \pi^-$$

$$\text{CP: } D^0 \rightarrow \rho^0 K_s^0$$

- Matrix element is Dalitz space dependent, so also time distribution is

$$\frac{dN_{D^0 \rightarrow f}}{dt} \propto e^{-\Gamma t} \left| \mathcal{A}(m_-^2, m_+^2) + \frac{q}{p} \left(\frac{y + ix}{2} \Gamma t \right) \overline{\mathcal{A}}(m_-^2, m_+^2) \right|^2$$

- Total amplitude \mathcal{A} parametrized as a sum of quasi-two-body amplitudes of resonances \mathcal{A}_r

$$\mathcal{A}(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2)$$

- Both mixing parameters, x and y as well as CPV parameters ϕ and $|q/p|$ can be measured
- 3D fit in (m_-^2, m_+^2, t) ; many free parameters